

# Introduction to theoretical quantum CRYPTOGRAPHY

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School of Computer Science  
McGill University

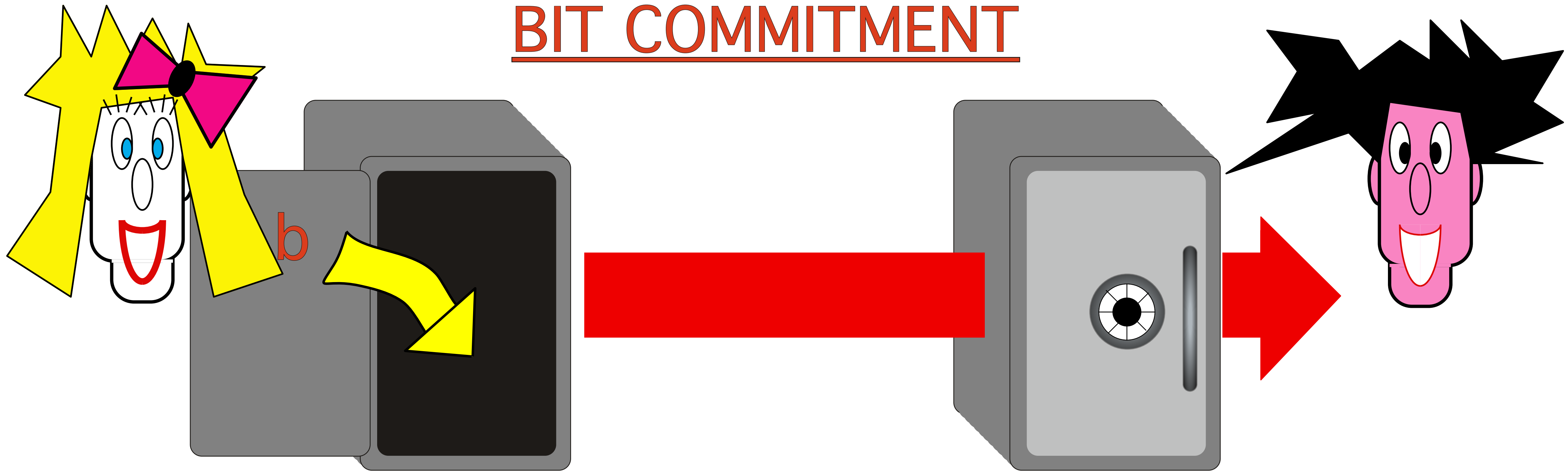


**(4)**

**two-party**

**Cryptographic Protocols**

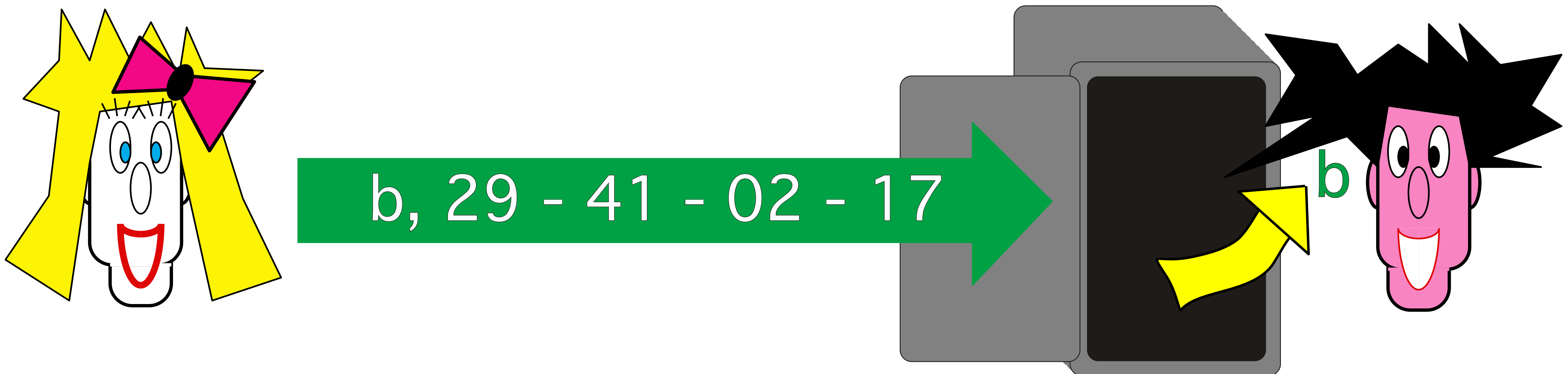
# BIT COMMITMENT



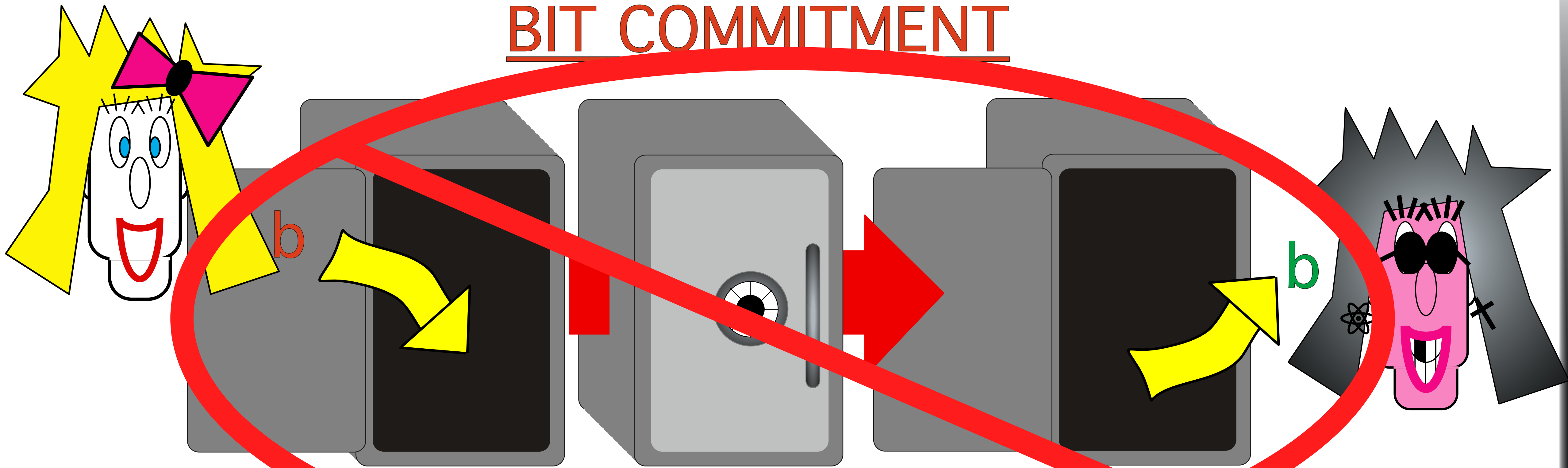
COMMIT

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UNVEIL

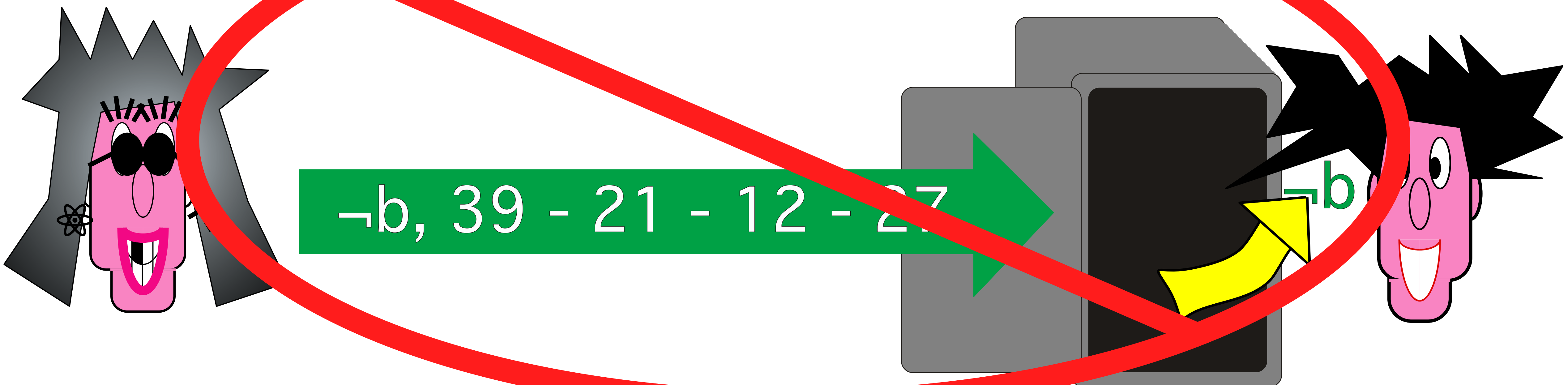


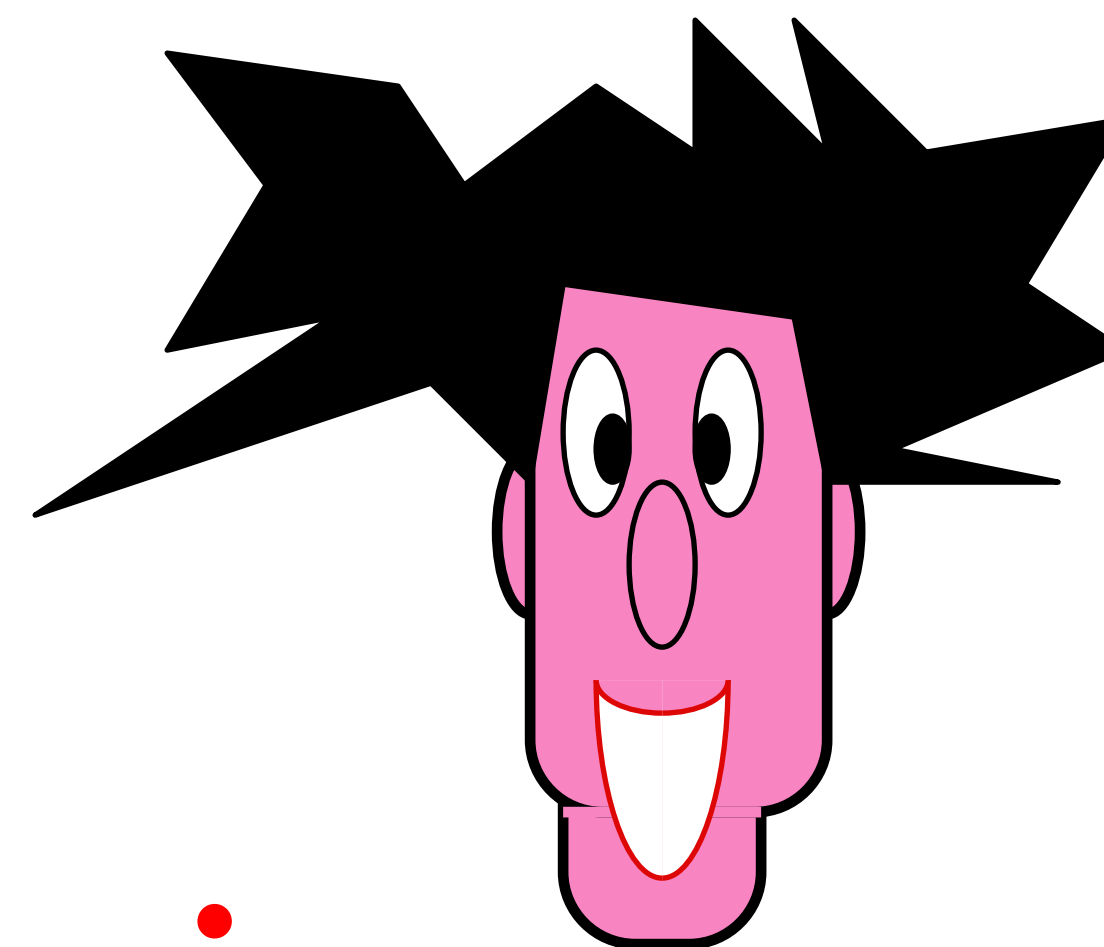
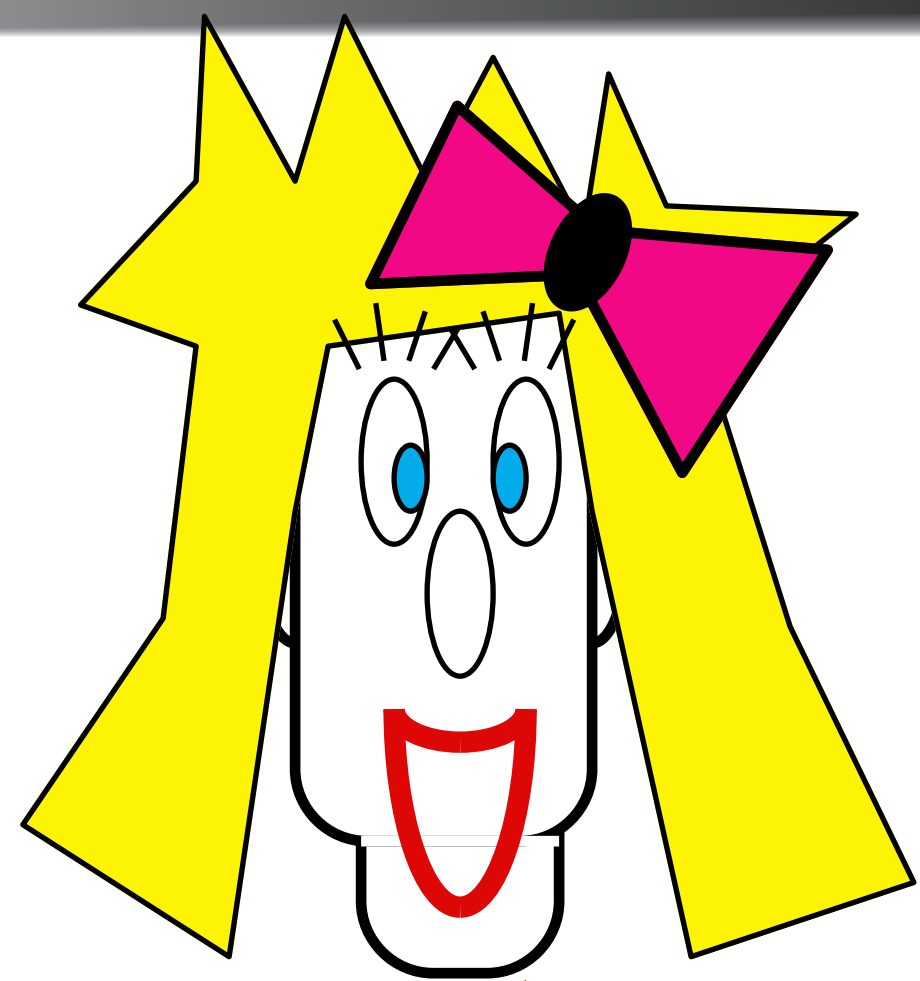
# BIT COMMITMENT



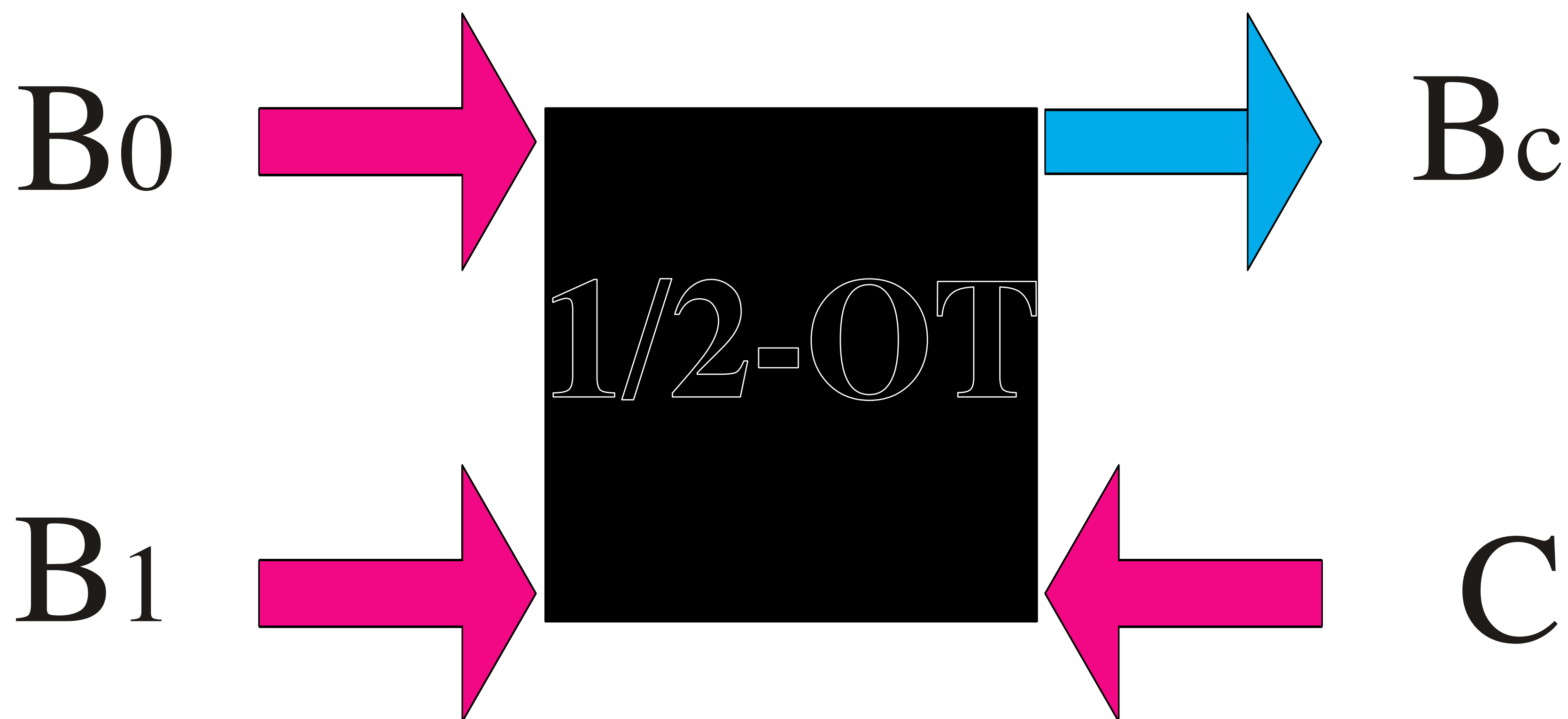
CONCEALING

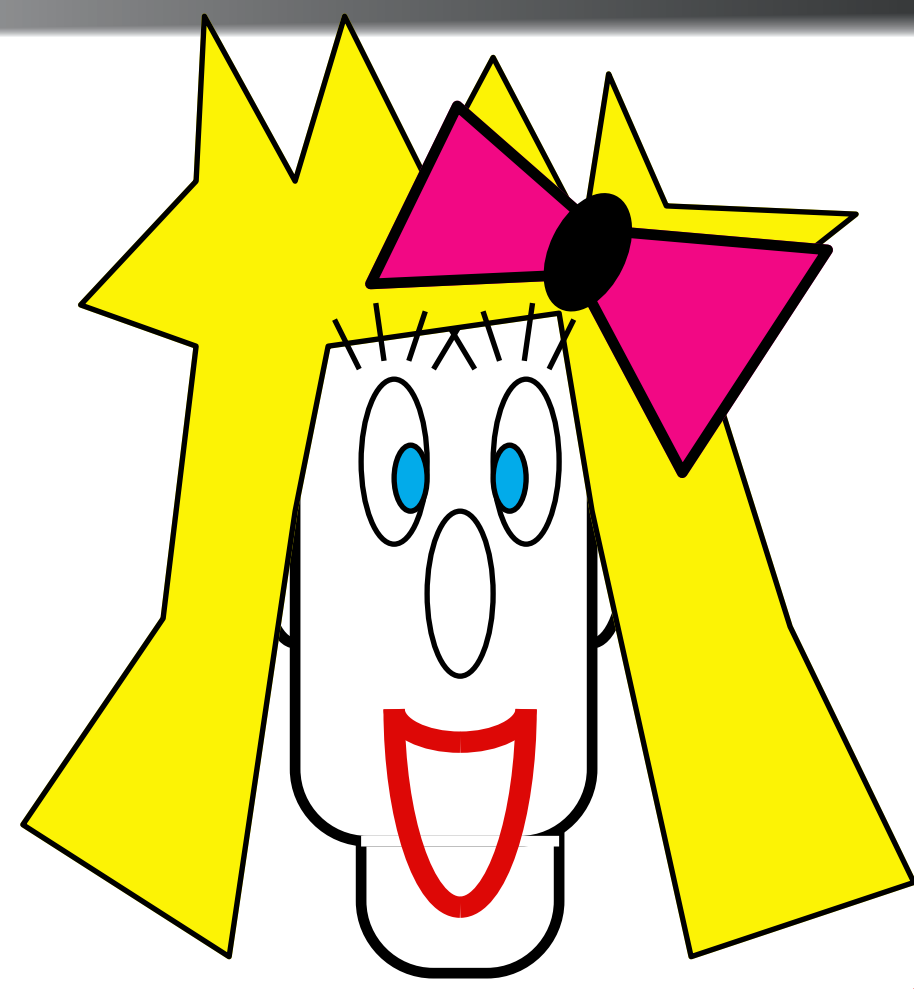
## BINDING



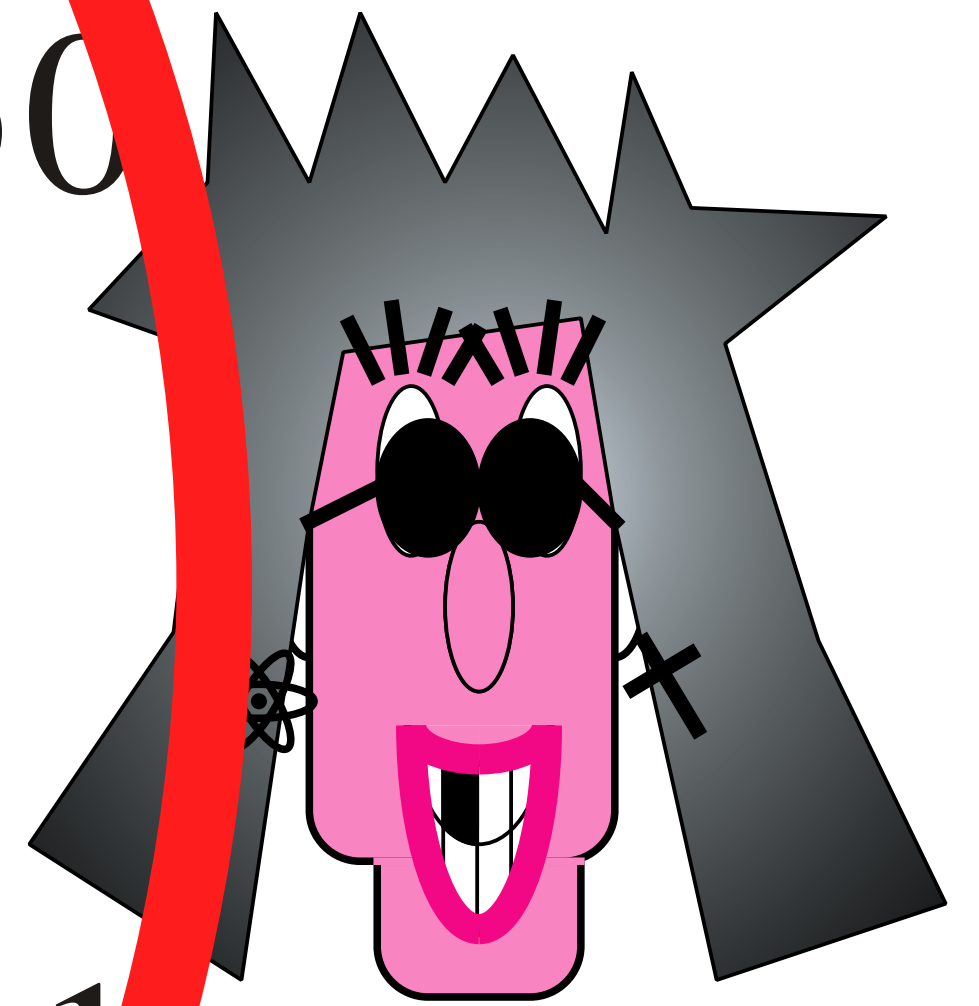
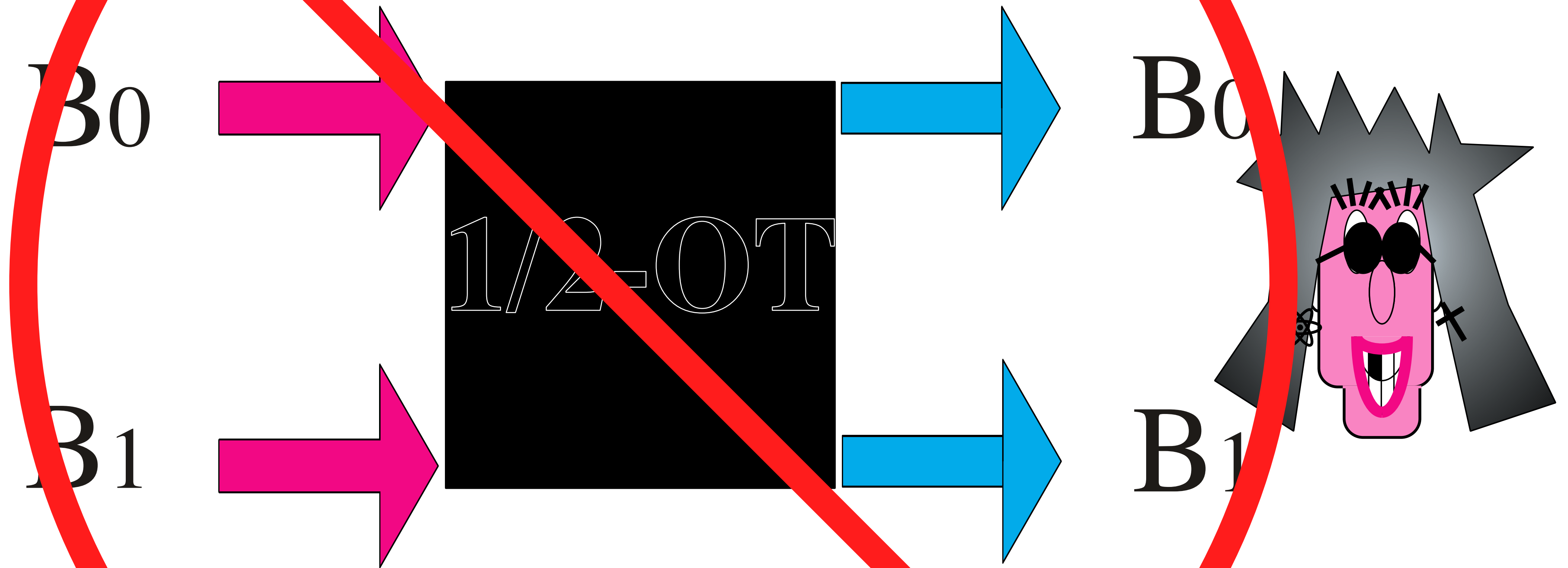


# Oblivious Transfer (message multiplexing)

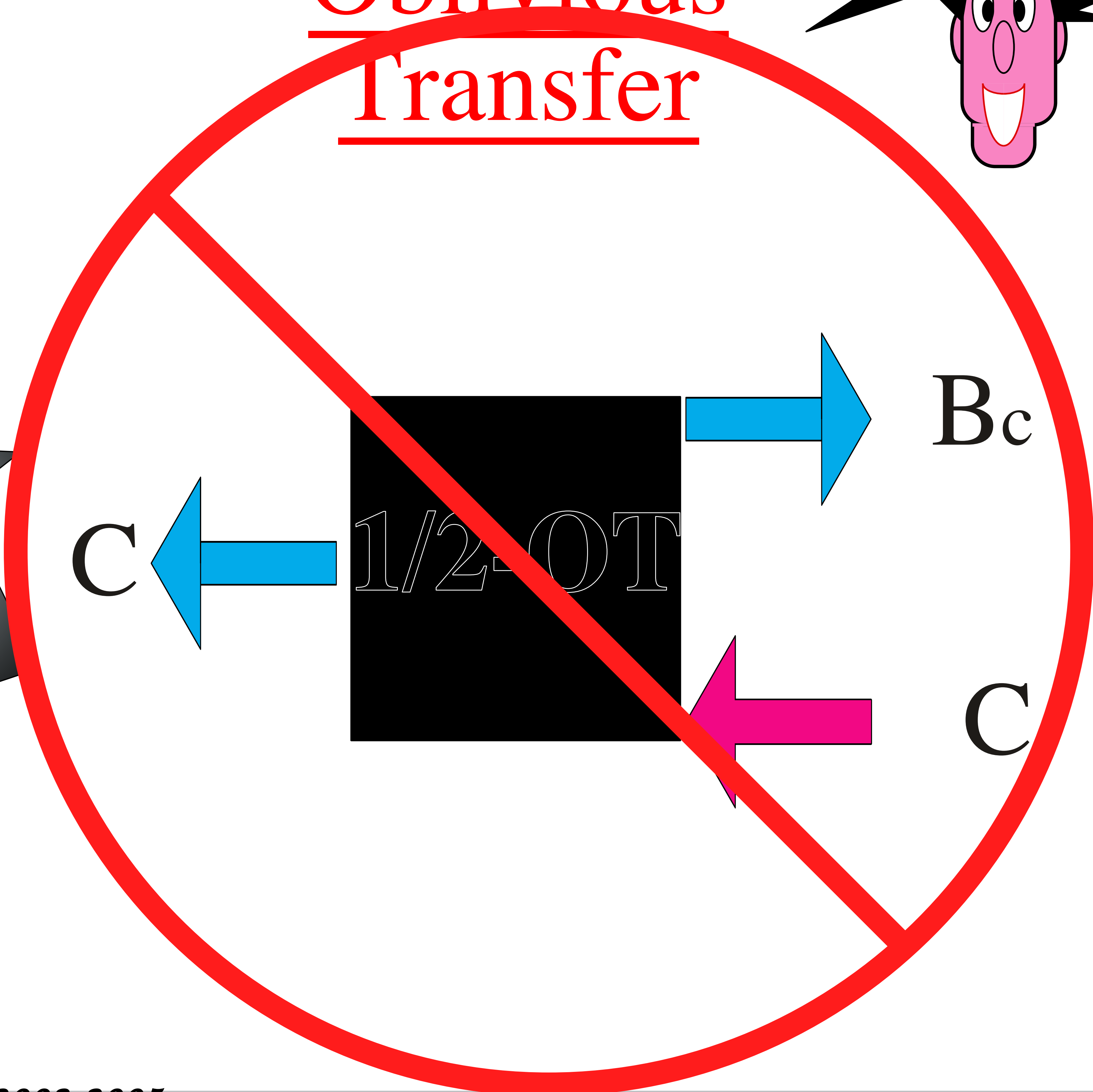
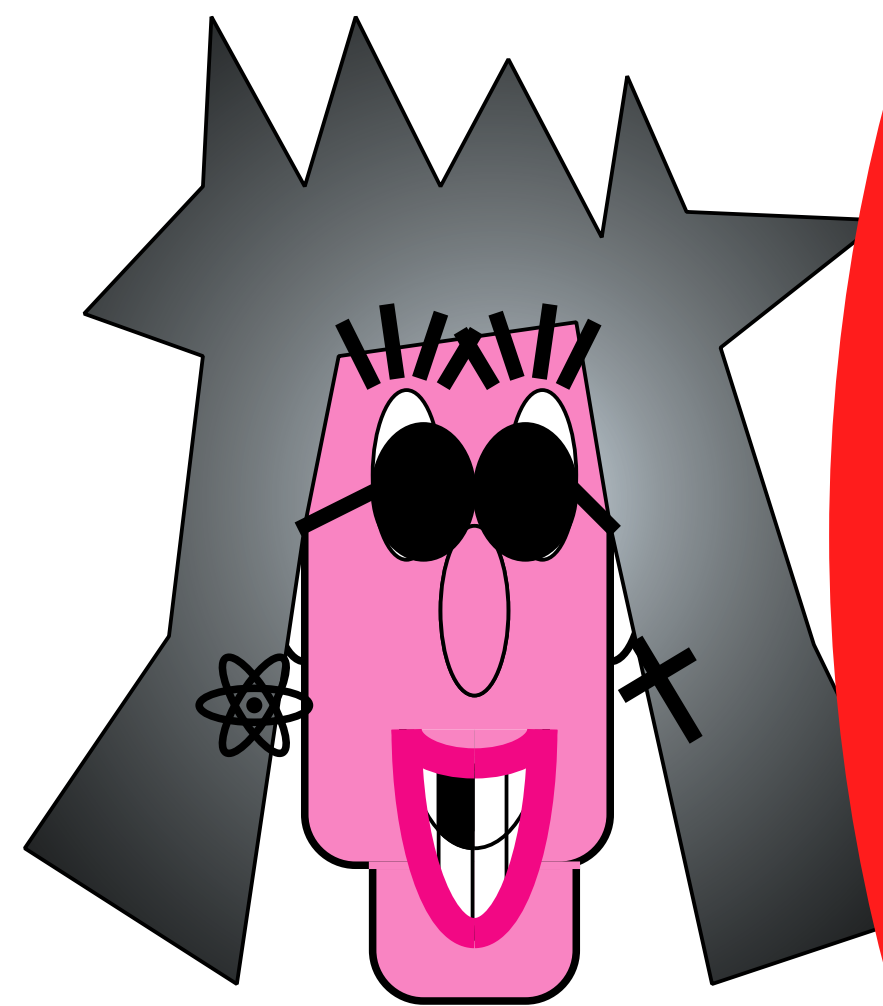
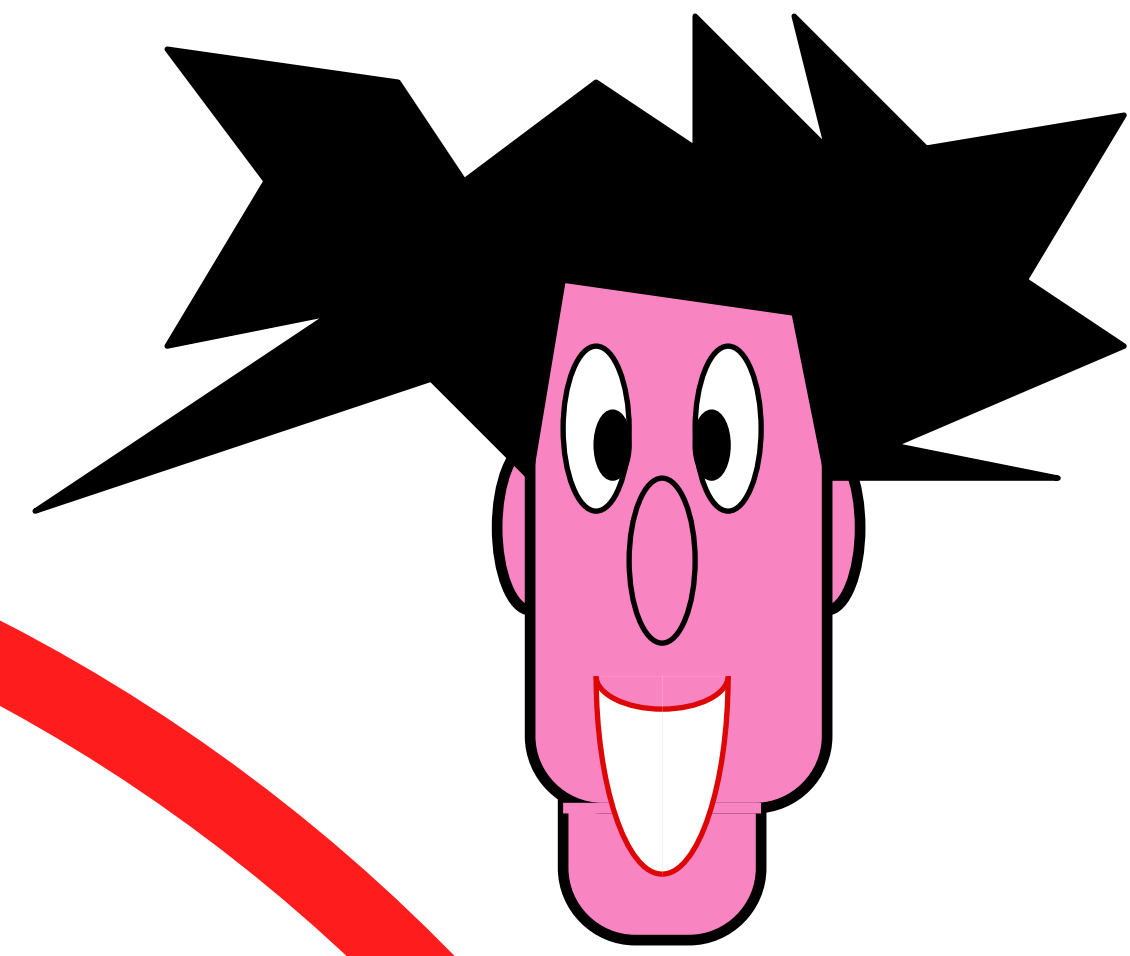


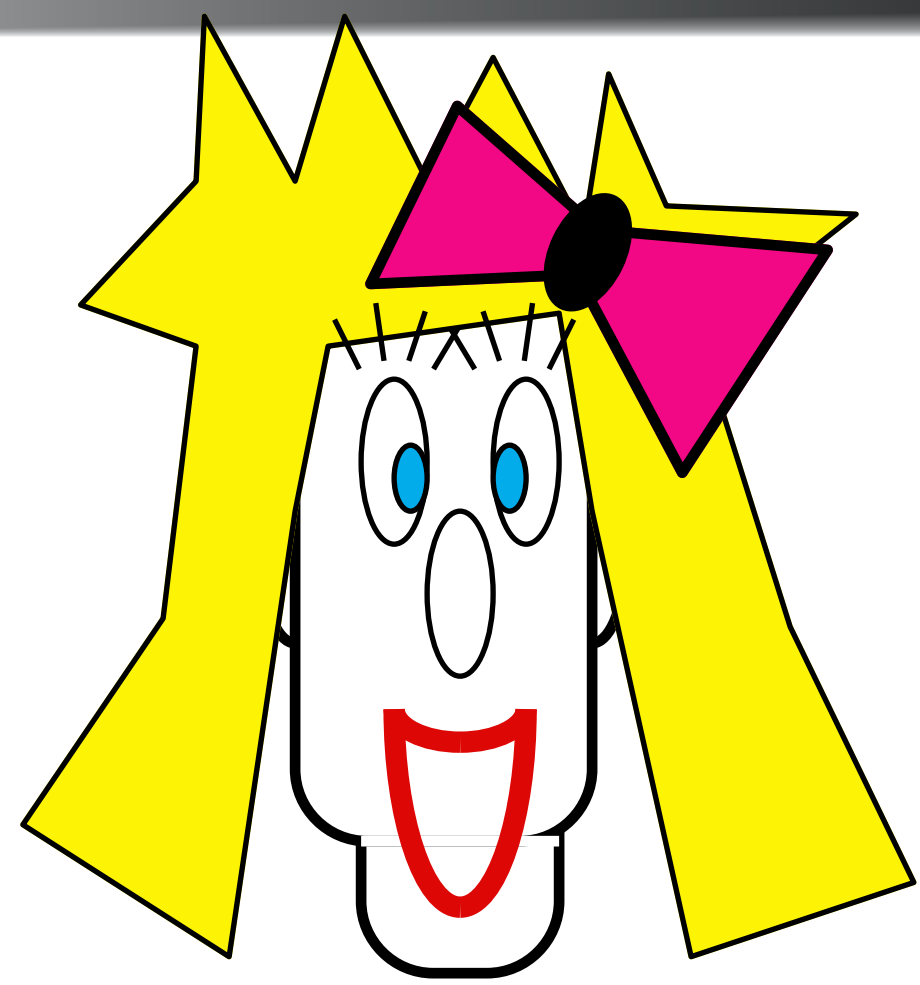


# Oblivious Transfer

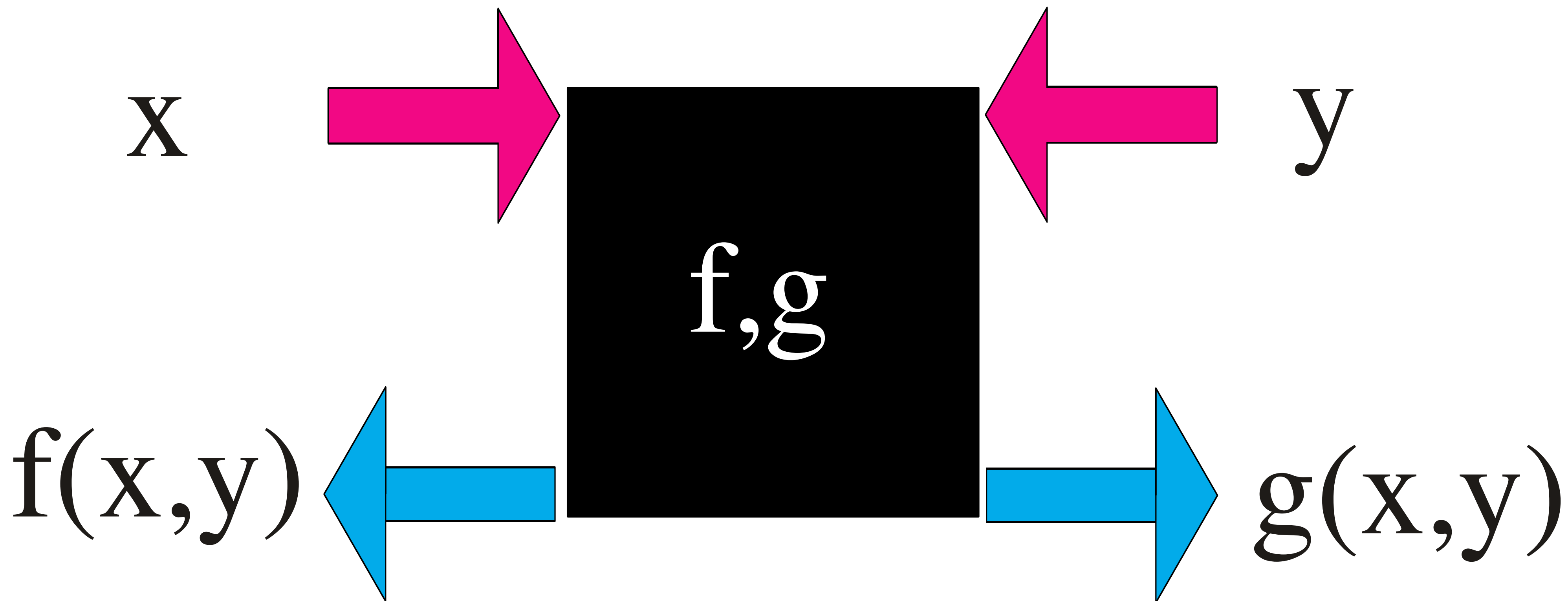
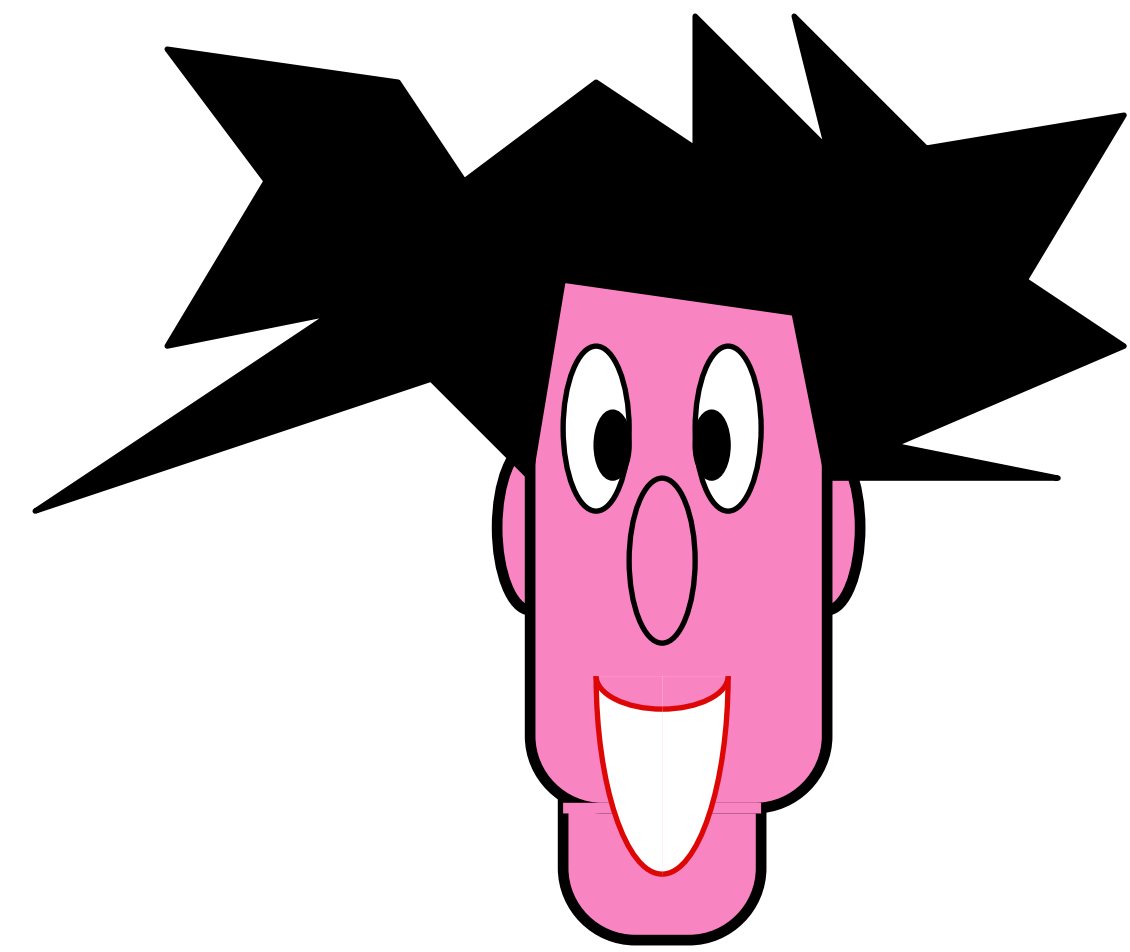


# Oblivious Transfer

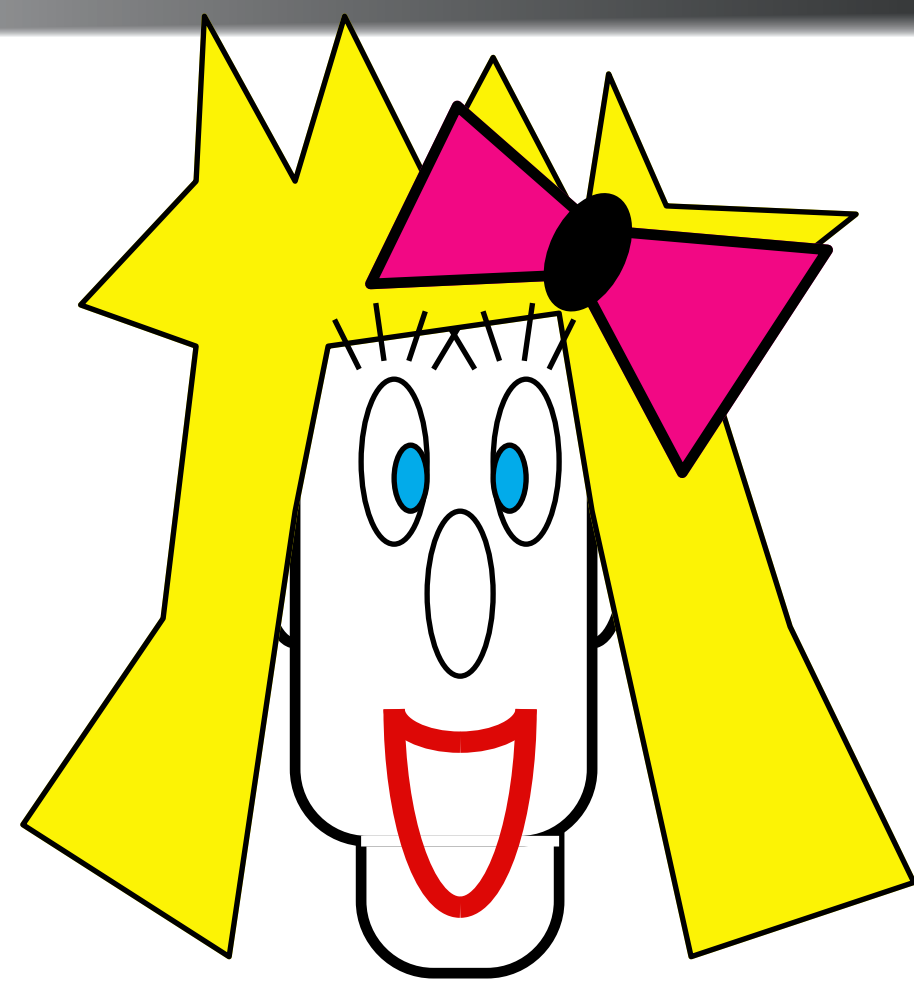




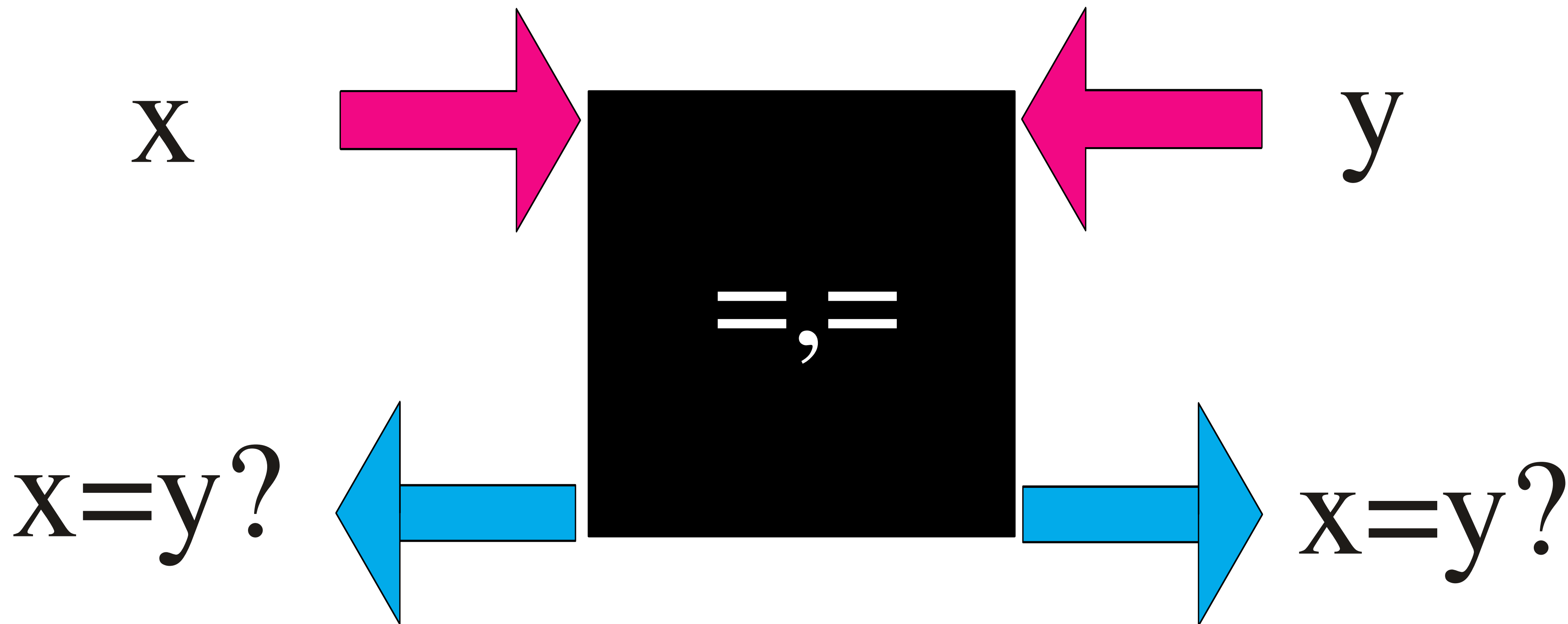
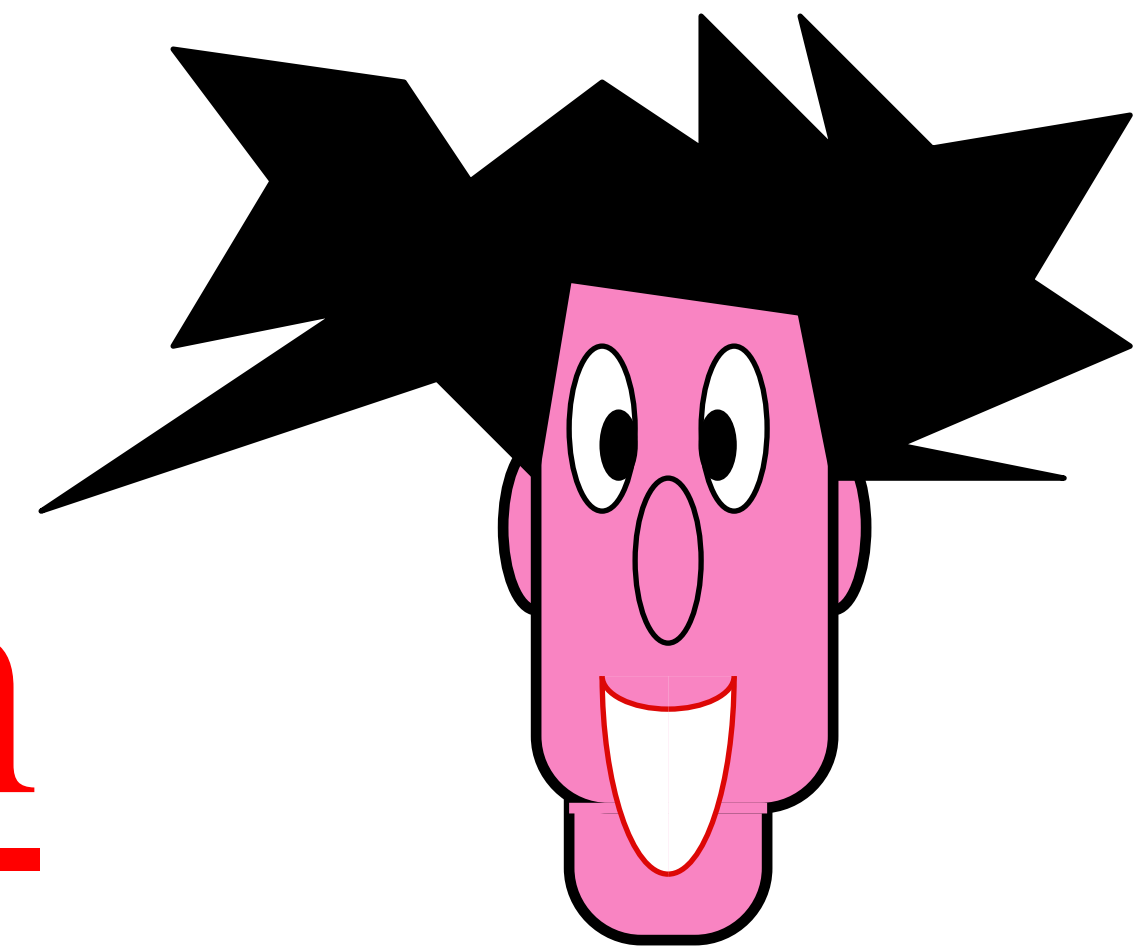
# Oblivious Function Evaluation



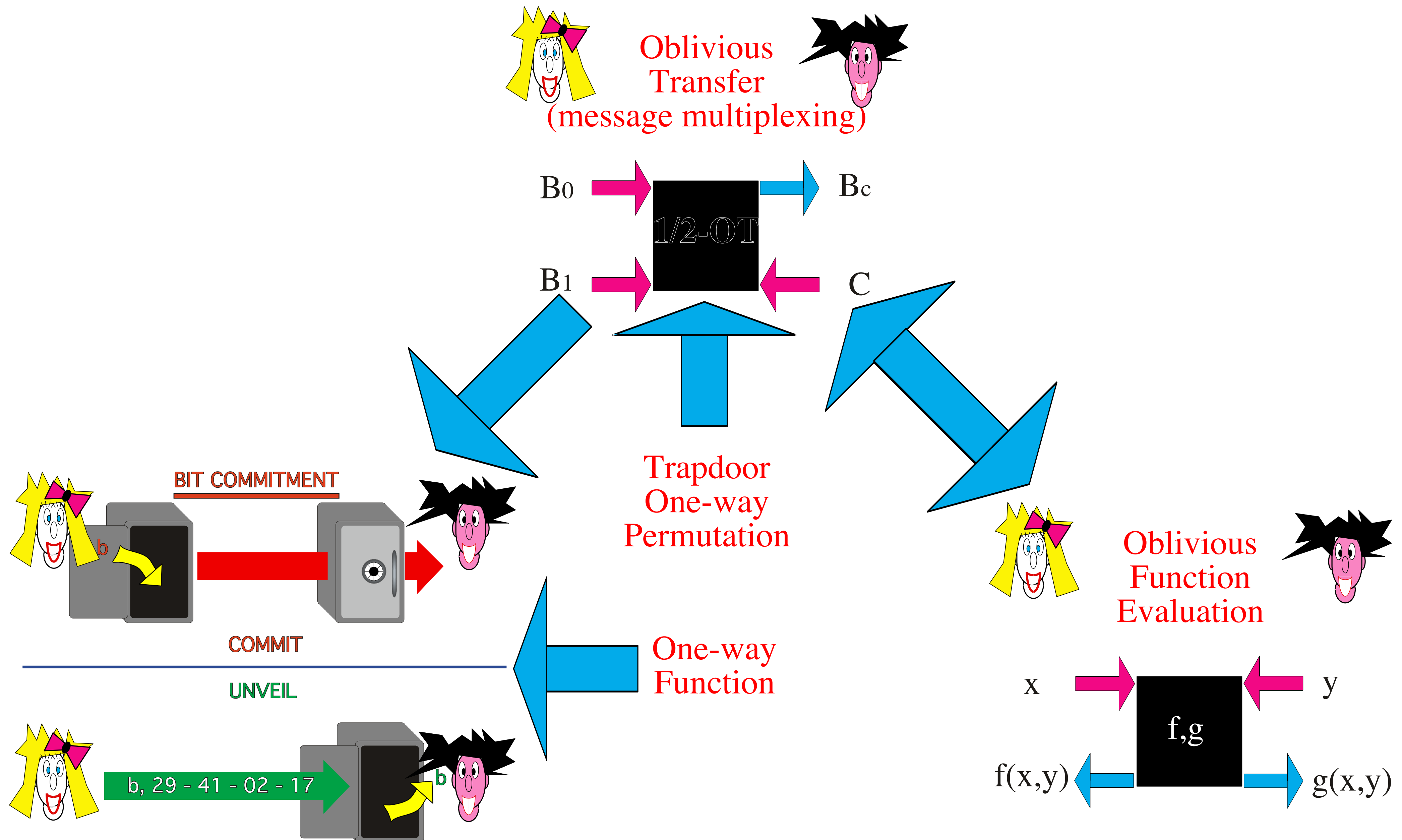




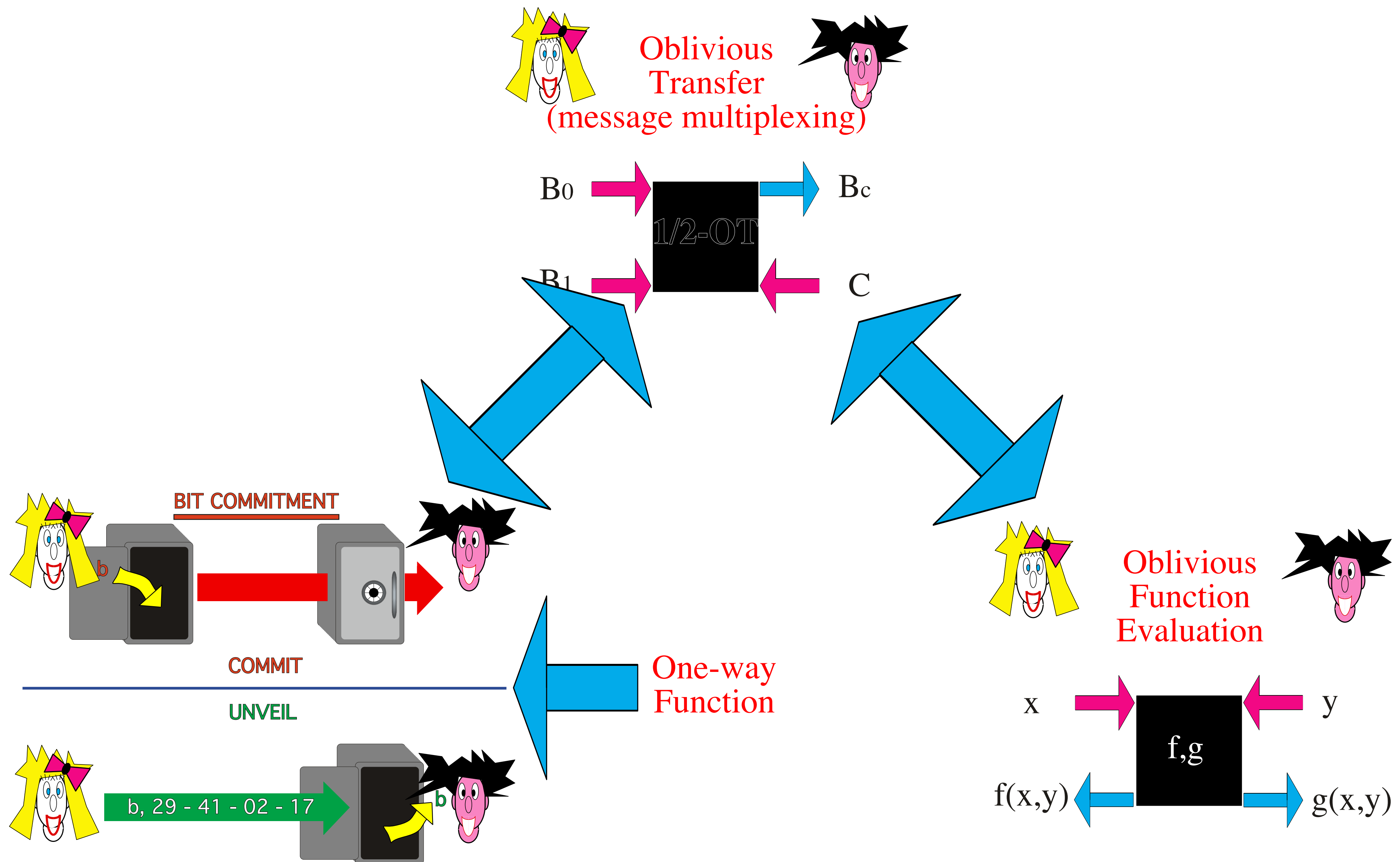
# Mutual Identification



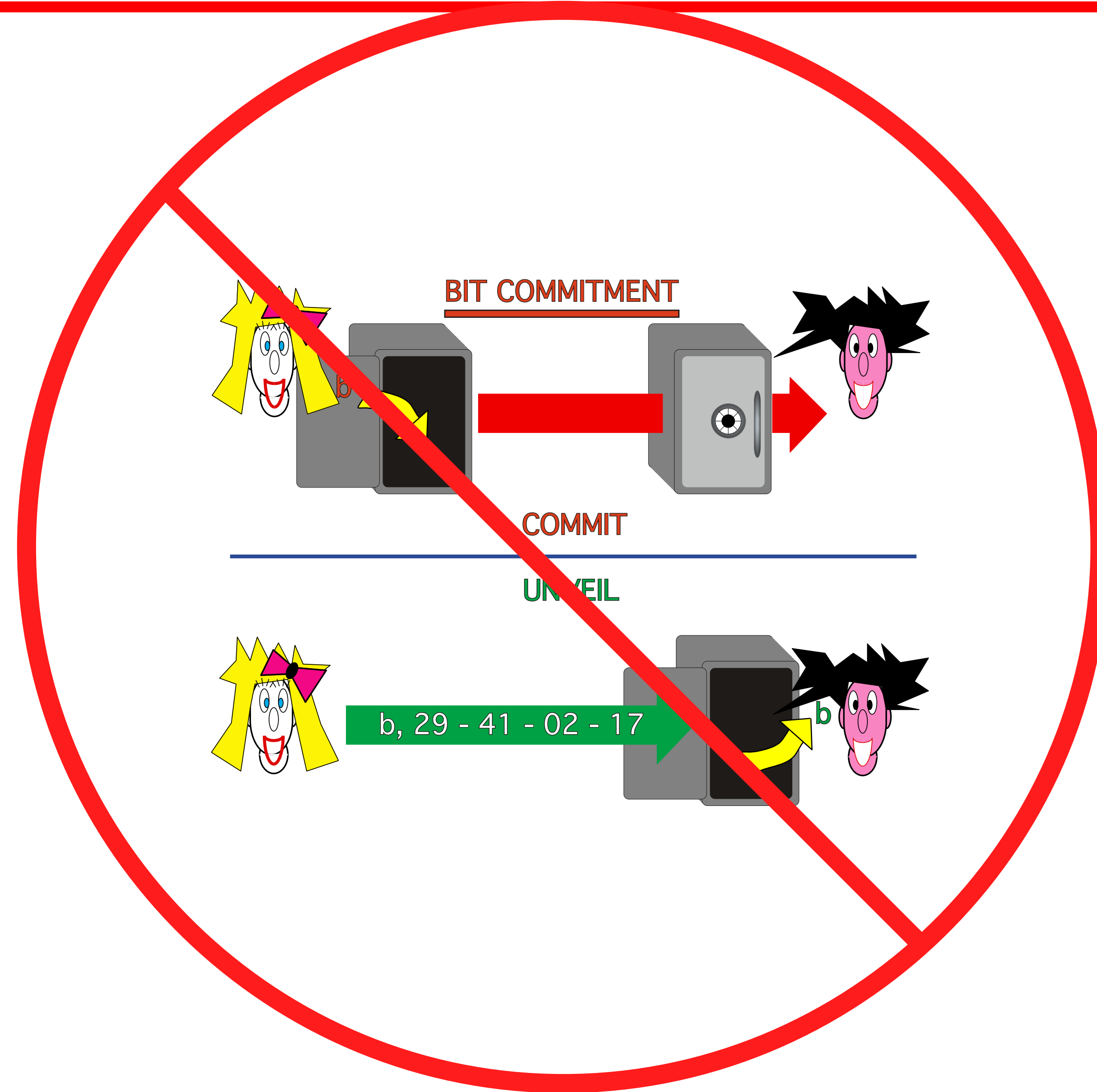
# Classically



# Quantumly

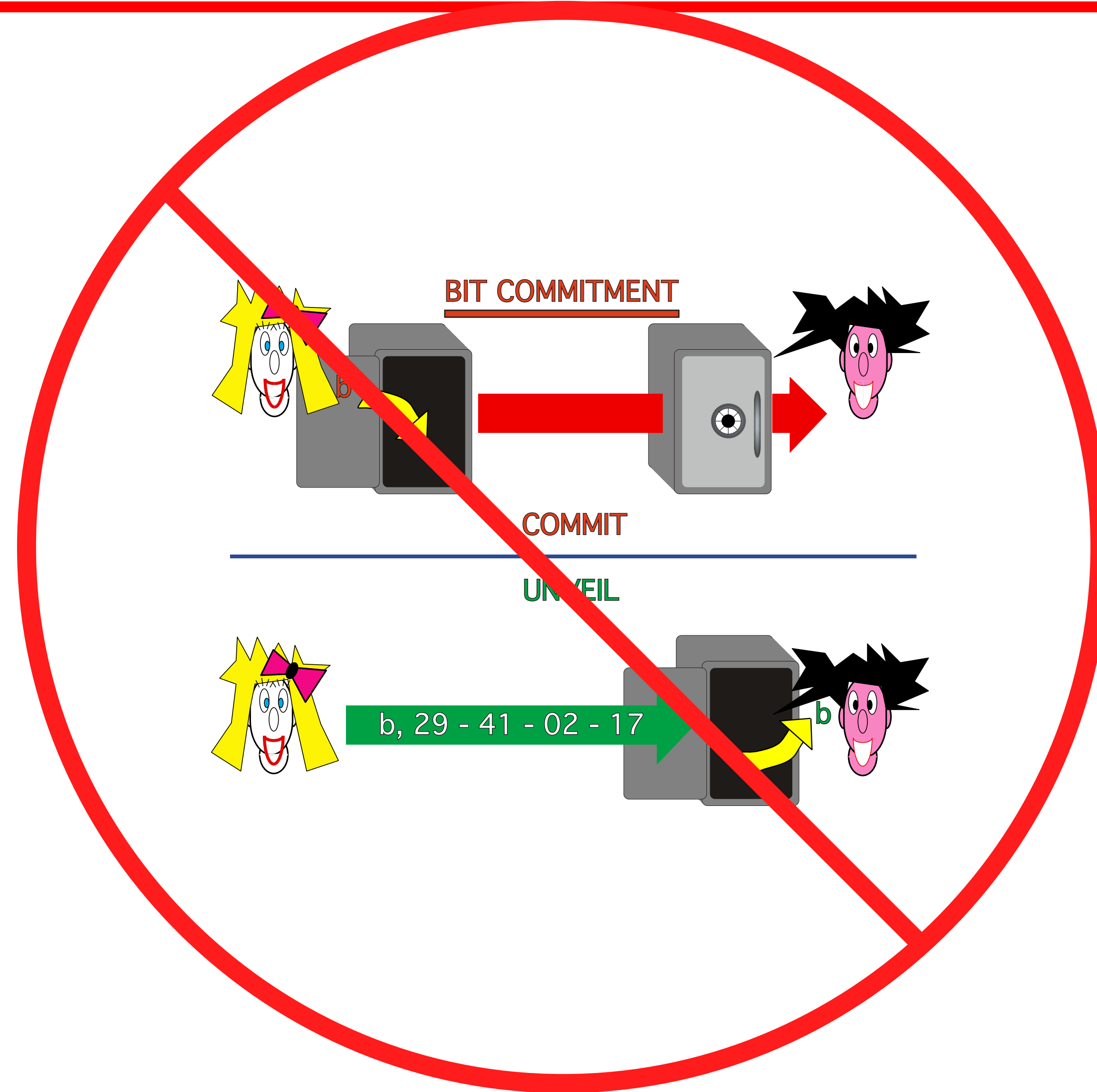


# Classically (information theoretical)



Folklore

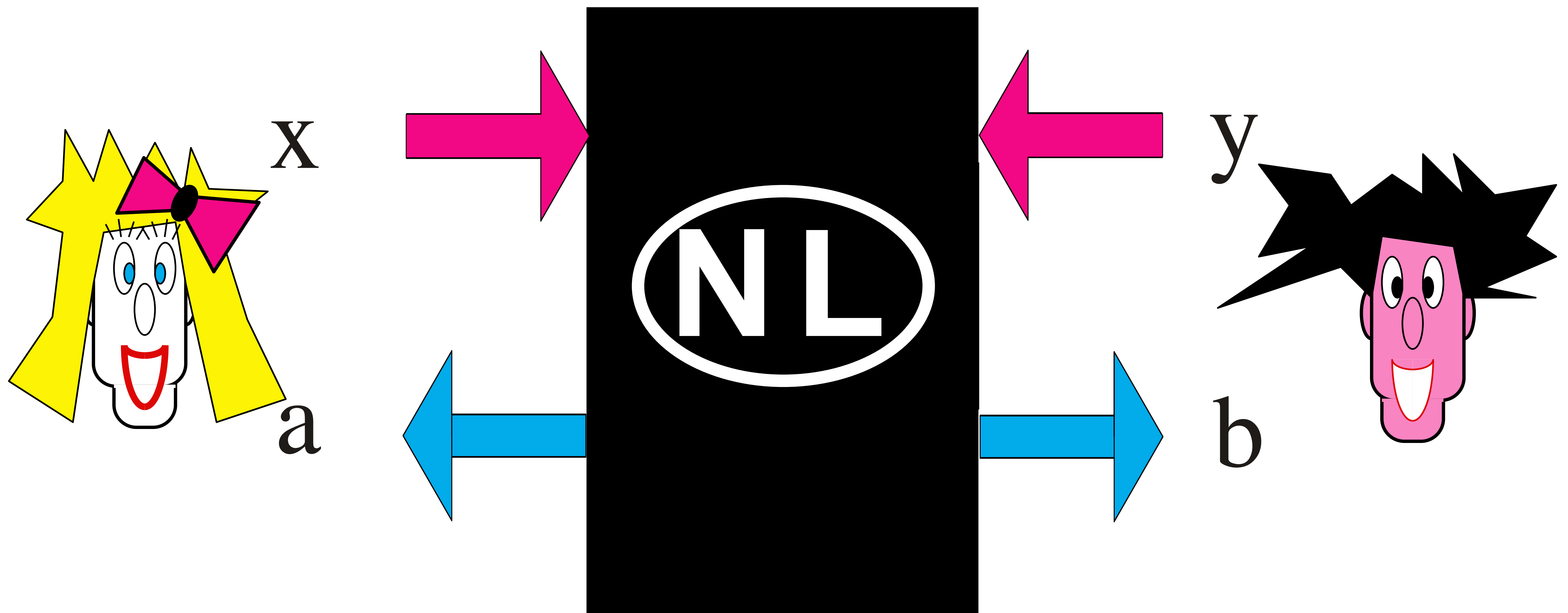
# Quantumly (information theoretical)



Mayers, Lo-Chau

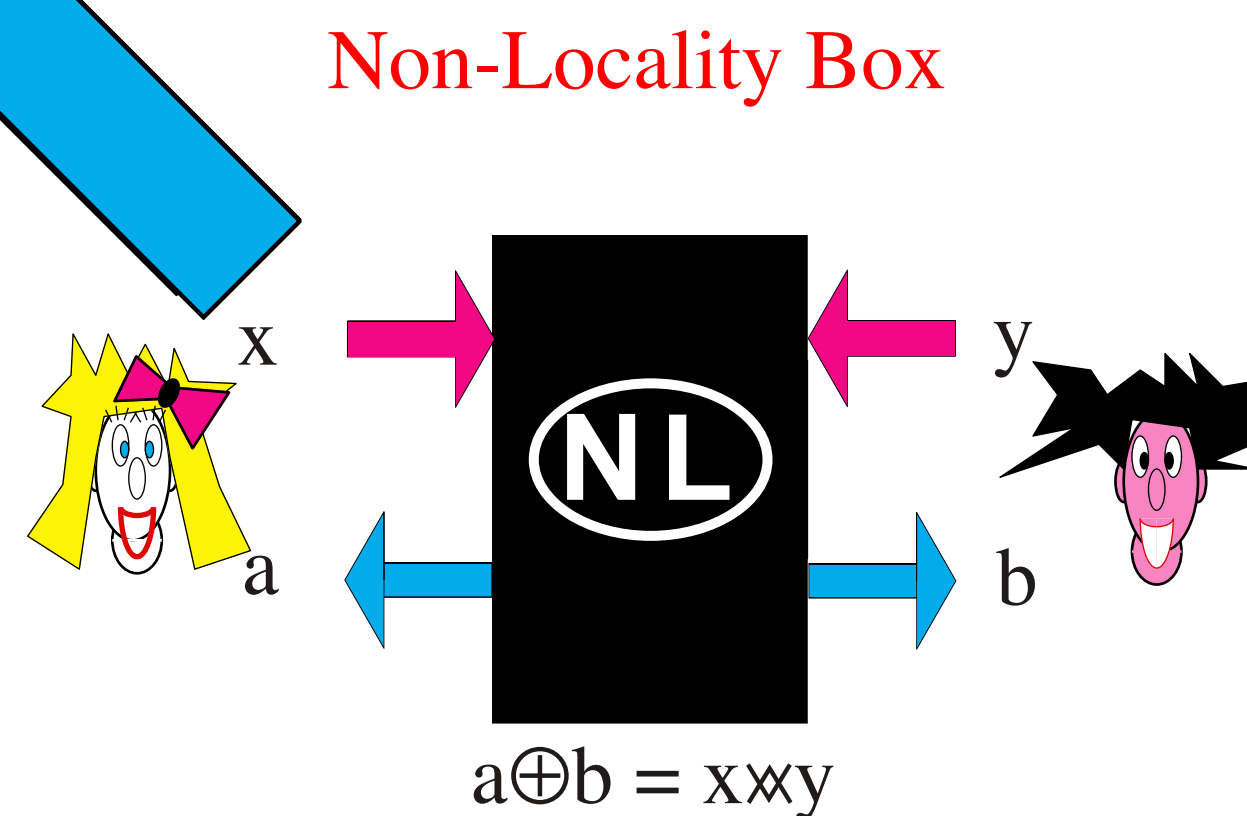
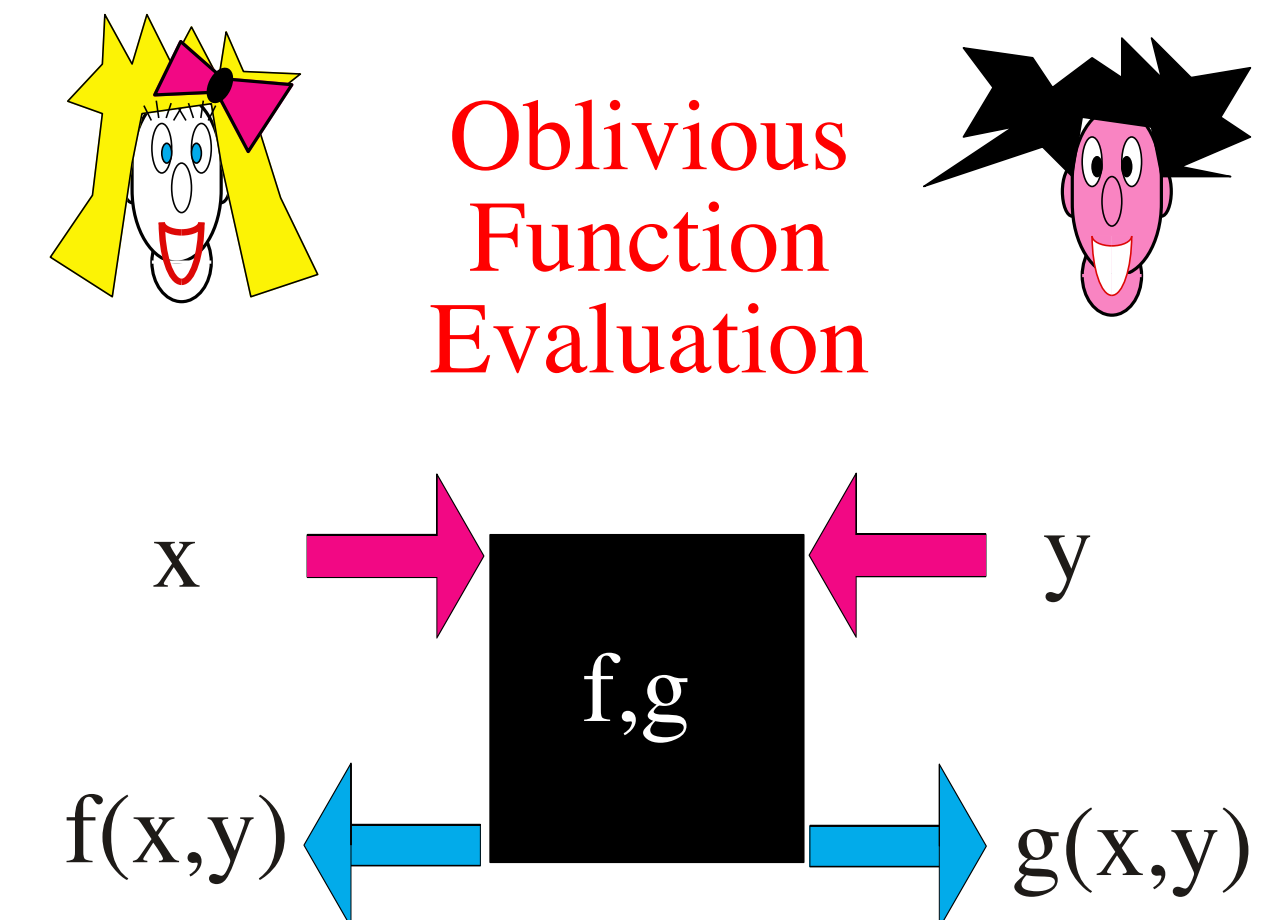
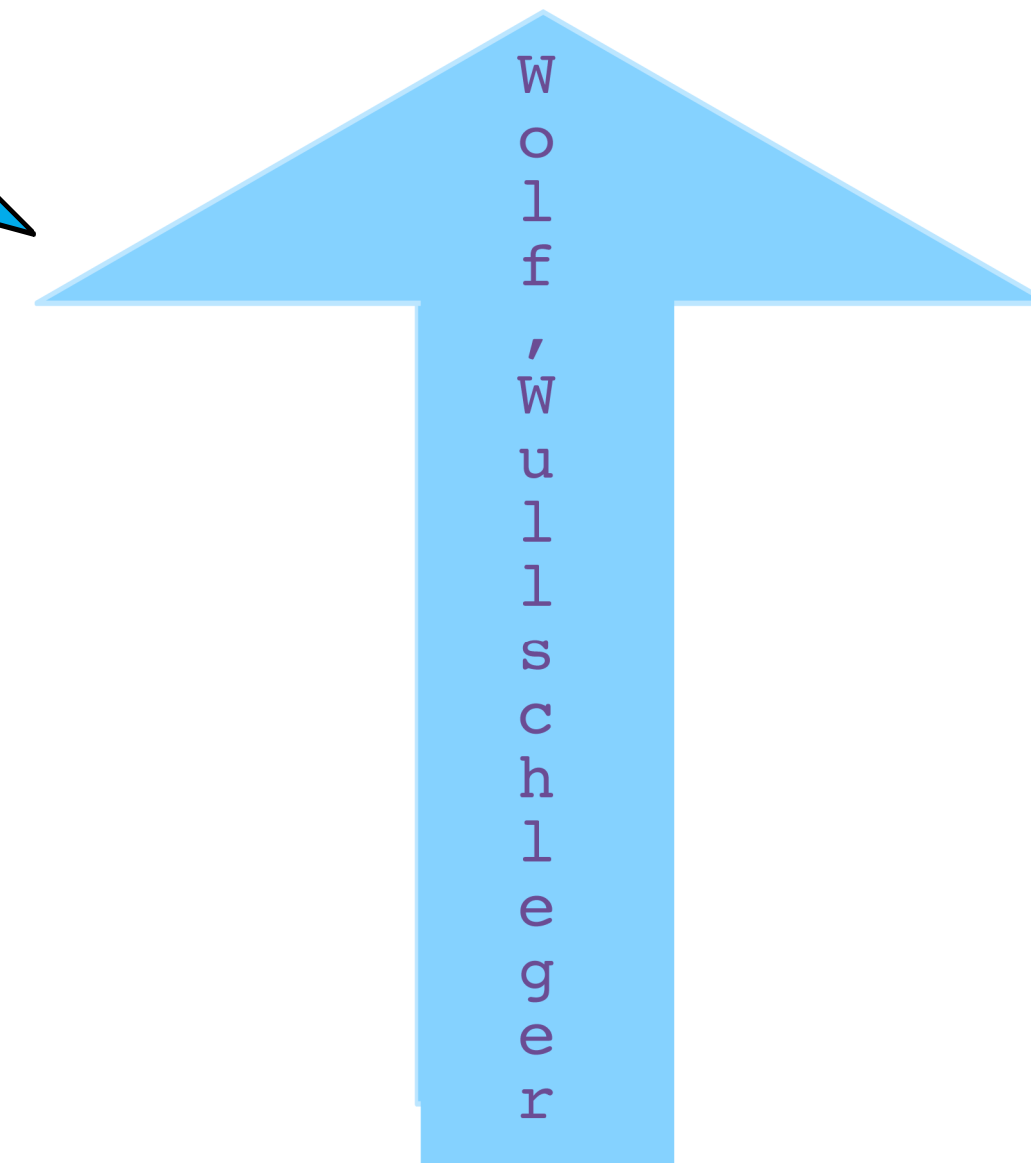
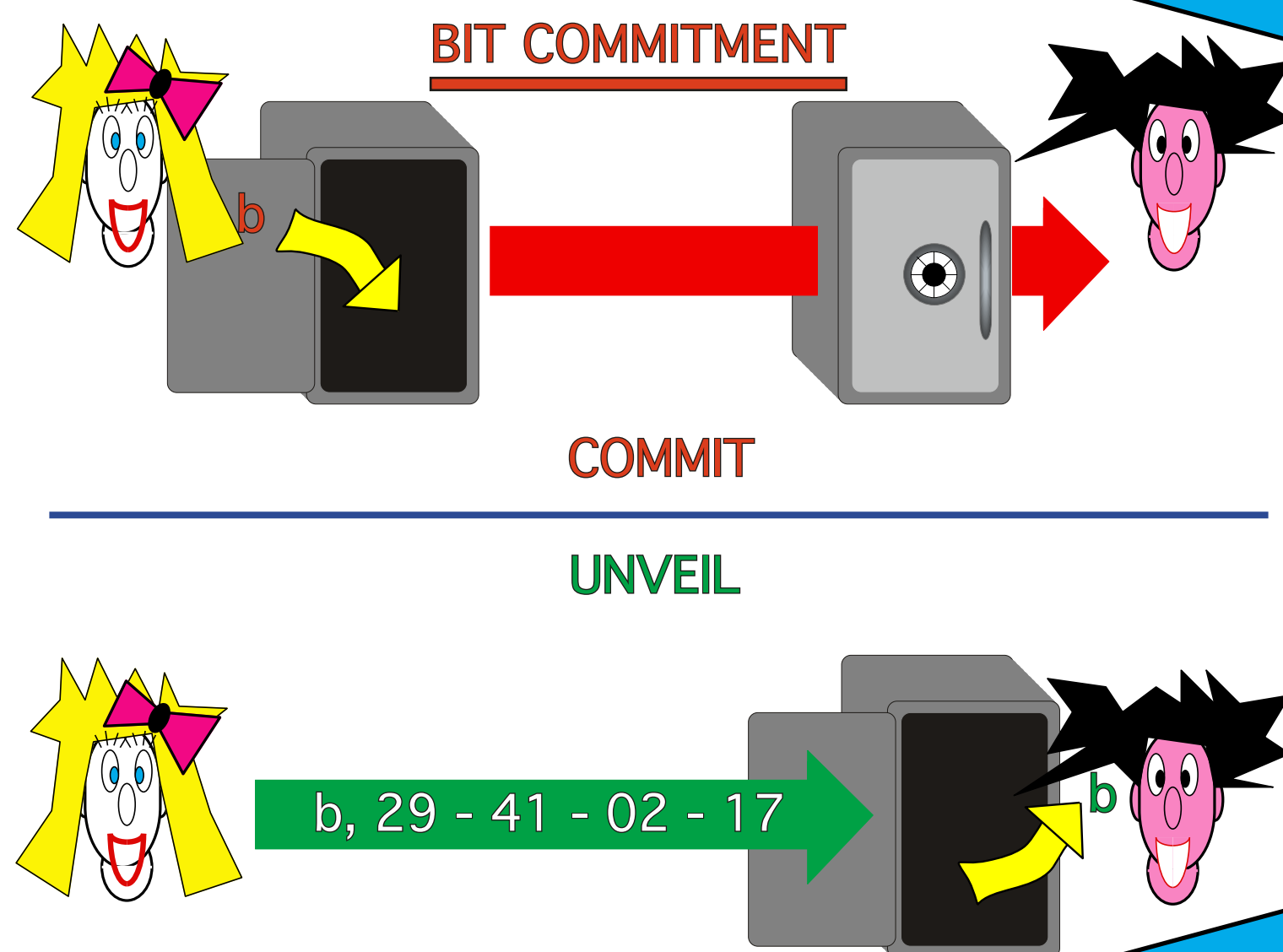
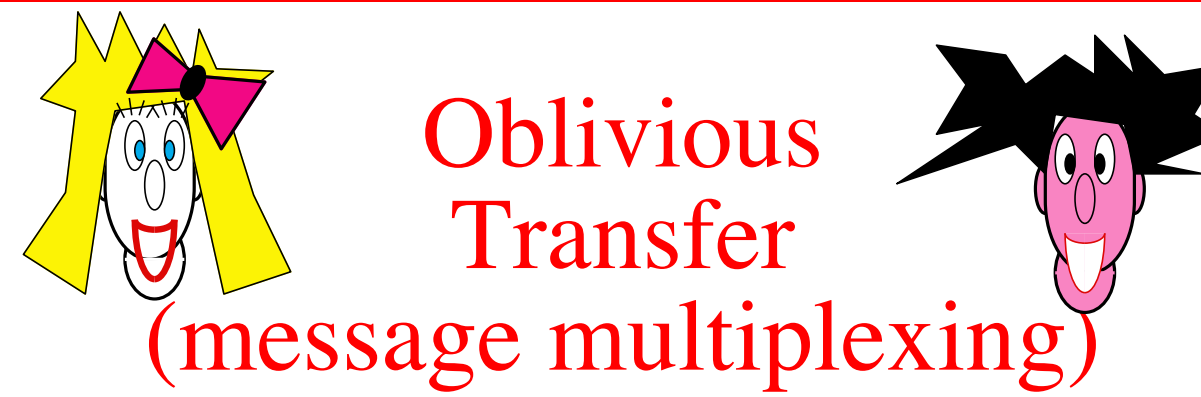
# Non-Locality Box

$$a \oplus b = x \otimes y$$



$$C: 3/4 \quad Q: \cos^2(\pi/8) \approx 85\%$$

# Quantumly



- 1) Wolf, Wullschlegler ?
- 2) Short, Gisin, Popescu
- 3) Buhrman, Christandl, Unger, Wehner, Winter

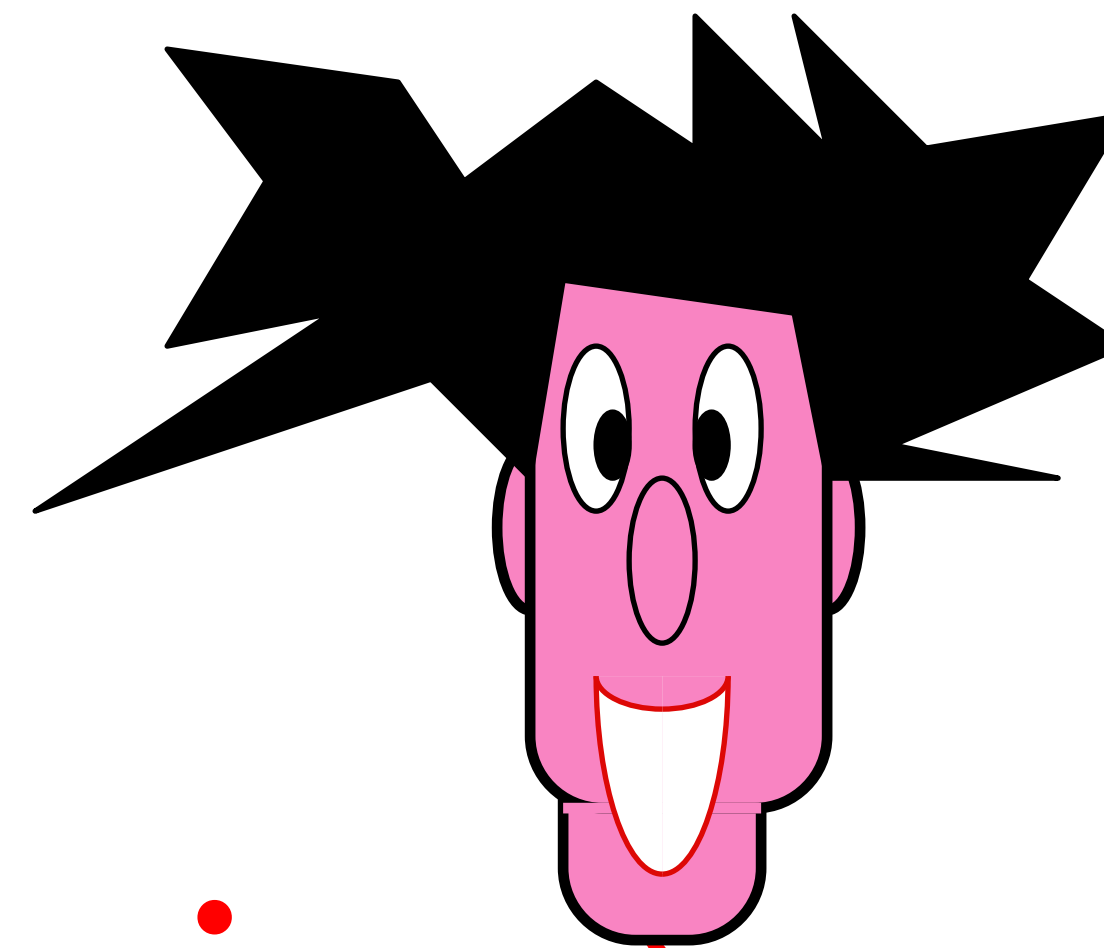
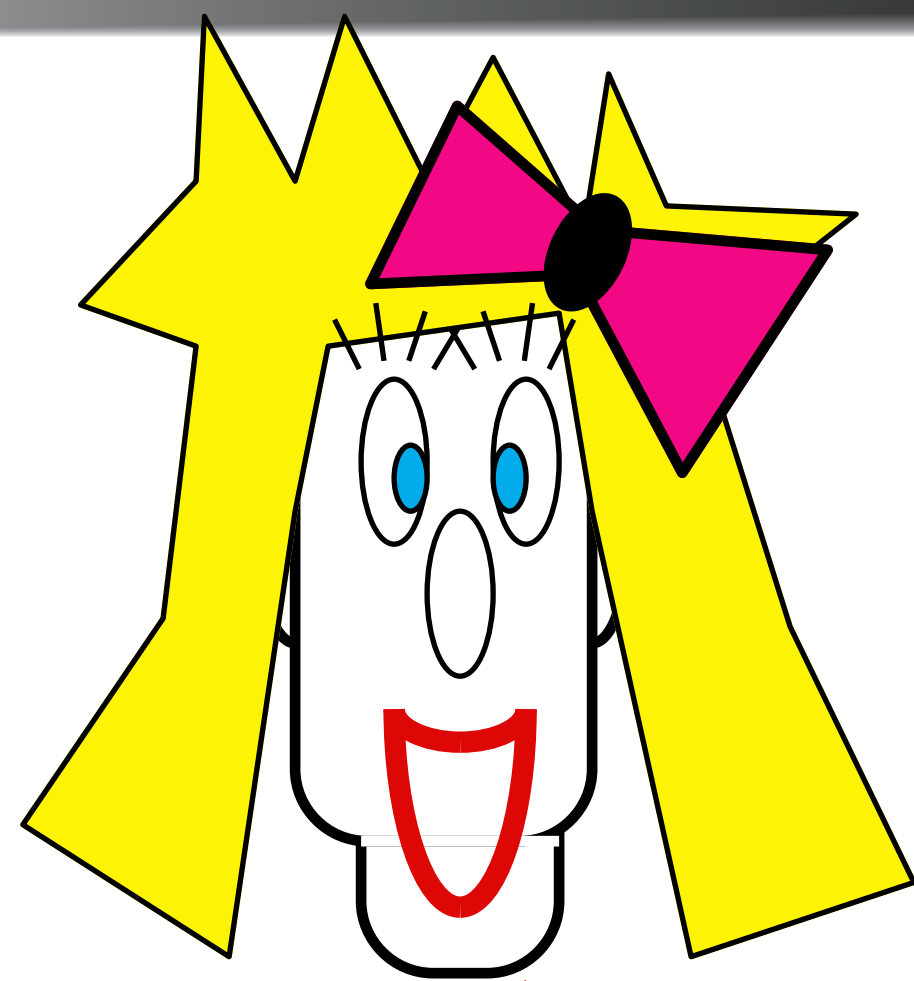
**(5)**

**Quantum**

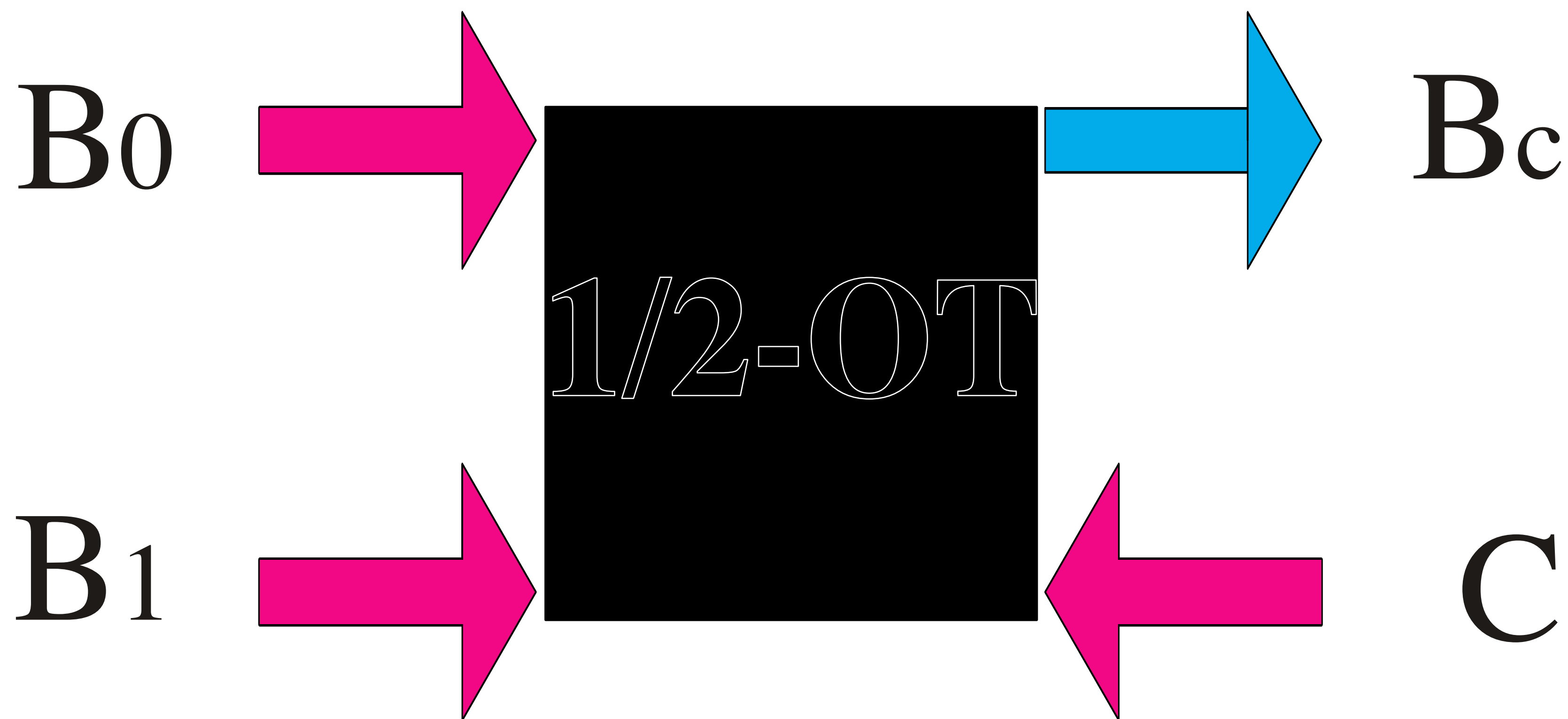
**Oblivious**

**Transfer**

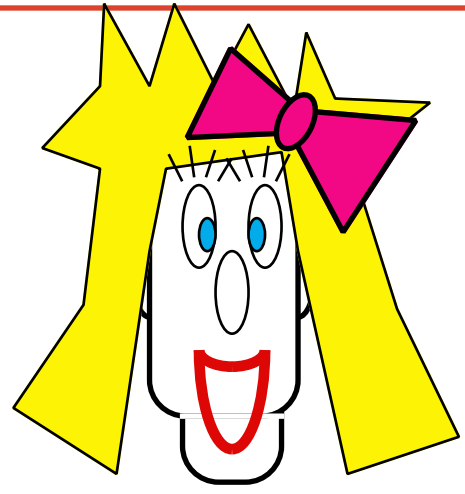




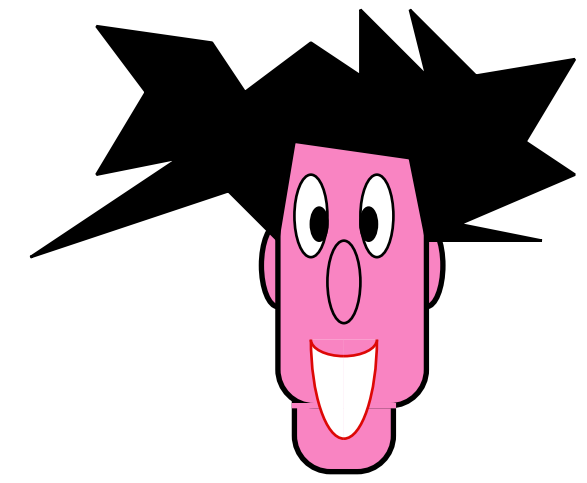
# Oblivious Transfer (message multiplexing)



# Q-OT



$b_0$   $b_1$



A: 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0  
 × + × + + + × × × × + + + + × × × + × + + + × +

B: × × + + × + + + × + + × × × + × × × + + × + × +  
 0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0

A: × + × + + + × × × × + + + + × × × + × + + + × +

B: 0 ↘ ↘ 0 ↘ 1 ↘ ↘ 1 ↘ 0 ↘ ↘ ↘ ↘ 1 0 ↘ ↘ 1 ↘ 0 0 0

B: 0 0 1 1 0 1 0 1 0 0 0 ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘

A: 0 0 1 1 0 1 0 1 0 0 0 1 1 0 0 0 1 1 0 0 0 1 0 1

B: 0 0 1 1 0 1 0 1 = 0 ↘ = ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘ ↘

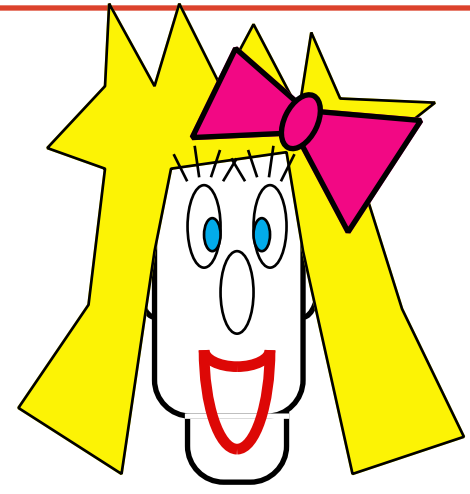
A: 0 0 1 1 0 1 0 1 = 0 0 = 1 1 0 0 0 1 0 1

A:  $\oplus$   $b_0$   $\oplus$   $b_1$

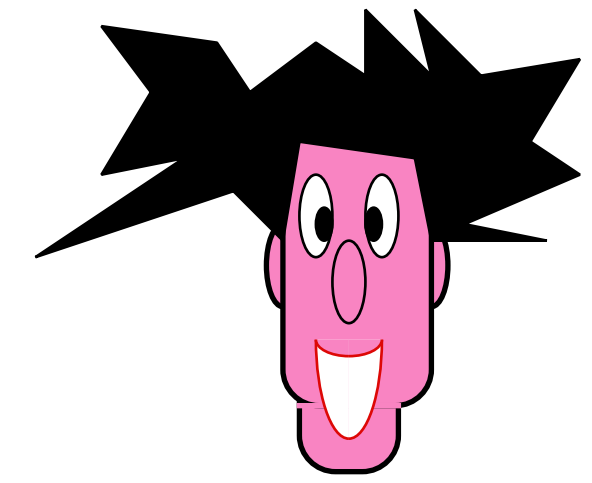
B:  $b_0 = 0$  ↘ = ↘

## Crépeau-Kilian

# Q-OT

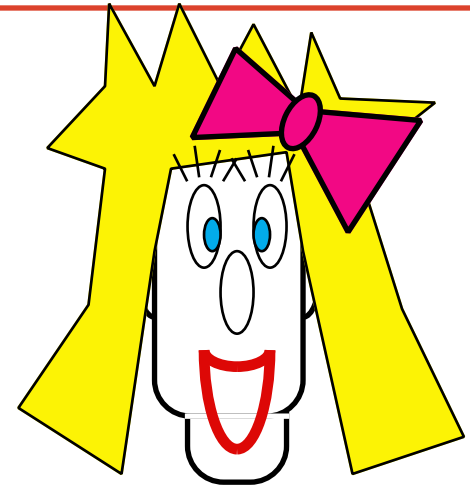


$b_0$   $b_1$

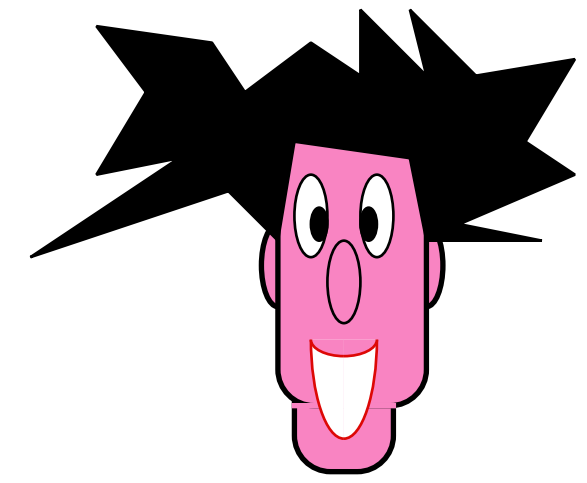


A: 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0  
× + × + + + × × × × + + + + × × × + × + + + × +

# Q-OT



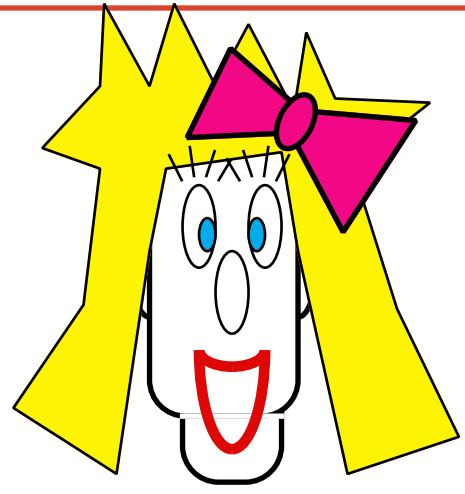
$b_0$   $b_1$



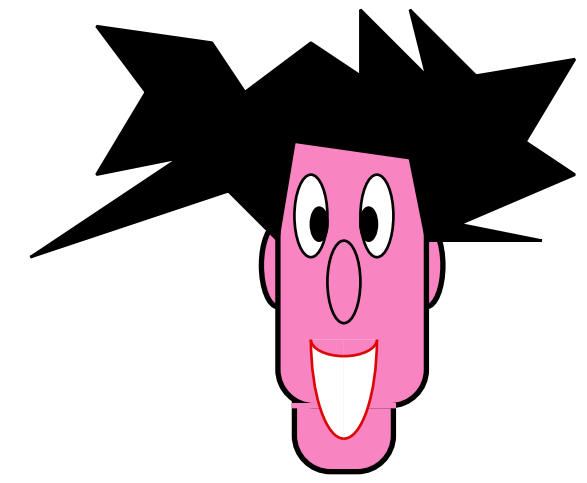
<b>A:</b>	0	1	1	0	0	1	0	0	1	1	0	1	0	0	0	1	1	1	0	1	1	0	0	0
	×	+	×	+	+	+	×	×	×	×	+	+	+	+	×	×	×	+	×	+	+	+	×	+
<b>B:</b>	×	×	+	+	×	+	+	+	×	+	+	×	×	×	+	×	×	×	+	+	×	+	×	+
	0	0	1	0	0	1	0	0	1	0	0	0	0	1	1	1	0	0	0	1	1	0	0	0

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# Q-OT



**b<sub>0</sub>** **b<sub>1</sub>**

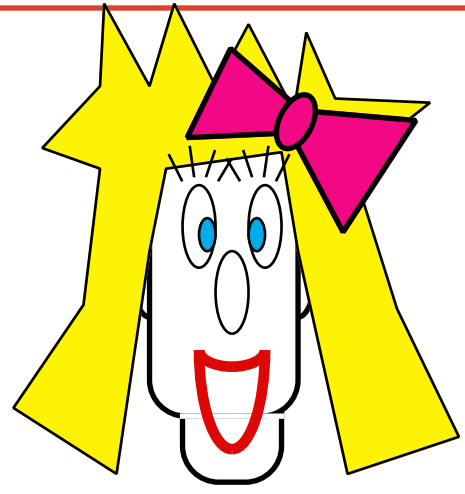


**A:** 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0  
× + × + + + × × × × + + + + × × × + × + + + × +

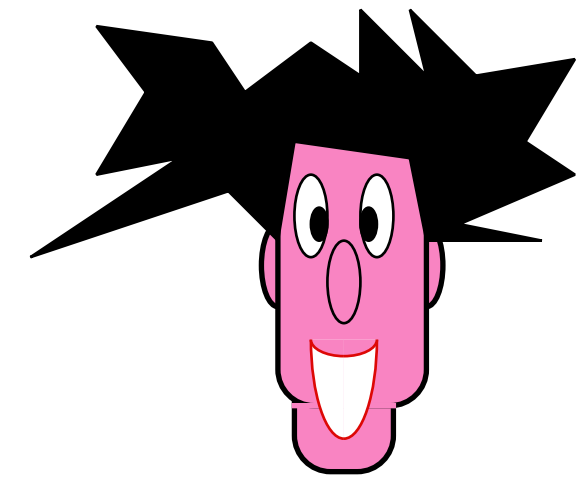
**B:** × × + + × + + + × + + × × × + × × × + + × + × +  
0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0

**A:** × + × + + + × × × × + + + + × × × + × + + + × +

# Q-OT



$b_0$   $b_1$

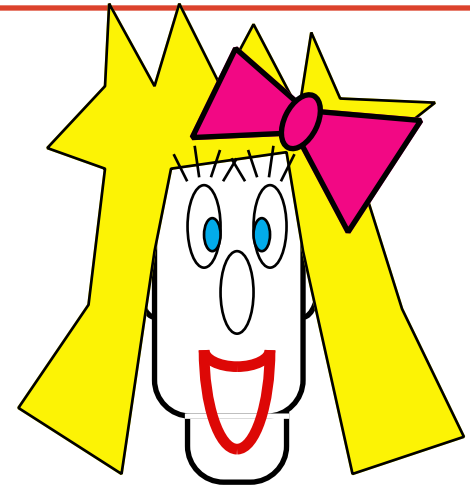


**B:**    × × + + × + + + × + + × × × + × × × + + × + × +  
         0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0

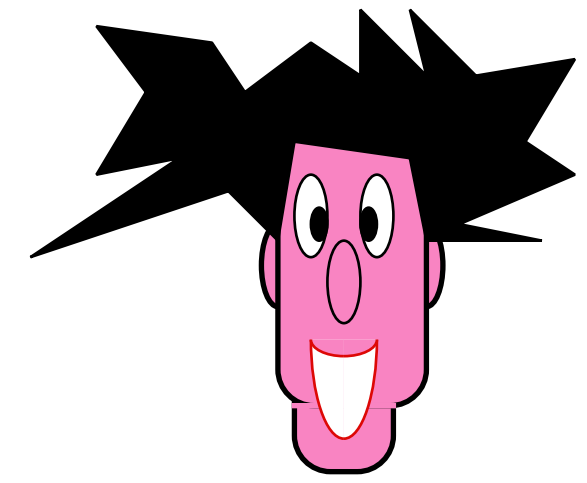
**A:**    × + × + + + × × × × + + + + × × × + × + + + × +

**B:**    0 0 1 1 0 1 0 1 0 0 0

# Q-OT



$b_0$   $b_1$



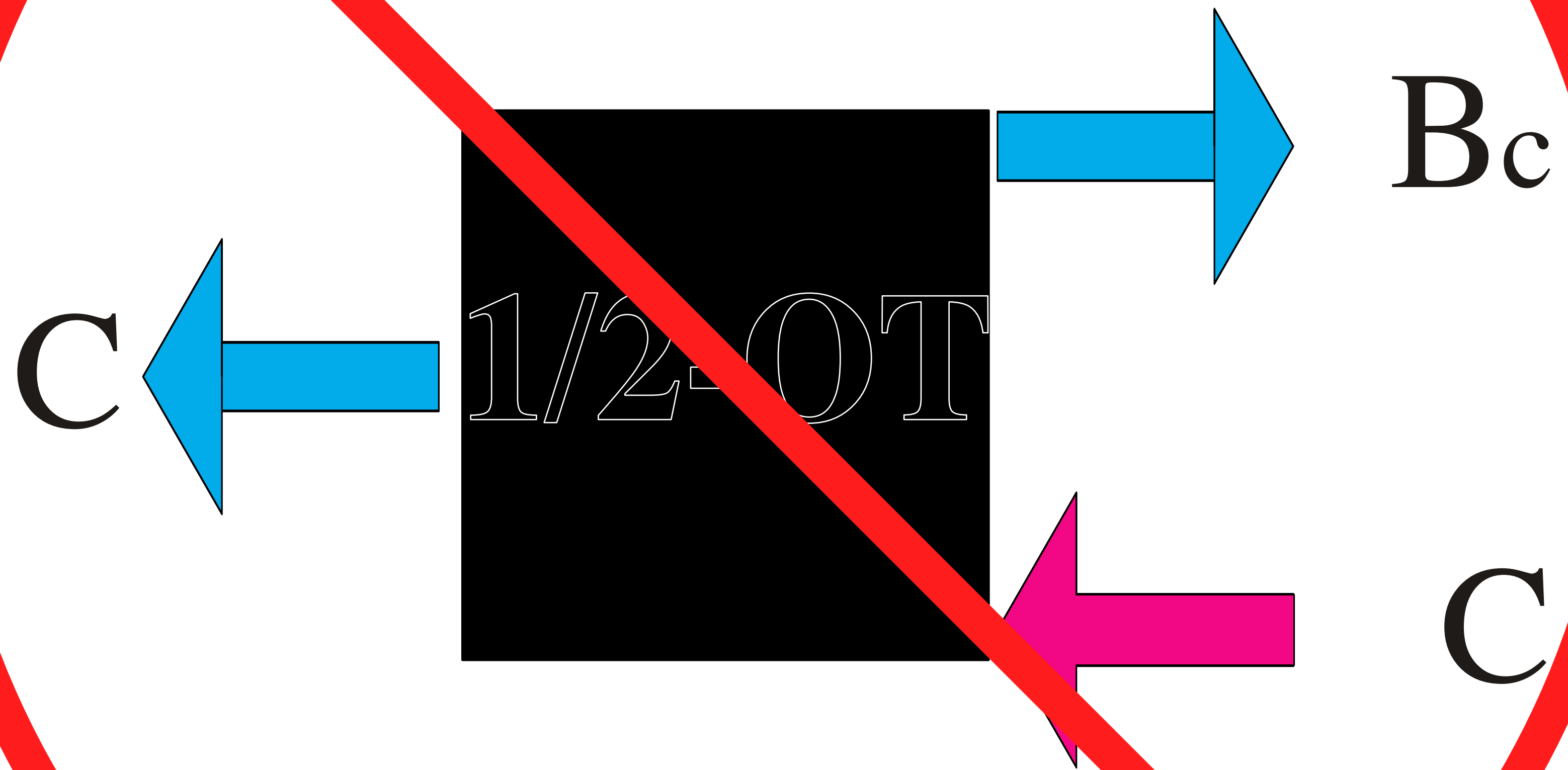
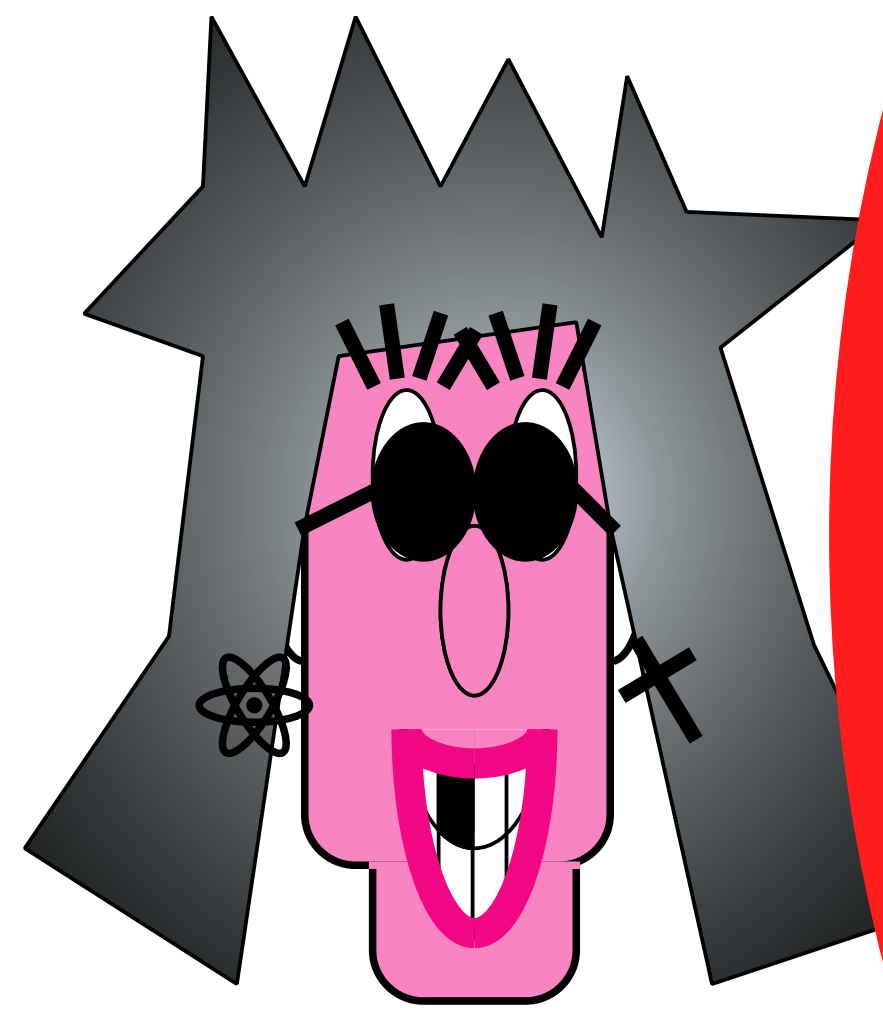
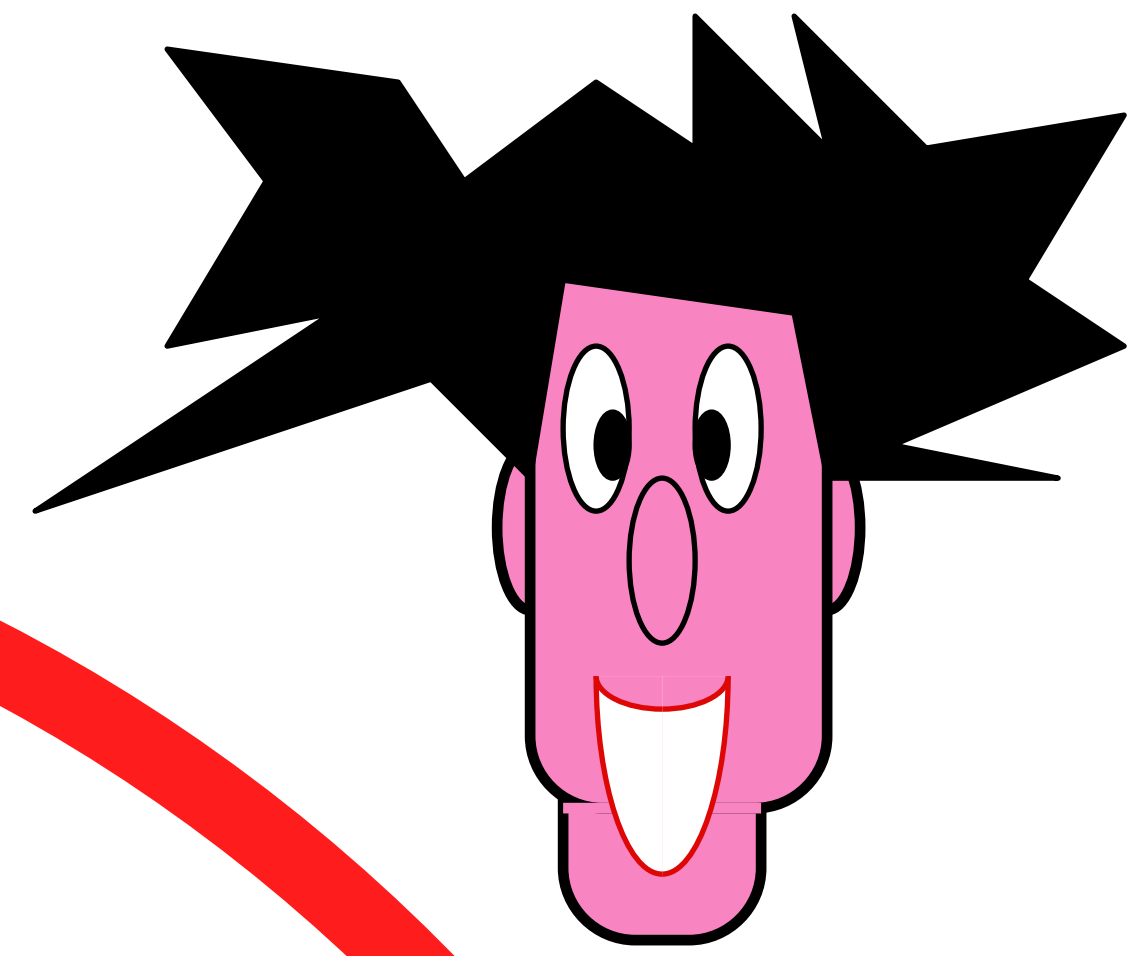
**A:** 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0

**B:** 0 0 1 1 0 1 0 1 0 0 0

**B:** 0 0 1 1 0 1 0 1

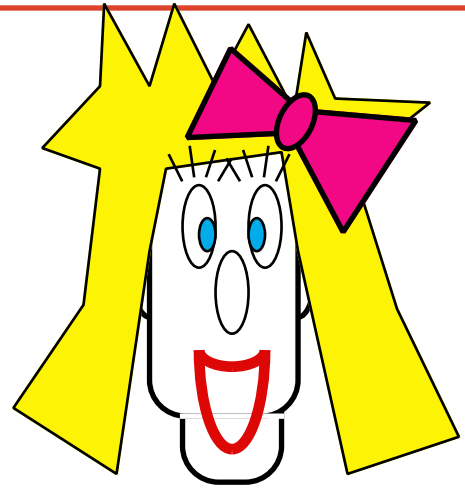
**A:** 0 0 1 1 0 1 0 1 0 0 0 1 1 0 0 0 1 1 0 0 0 1 0 1

# Oblivious Transfer

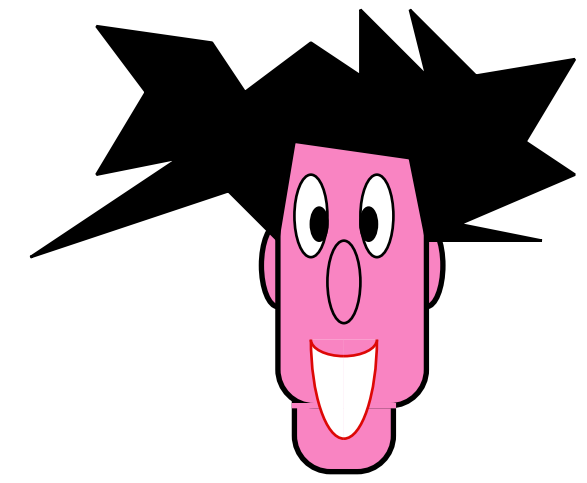




# Q-OT

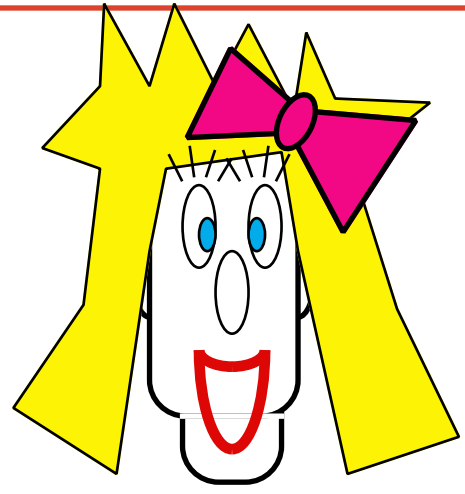


$b_0$   $b_1$

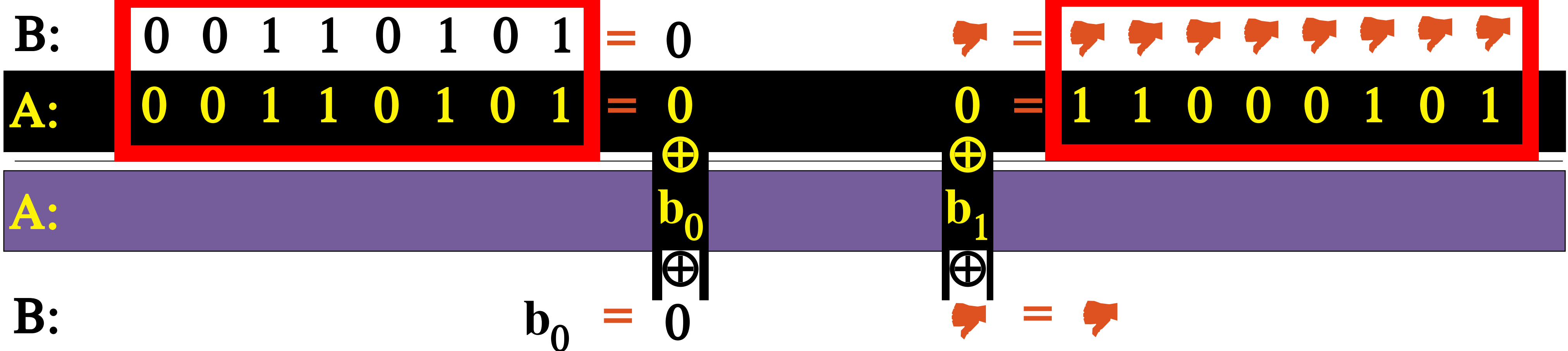
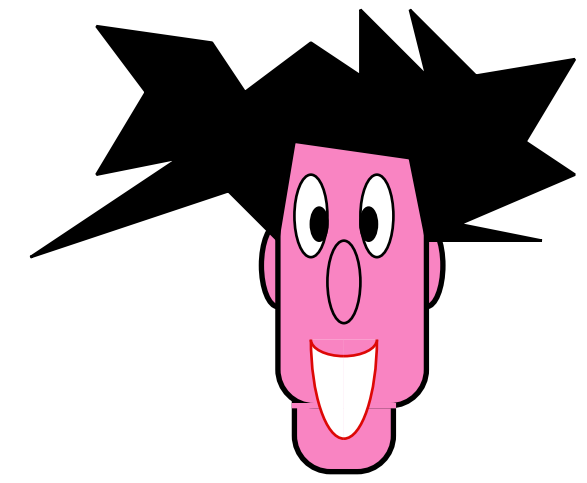


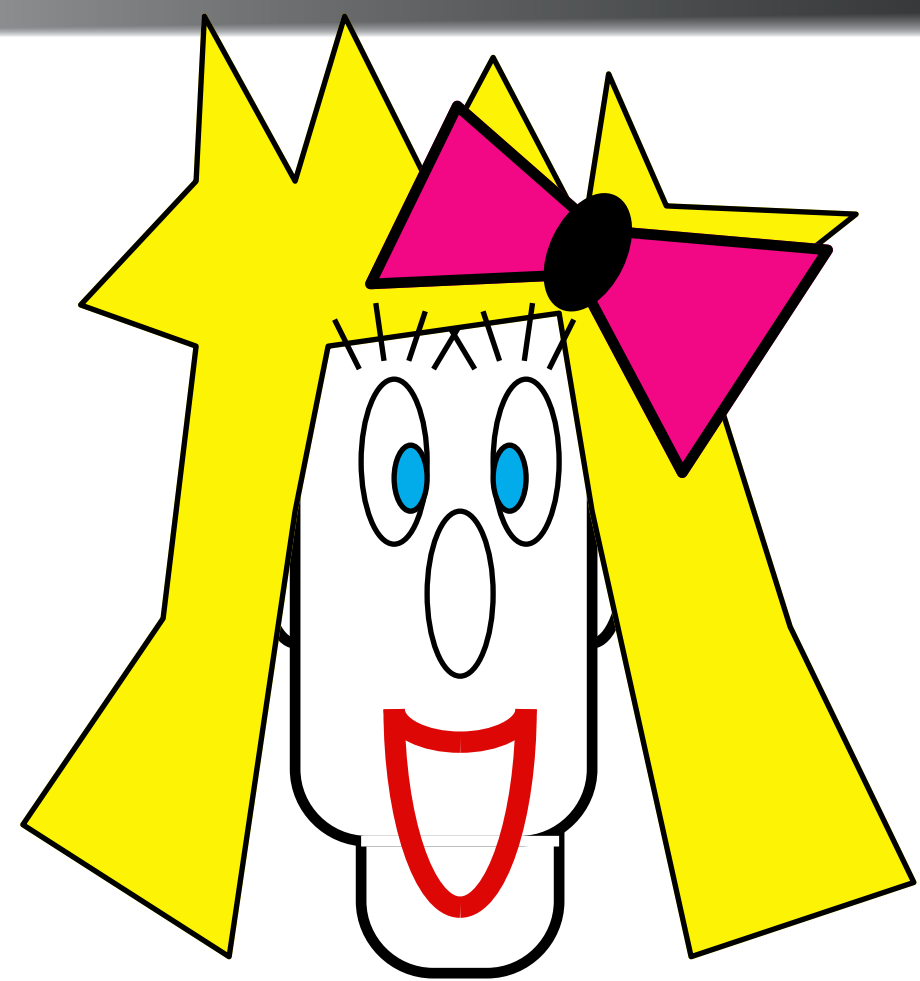
B:	0 0 1 1 0 1 0 1	0 0 0	☞ ☞ ☞ ☞ ☞	☞ ☞ ☞ ☞ ☞ ☞ ☞ ☞
A:	0 0 1 1 0 1 0 1	0 0 0 1 1 0 0 0		1 1 0 0 0 1 0 1
B:	0 0 1 1 0 1 0 1	= 0	☞ =	☞ ☞ ☞ ☞ ☞ ☞ ☞ ☞
A:	0 0 1 1 0 1 0 1	= 0	0 =	1 1 0 0 0 1 0 1

# Q-OT

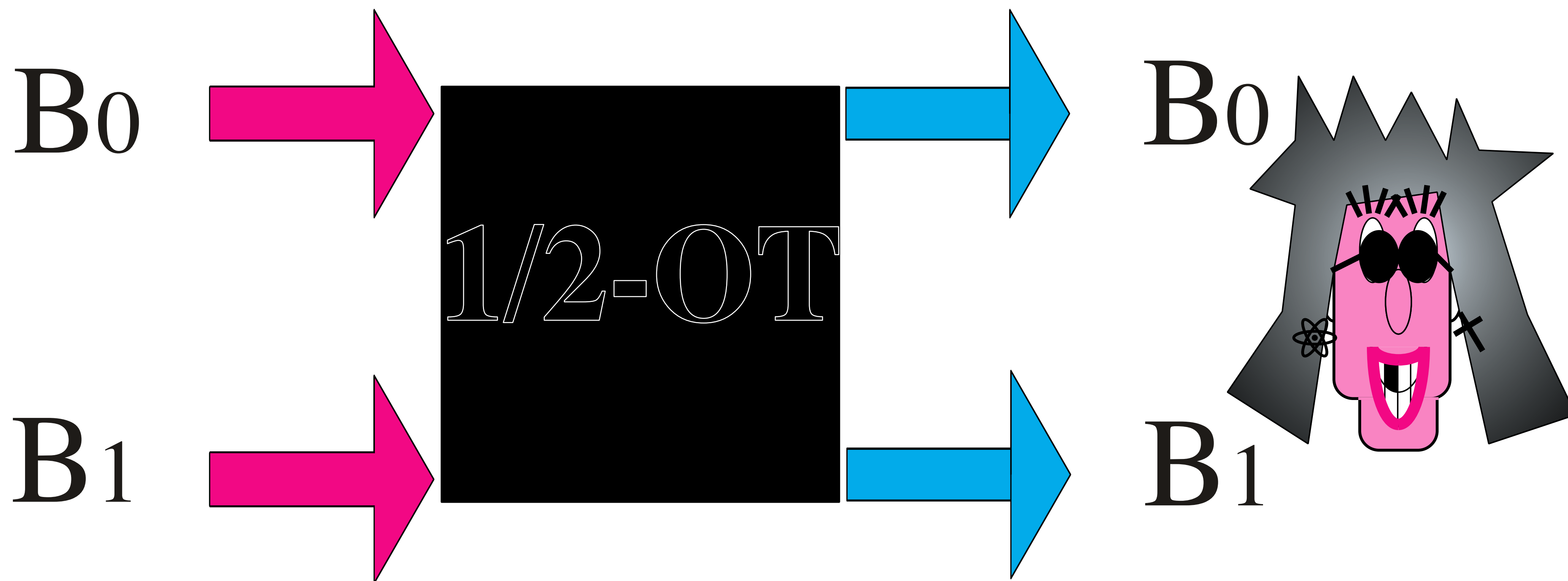


$b_0$   $b_1$

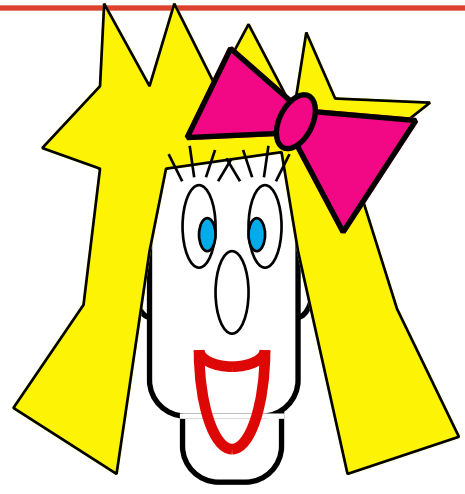




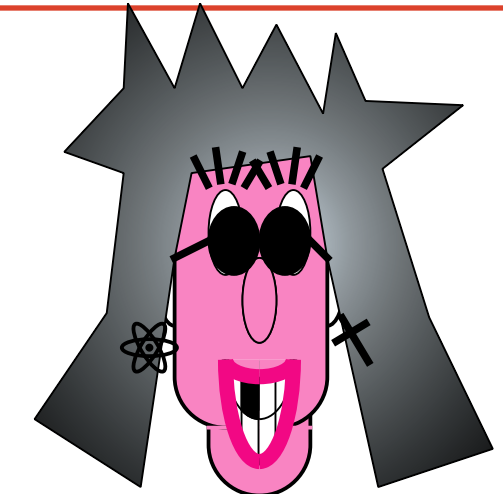
# Oblivious Transfer



# Q-OT



$b_0$   $b_1$



**A:** 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0  
 × + × + + + × × × × + + + + × × × + × + + + × +

**A:** × + × + + + × × × × + + + + × × × + × + + + × +

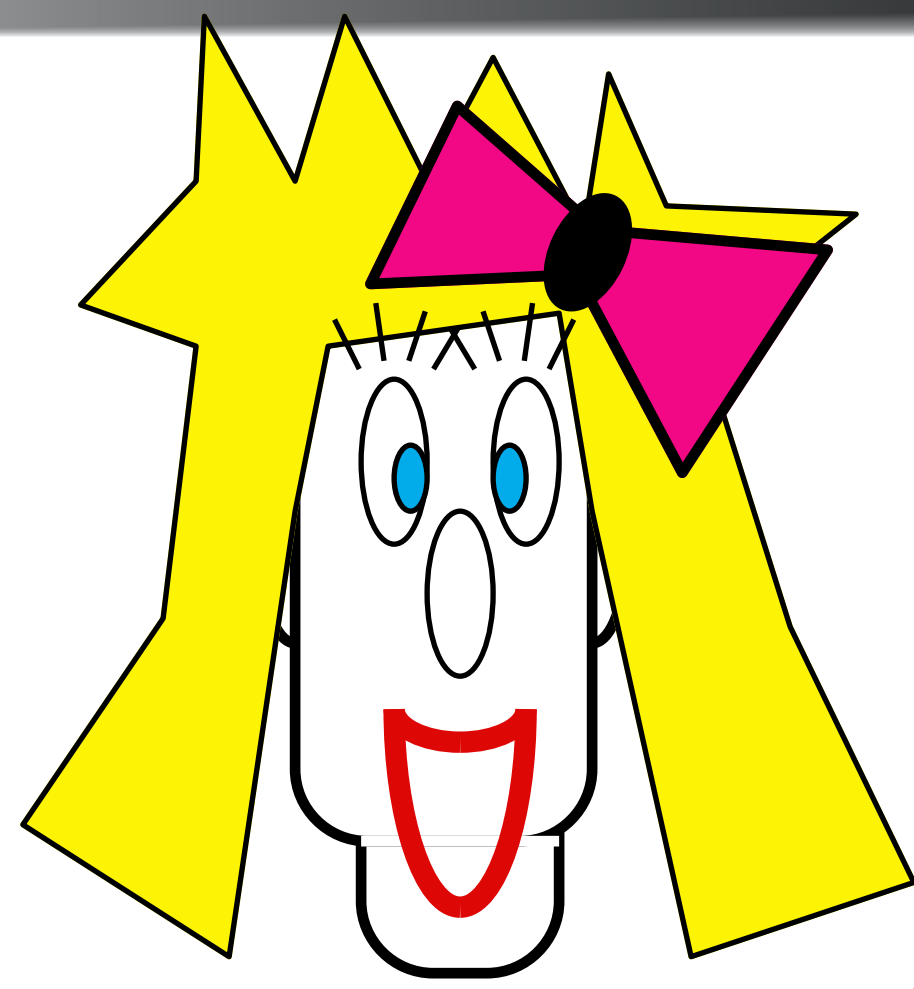
**B:** × + × + + + × × × × + + + + × × × + × + × + × +  
 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0

**B:** 0 0 1 1 0 1 0 1 = 0      0 = 1 1 0 0 0 1 0 1

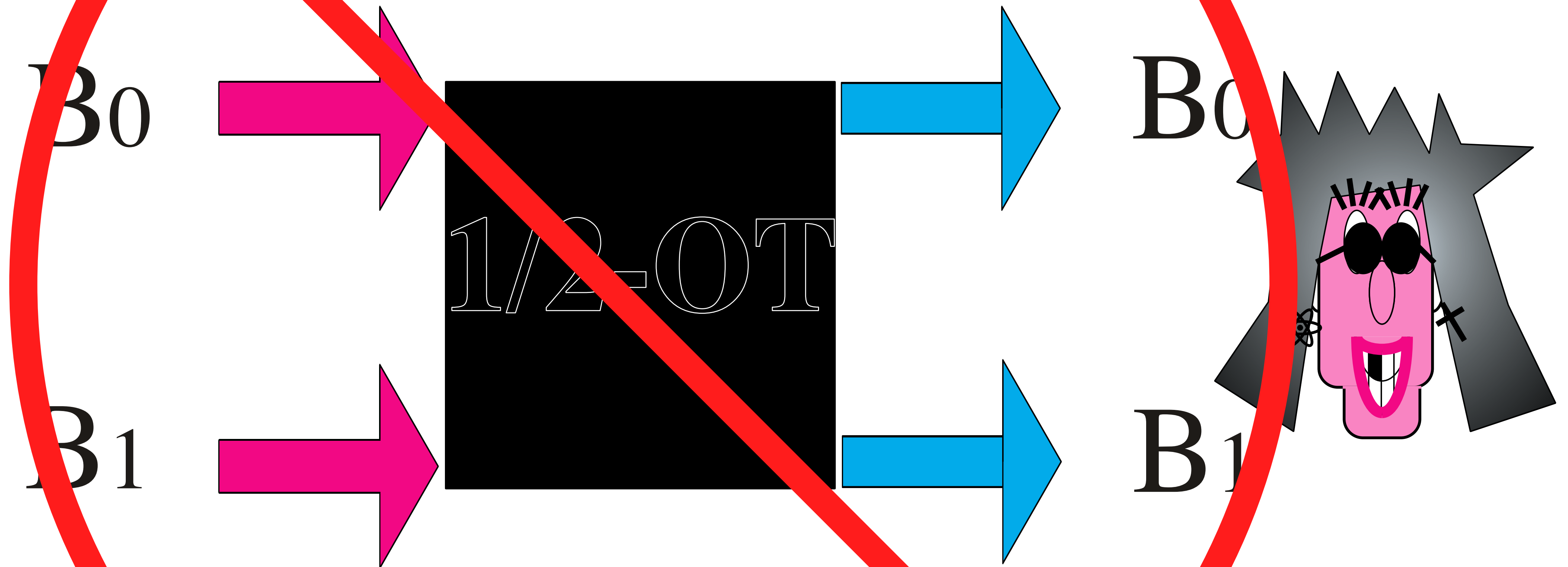
**A:** 0 0 1 1 0 1 0 1 = 0      0 = 1 1 0 0 0 1 0 1

**A:**  $\oplus$   
 $b_0$   $\oplus$   $b_1$

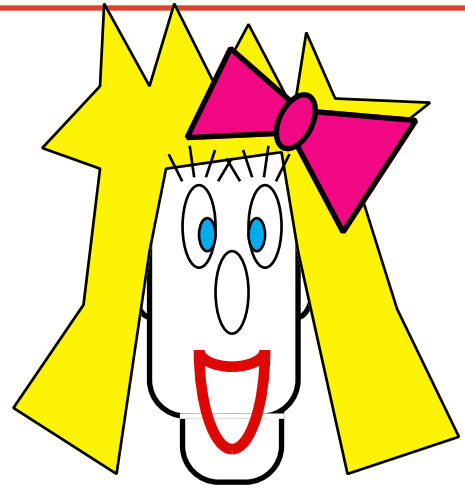
**B:**  $b_0 = 0$        $0 = b_1$



# Oblivious Transfer



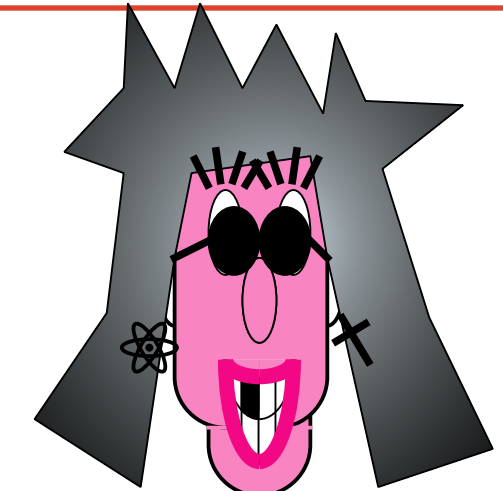
# Q-OT



$b_0$

$b_1$

## from Q-BC

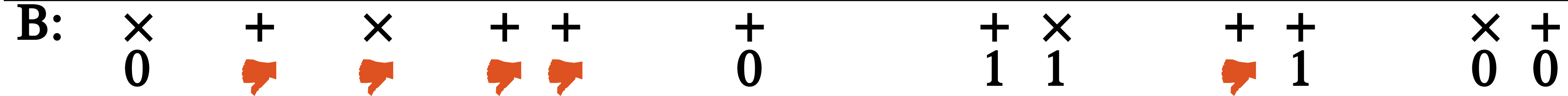
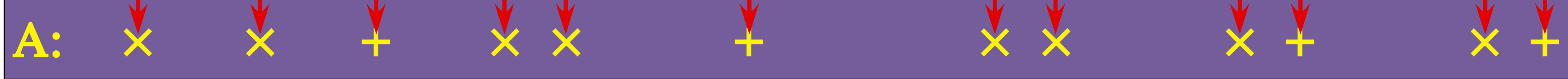
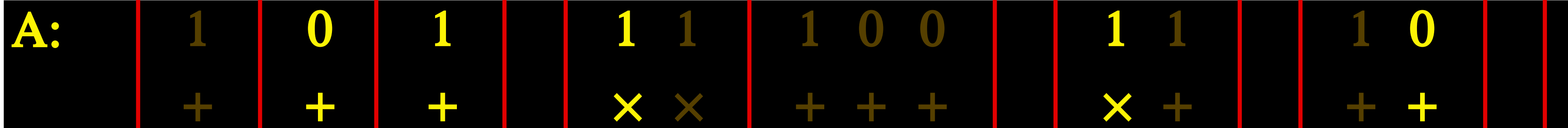
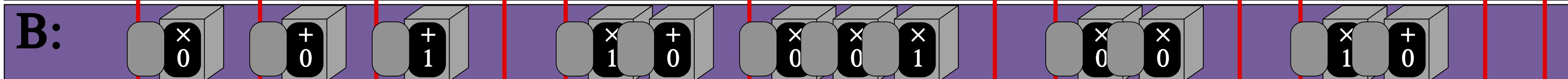
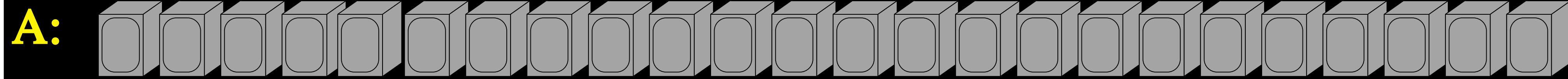
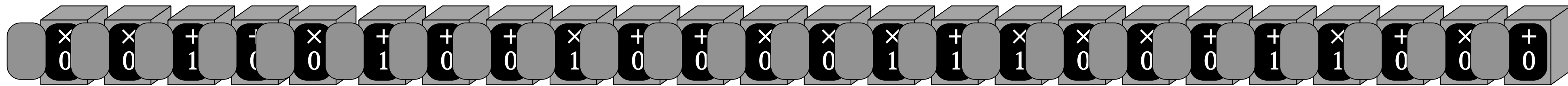


A: 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0

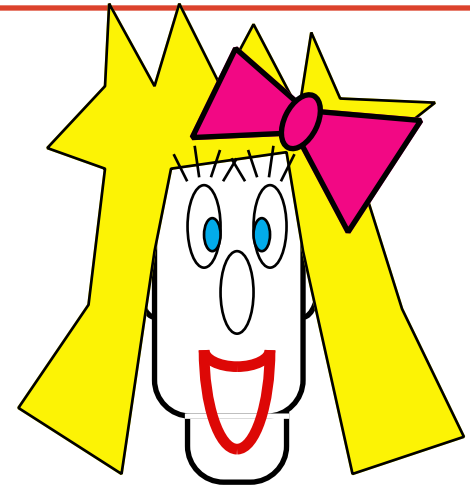
× + × + + + × × × × + + + + × × × + × + + + × +

B: × × + + × + + + × + + × × × + × × × + + × + × +

0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0



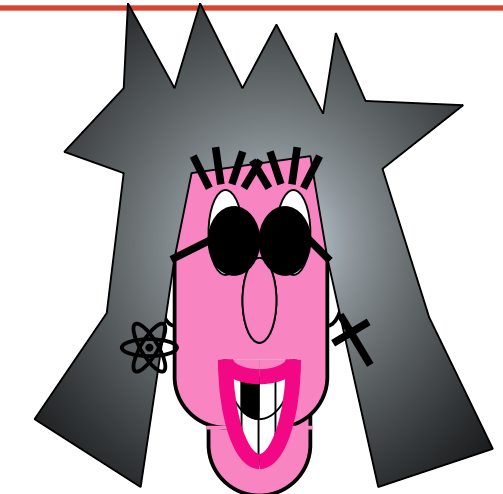
# Q-OT



**b<sub>0</sub>**

**b<sub>1</sub>**

## from Q-BC



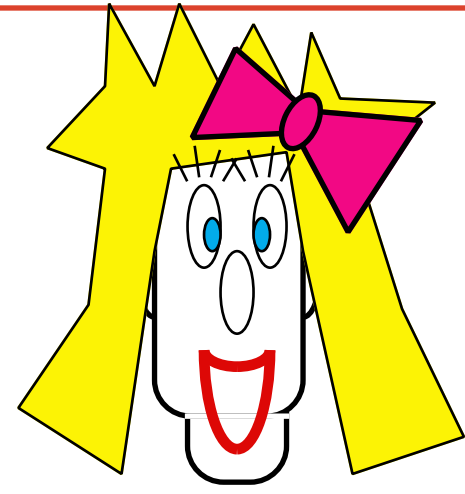
**A:** 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0

× + × + + + × × × × + + + + × × × + × + + + × +

**B:** × × + + × + + + × + + × × × + × × × + + × + × +

0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0

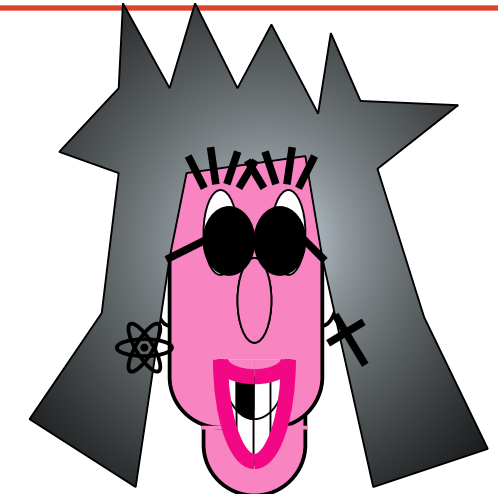
# Q-OT



$b_0$

$b_1$

## from Q-BC



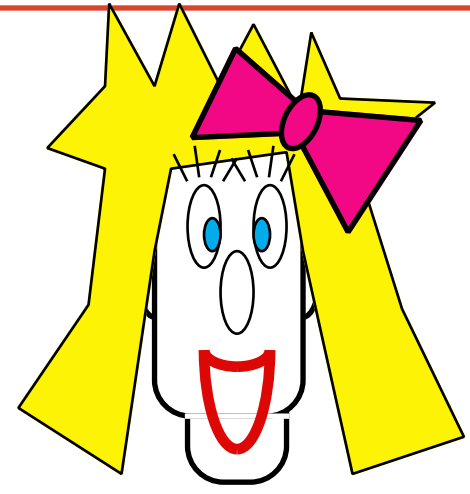
**B:**    × × + + × + + + × + + × × × + × × × + + × + × +  
          0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0

×	×	+	+	×	+	+	+	×	+	+	×	×	×	+	×	×	×	+	+	×	+	×	+
0	0	1	0	0	1	0	0	1	0	0	0	0	1	1	1	0	0	0	1	1	0	0	0
×	×	+	+	×	+	+	+	×	+	+	×	×	×	+	×	×	×	+	+	×	+	×	+
0	0	1	0	0	1	0	0	1	0	0	0	0	1	1	1	0	0	0	1	1	0	0	0

**A:**    [ ]



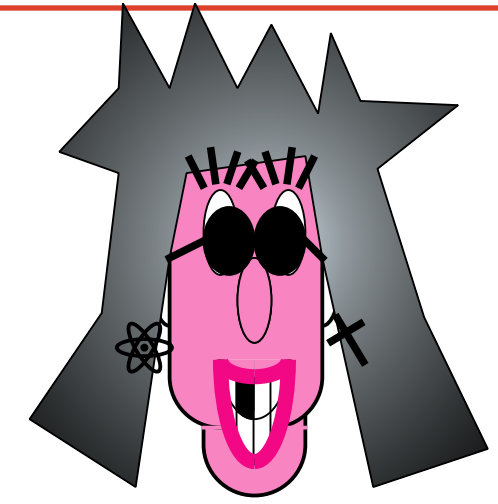
# Q-OT



$b_0$

$b_1$

## from Q-BC



**A:** [20 empty boxes]

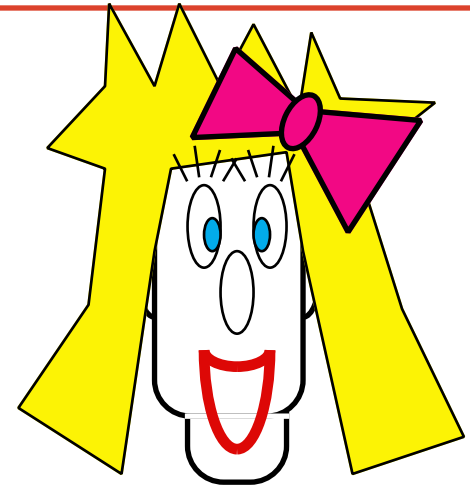
**A:** [20 red arrows pointing right]

**B:** [10 blocks: (x0, +0, +1), (x1, +0), (x0, x0, x1), (x0, x0), (x1, +0)]

**A:** 1 0 1 1 1 1 0 0 1 1 1 0

          +   +   +   × ×   + + +   × +   + +

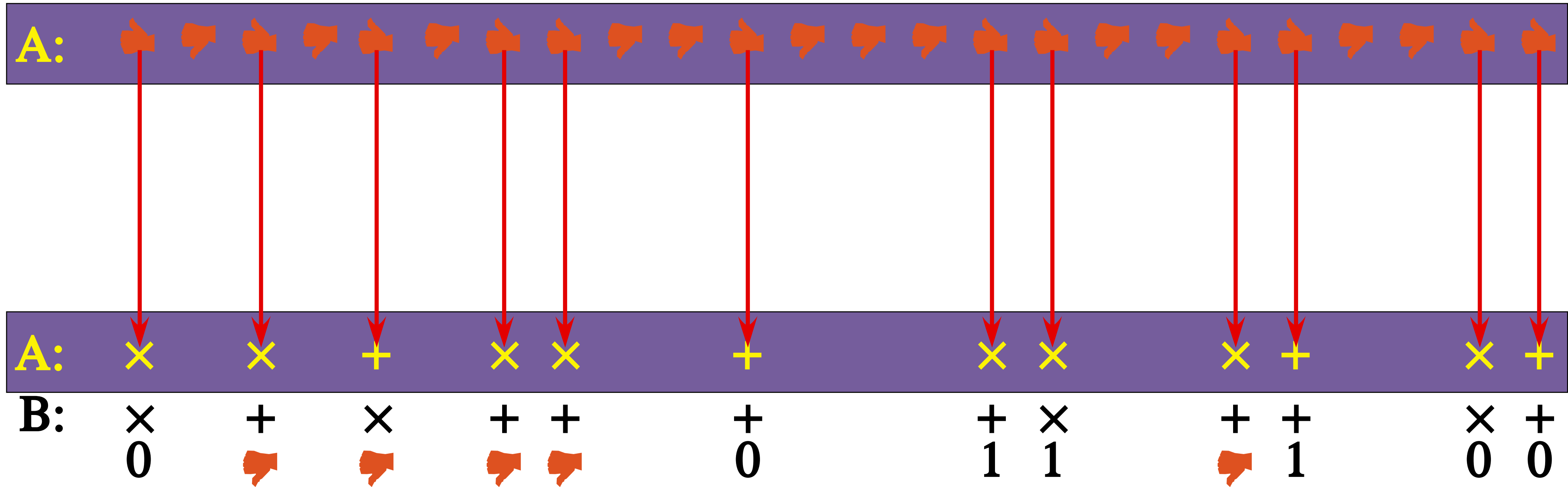
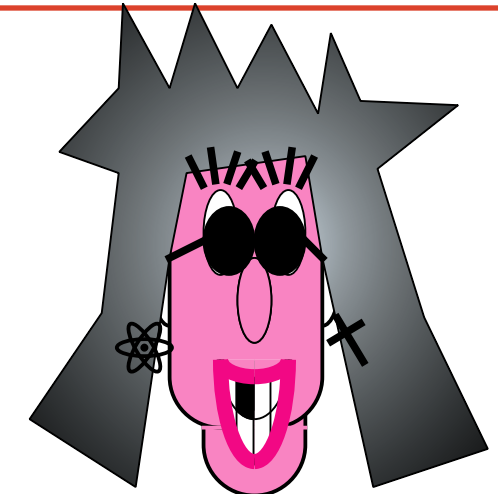
# Q-OT



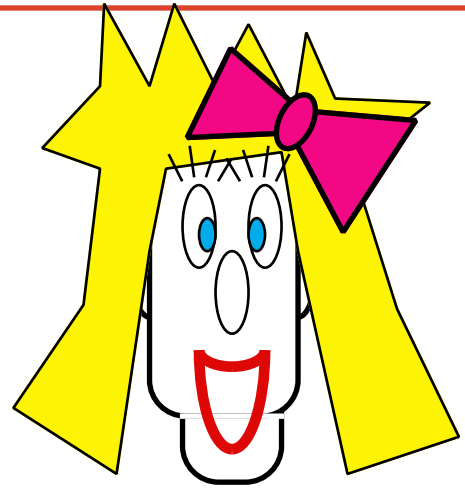
**b<sub>0</sub>**

**b<sub>1</sub>**

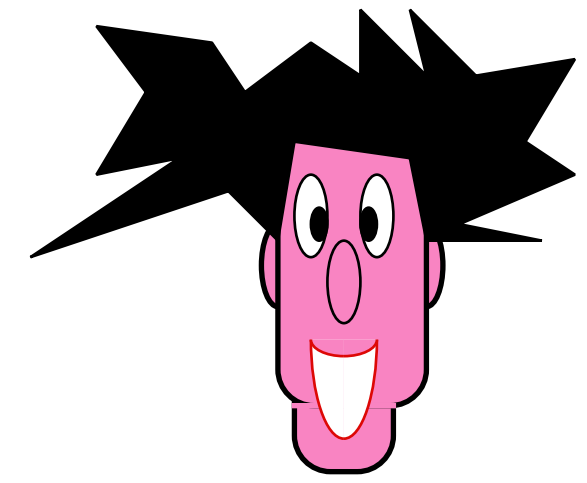
## from Q-BC



# Q-OT



$b_0$   $b_1$



**A:** 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 0 1 1 0 0 0  
 × + × + + + × × × × + + + + × × × + × + + + × +

**B:** × × + + × + + + × + + × × × + × × × + + × + × +  
 0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 0 0 0 1 1 0 0 0

**A:** × + × + + + × × × × + + + + × × × + × + + + × +

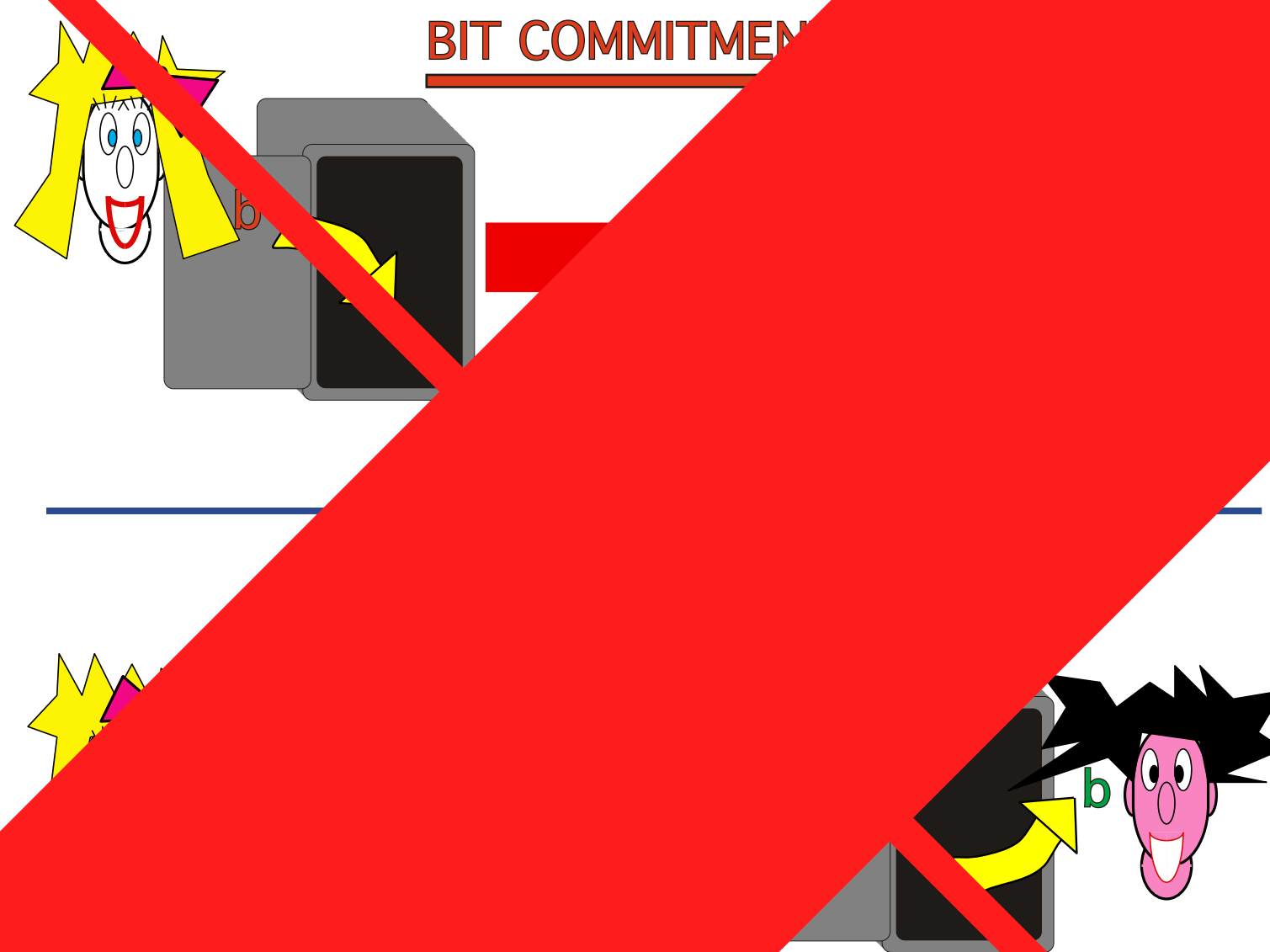
**B:** 0 0 1 1 0 1 0 1 0 0 0

**(6)**

**two provers**

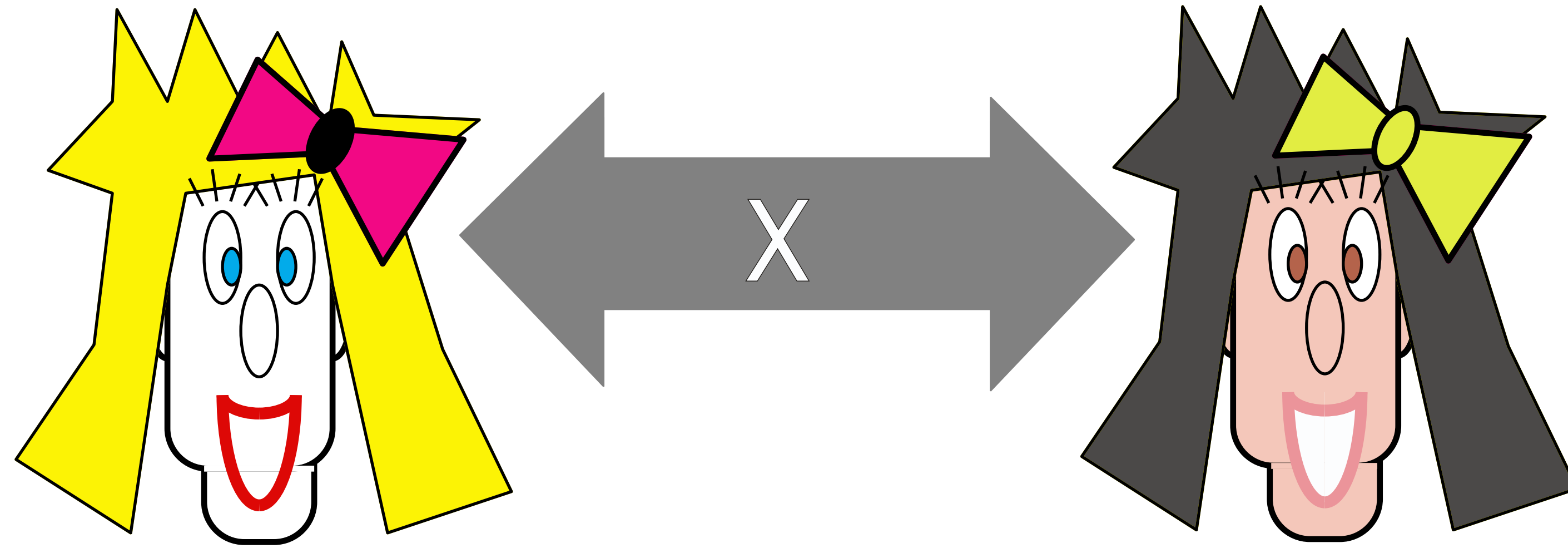
**Cryptographic Protocols**

Classically

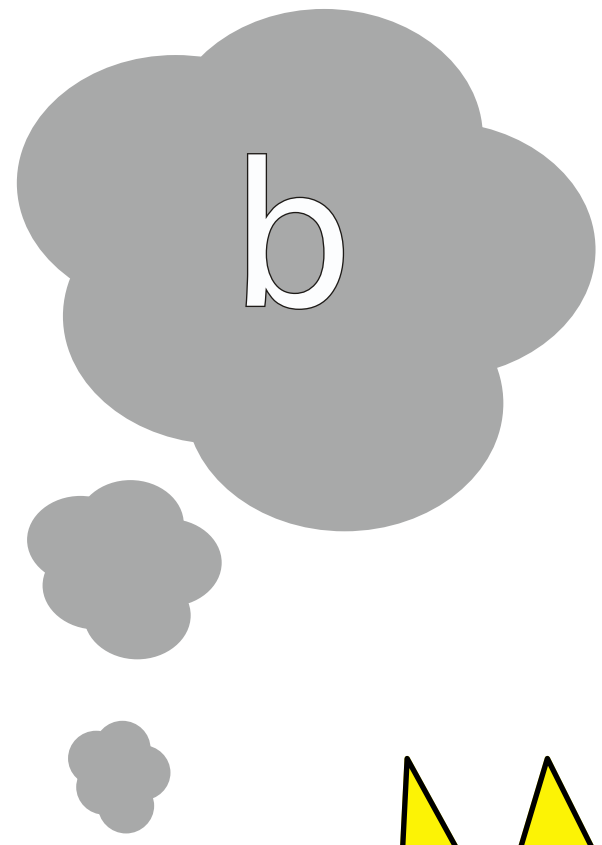


BGKW88

# Classically

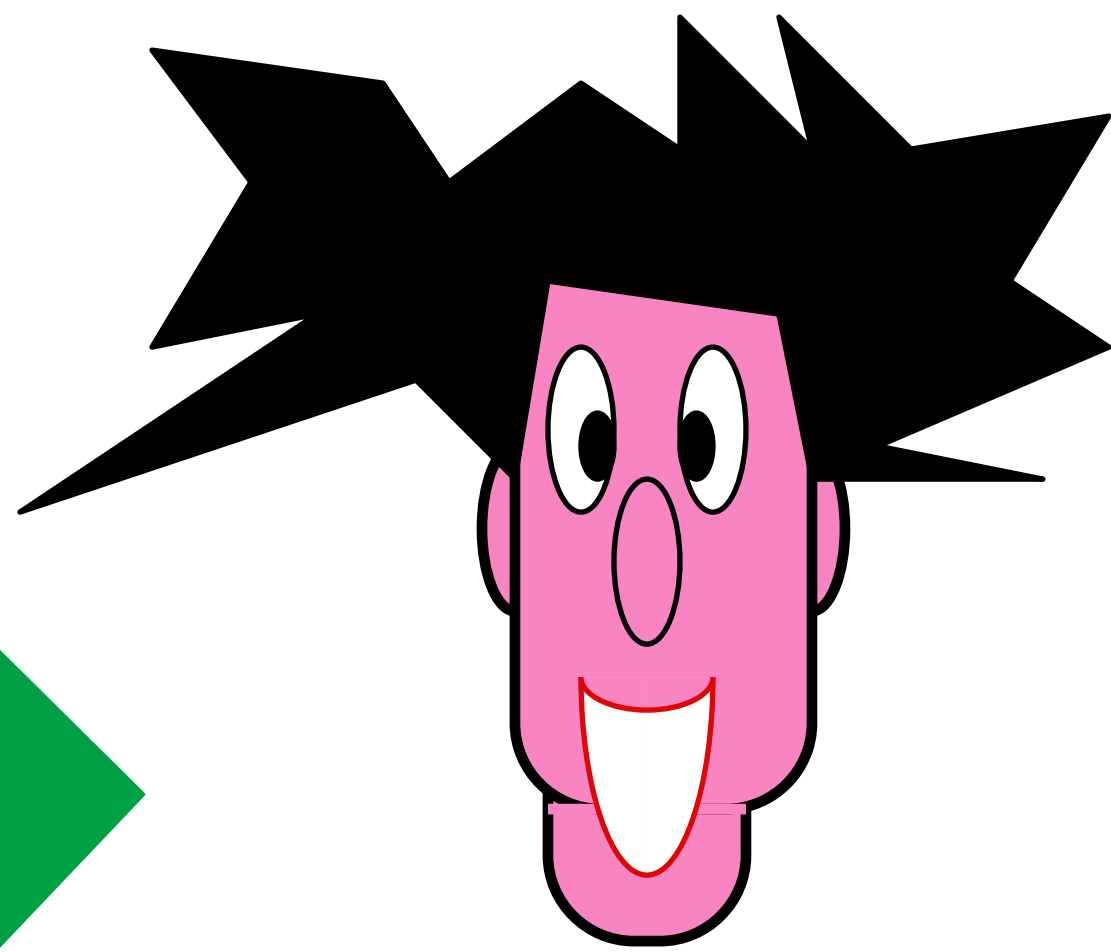
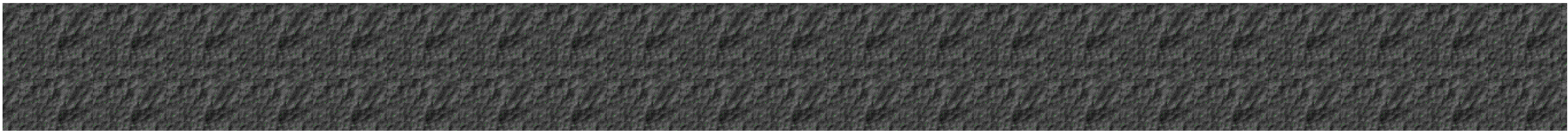
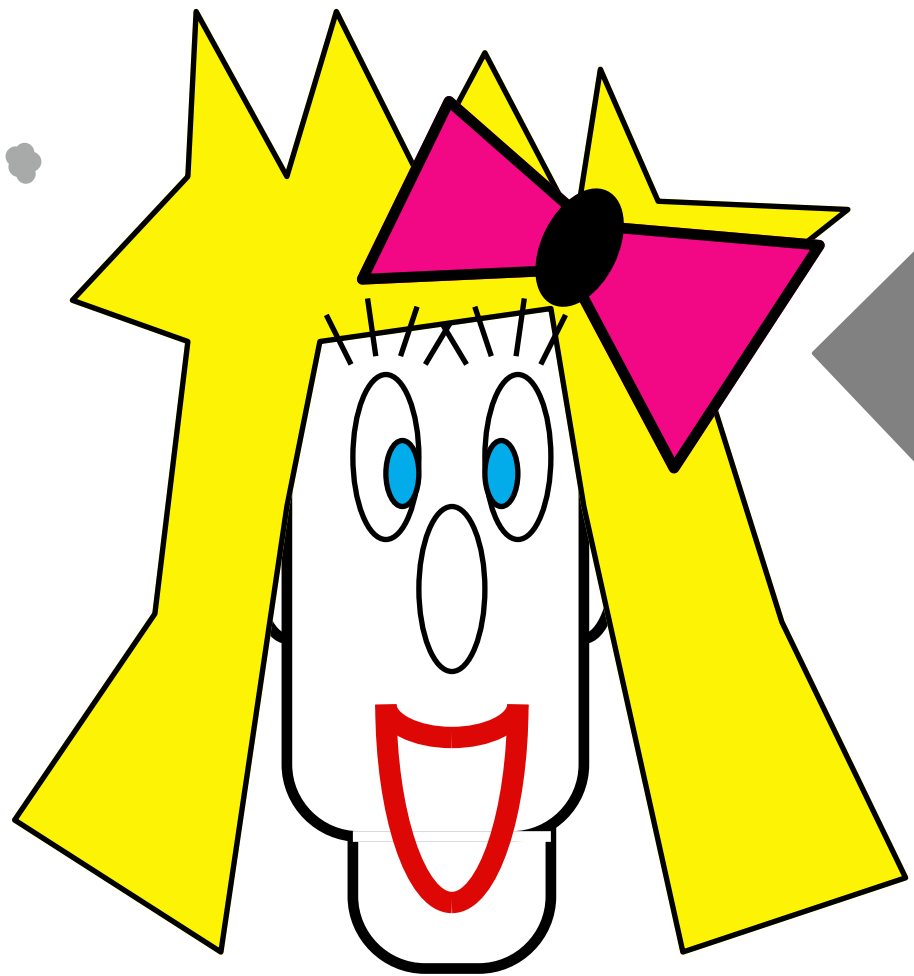


Ben-Or, Goldwasser, Kilian, Wigderson



$$z = x \quad \text{if } b = 0$$

$$z = x \oplus y \quad \text{if } b = 1$$



$$x \oplus z = b \cdot y?$$

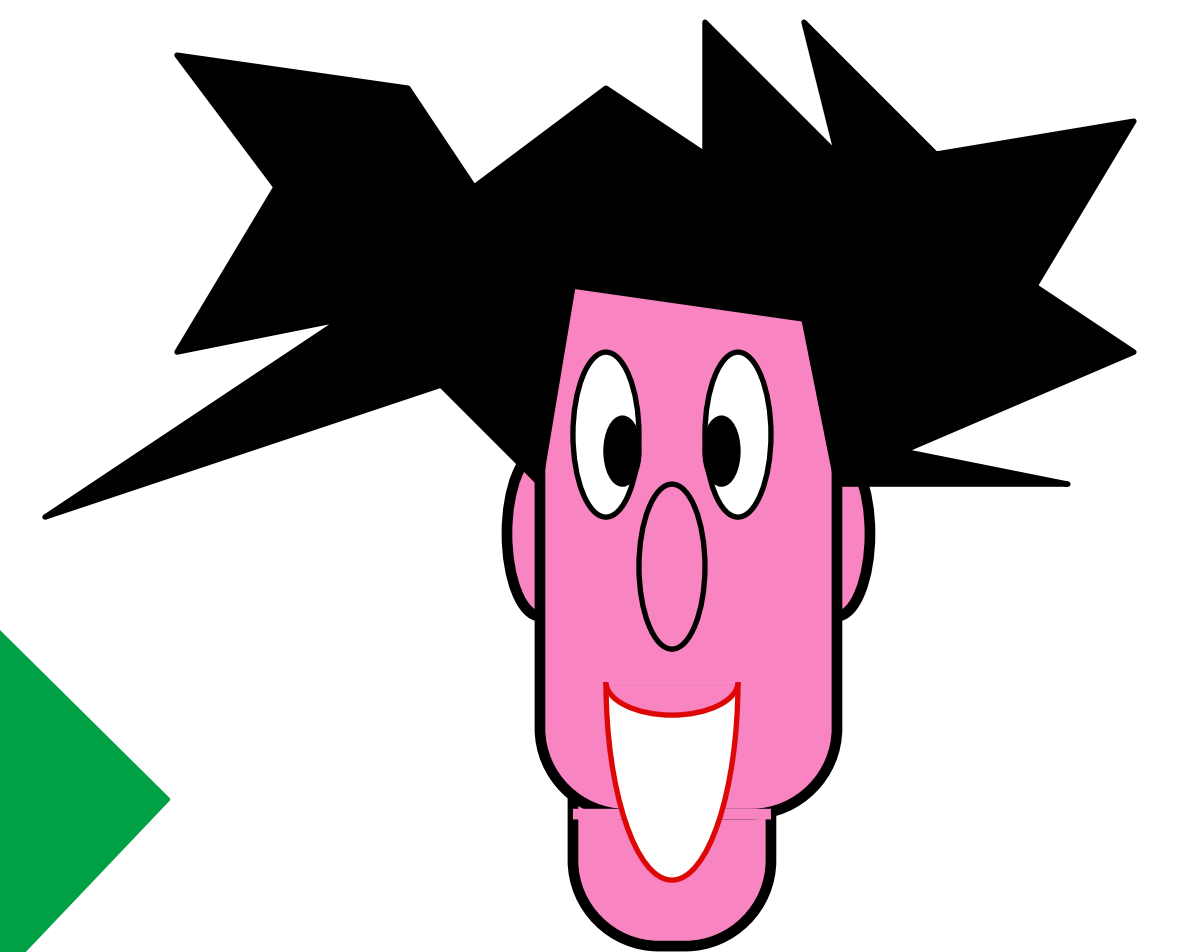
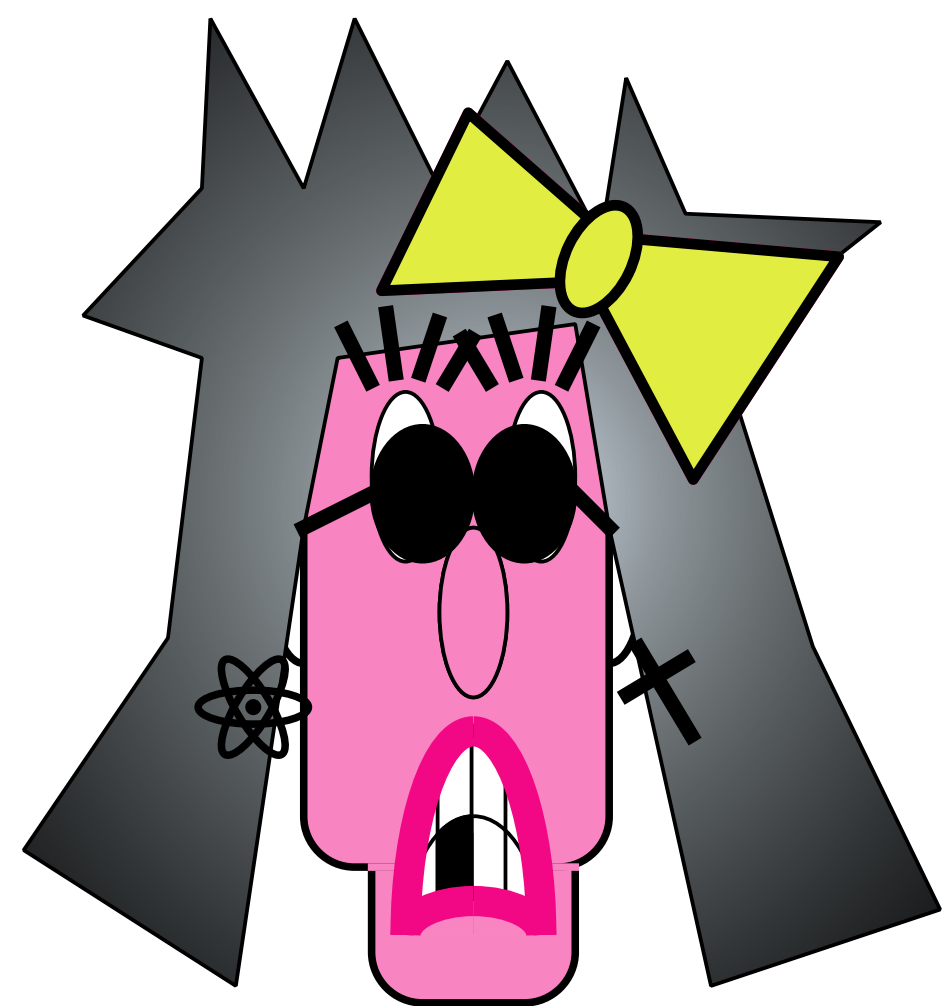
Ben-Or, Goldwasser, Kilian, Wigderson

$$x_0 \oplus z = 0 \cdot y = 0$$

$$x_1 \oplus z = 1 \cdot y = y$$

$$x_0 \oplus x_1 = (x_0 \oplus z) \oplus (x_1 \oplus z) = y$$

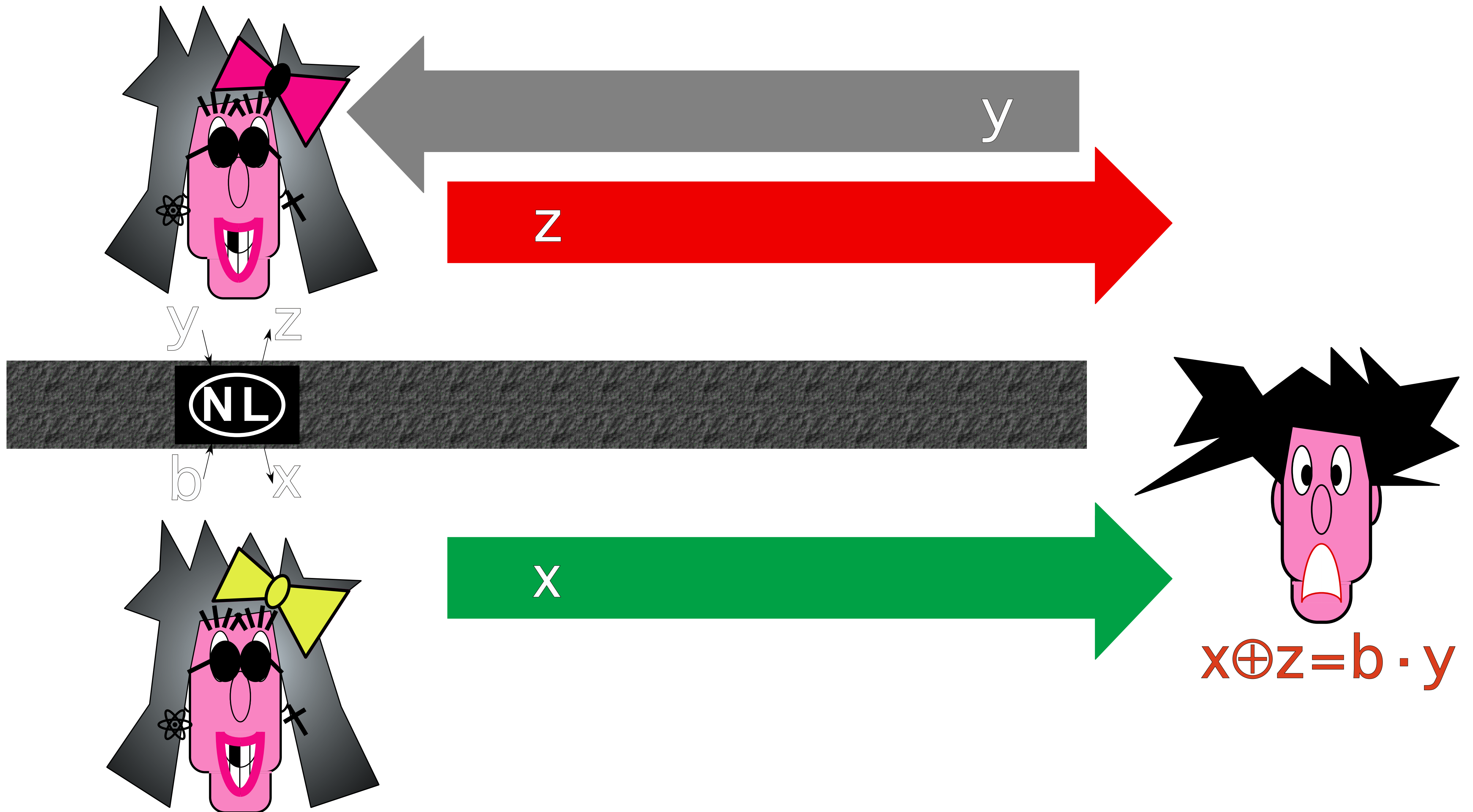
possible with prob. at most  $2^{-n}$



Ben-Or, Goldwasser, Kilian, Wigderson

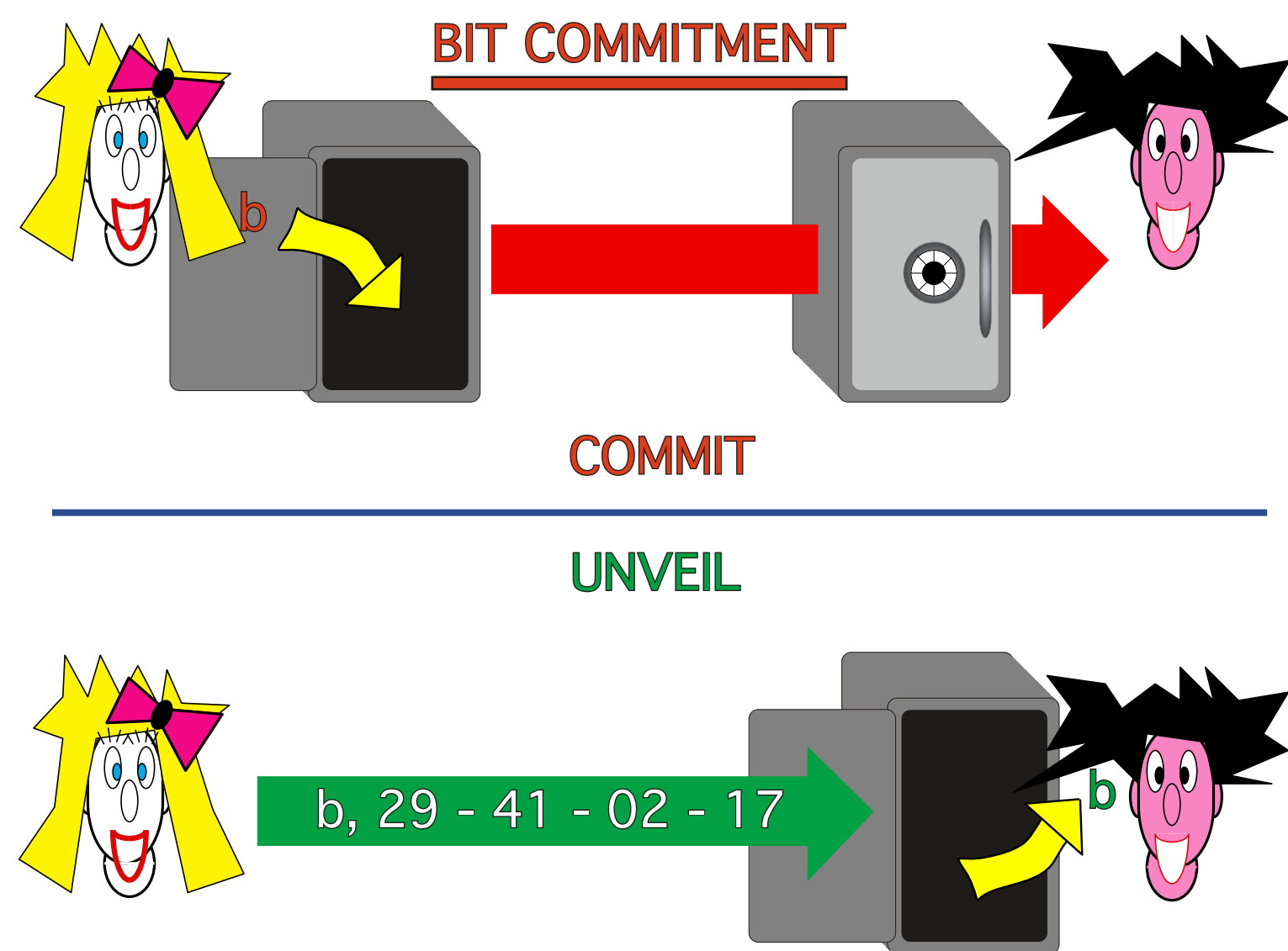


# Classically

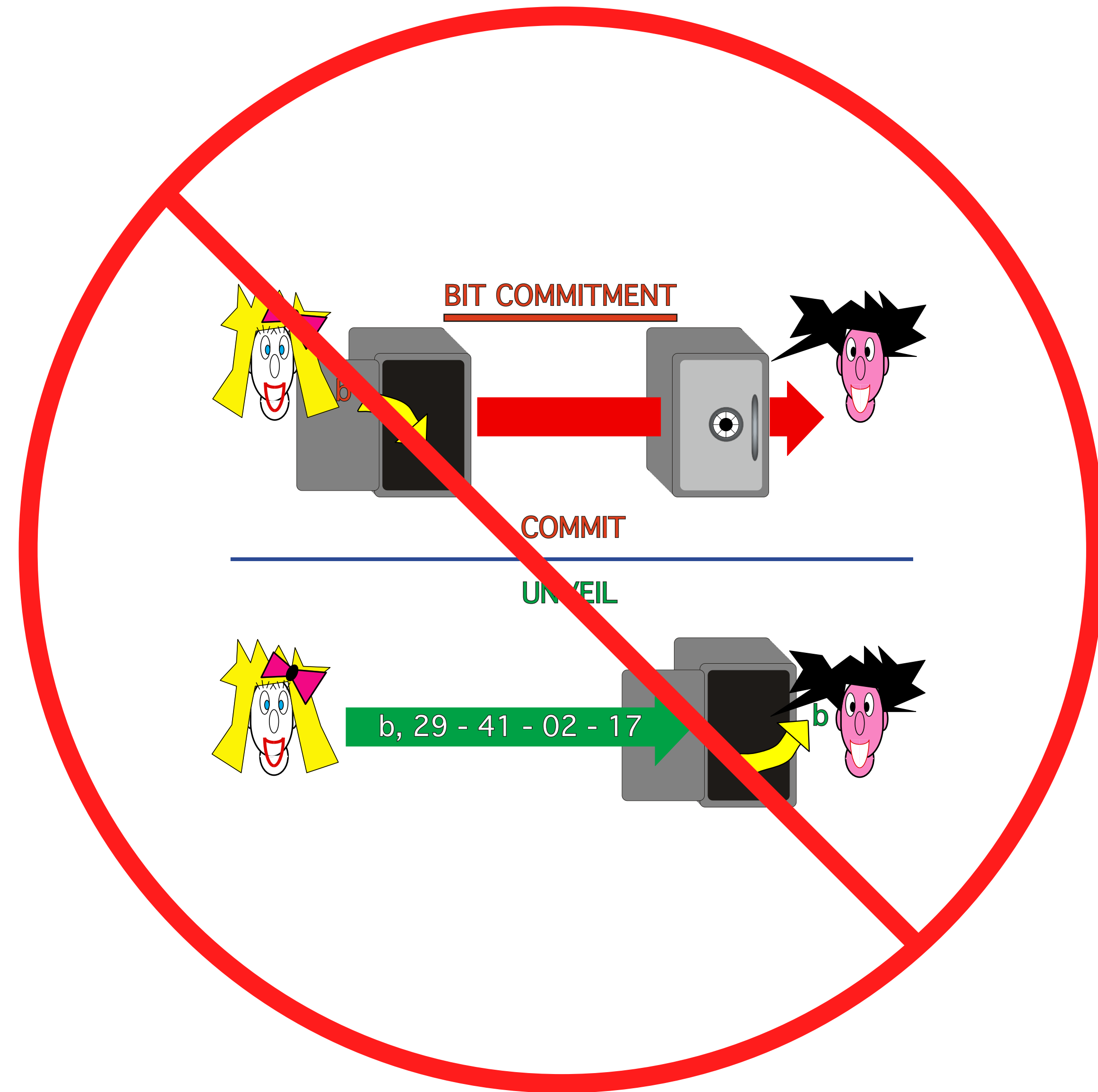


~~Ben-Or, Goldwasser, Kilian, Wigderson~~

# Quantumly



or



???

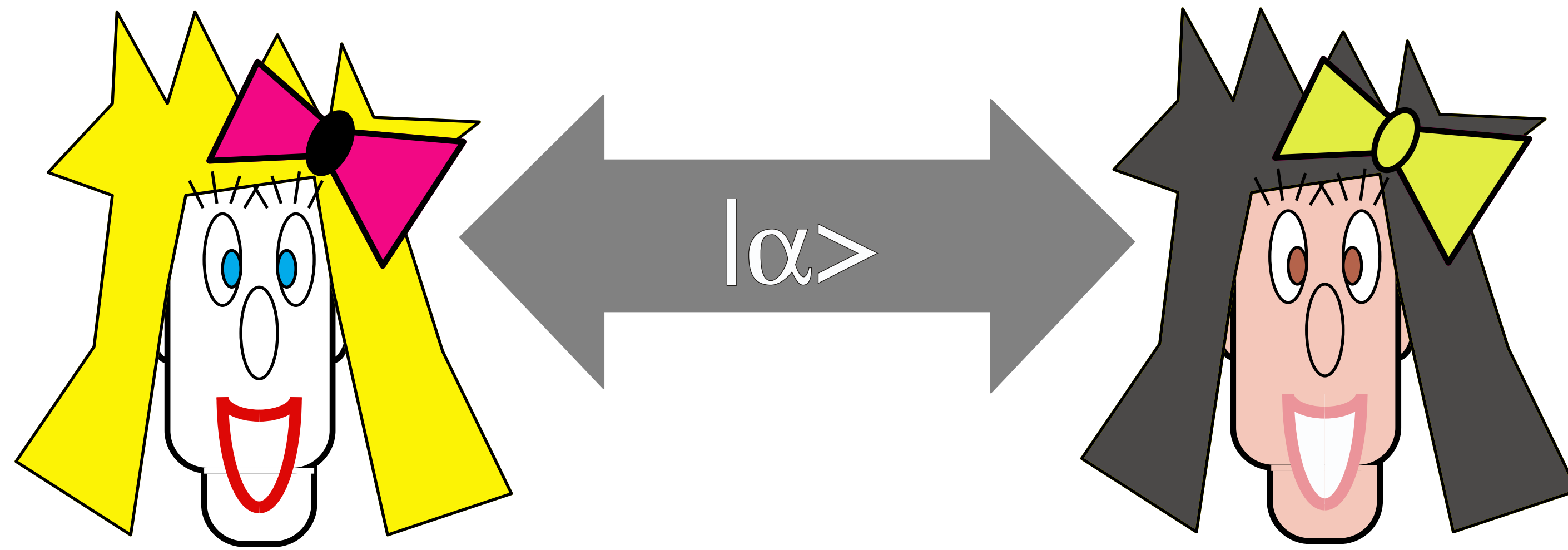
**(7)**

**two provers BC**

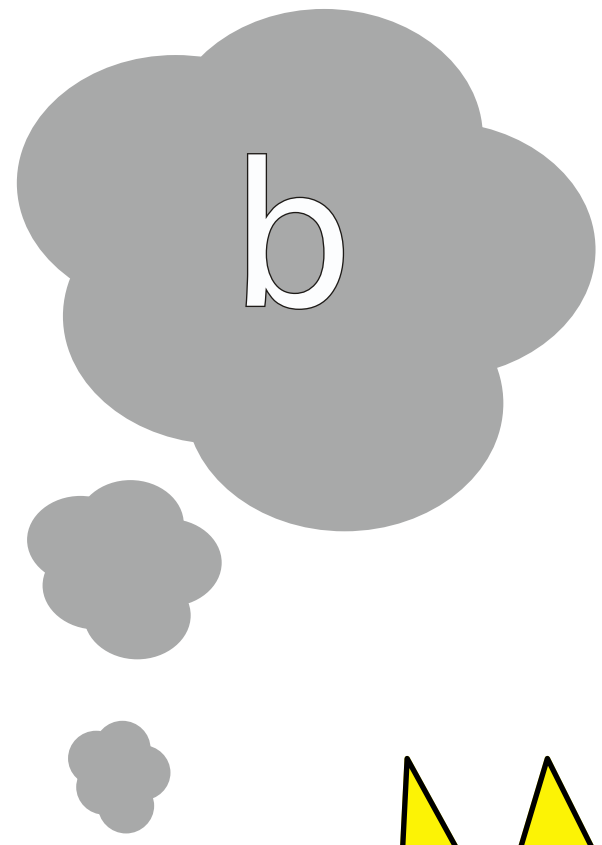
**Classically Secure**

**Quantumly Insecure**

# Quantumly

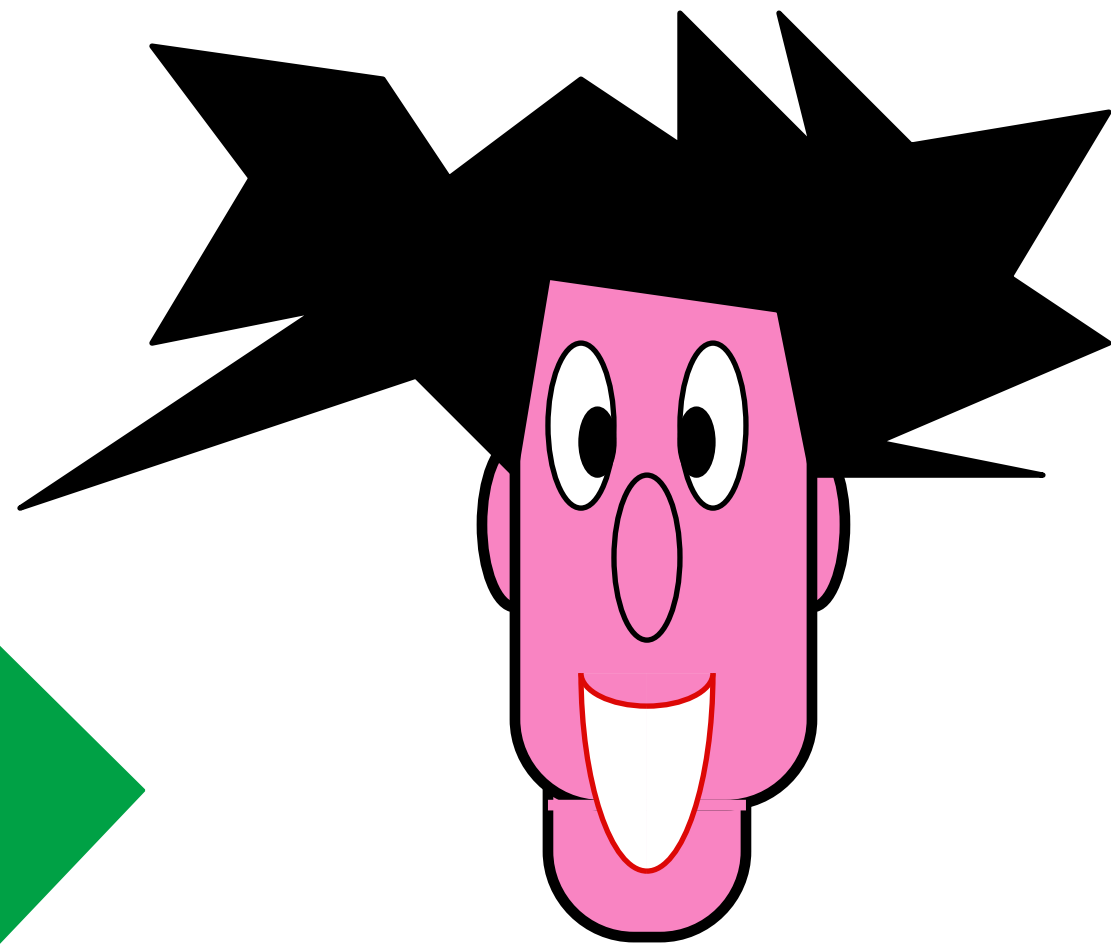
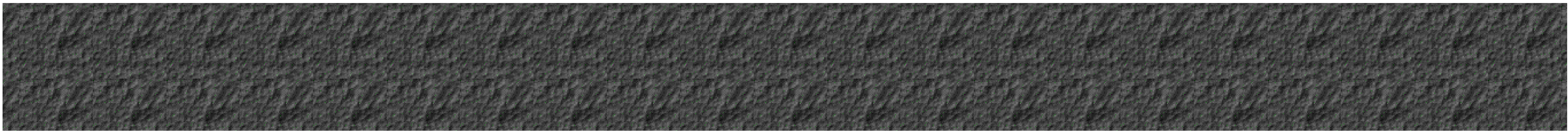
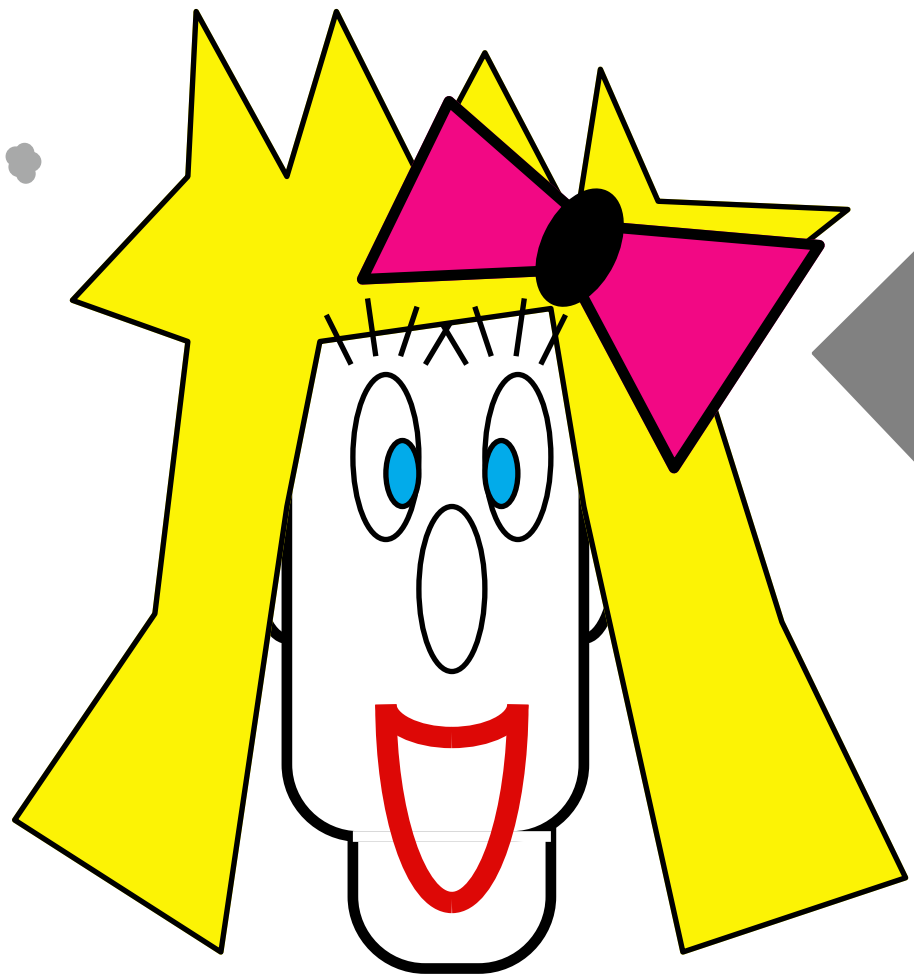


Ben-Or, Goldwasser, Kilian, Wigderson



$$z = x \quad \text{if } b = 0$$

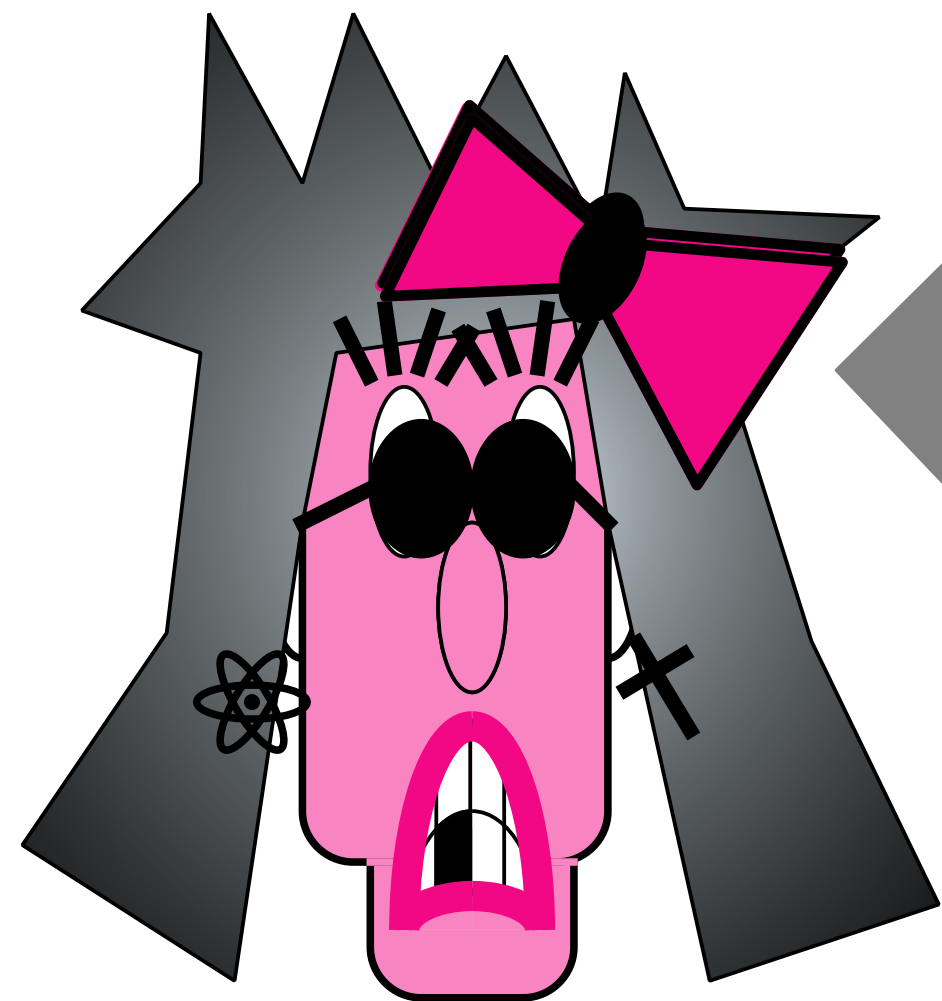
$$z = x \oplus y \quad \text{if } b = 1$$



$$D_H(x \oplus z, b \cdot y) < n/5?$$

Ben-Or, Goldwasser, Kilian, Wigderson

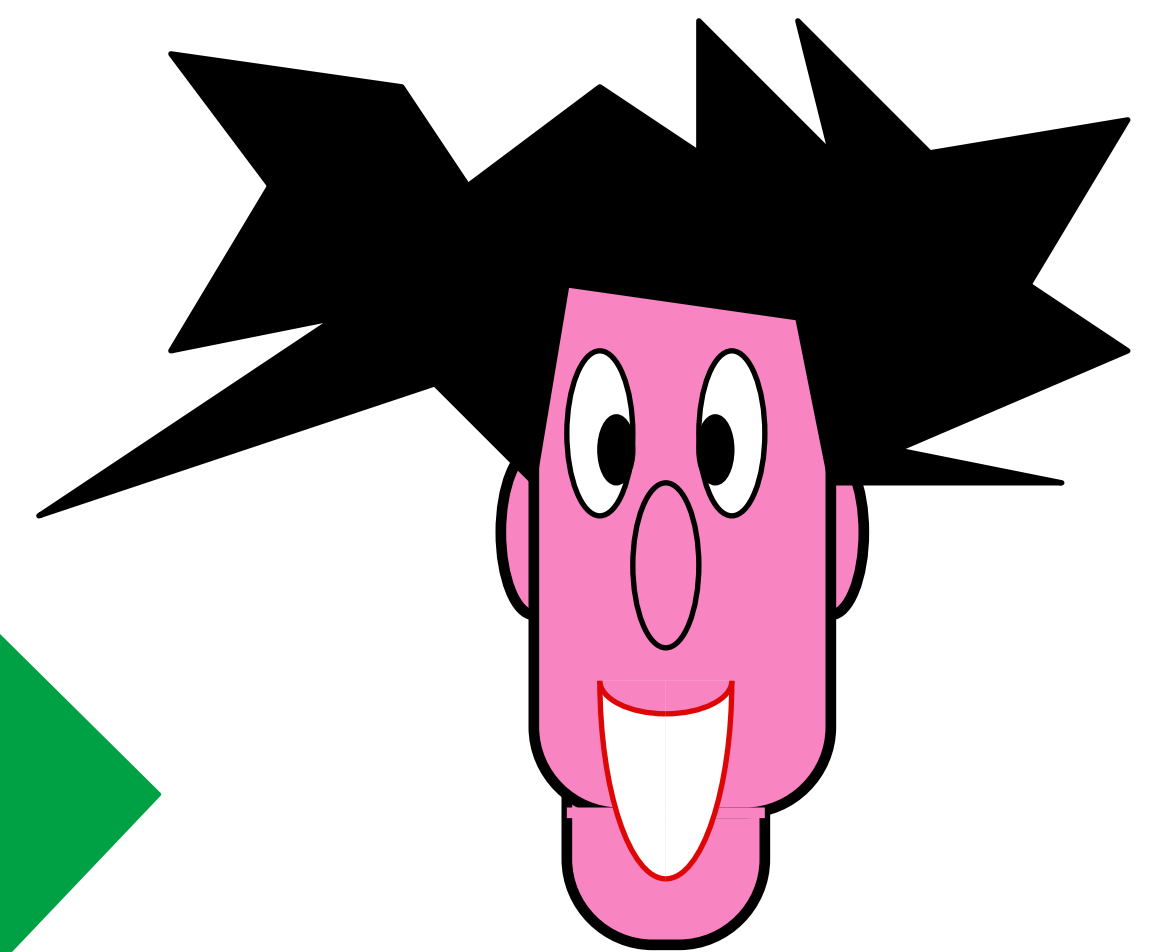
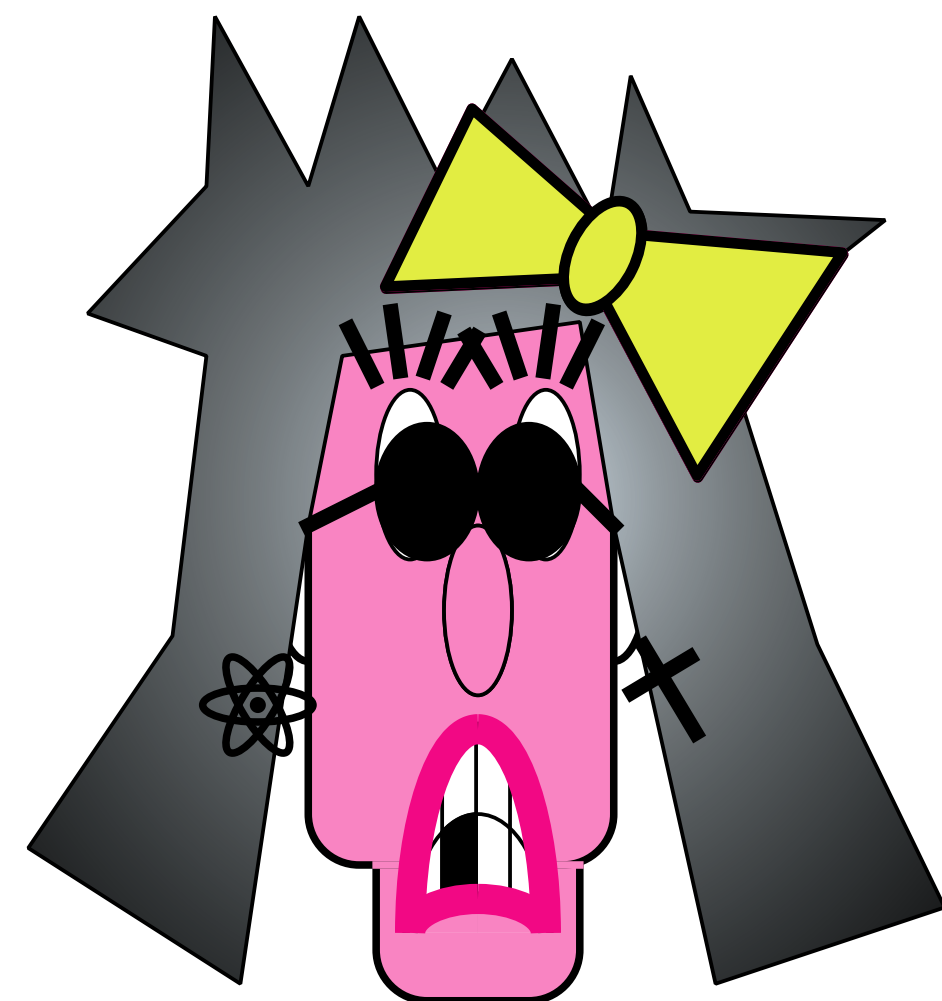
# Classically



75% **NL**  $\rightarrow D_H(x \oplus z, b \cdot y) \approx 25\%n > n/5$

y z

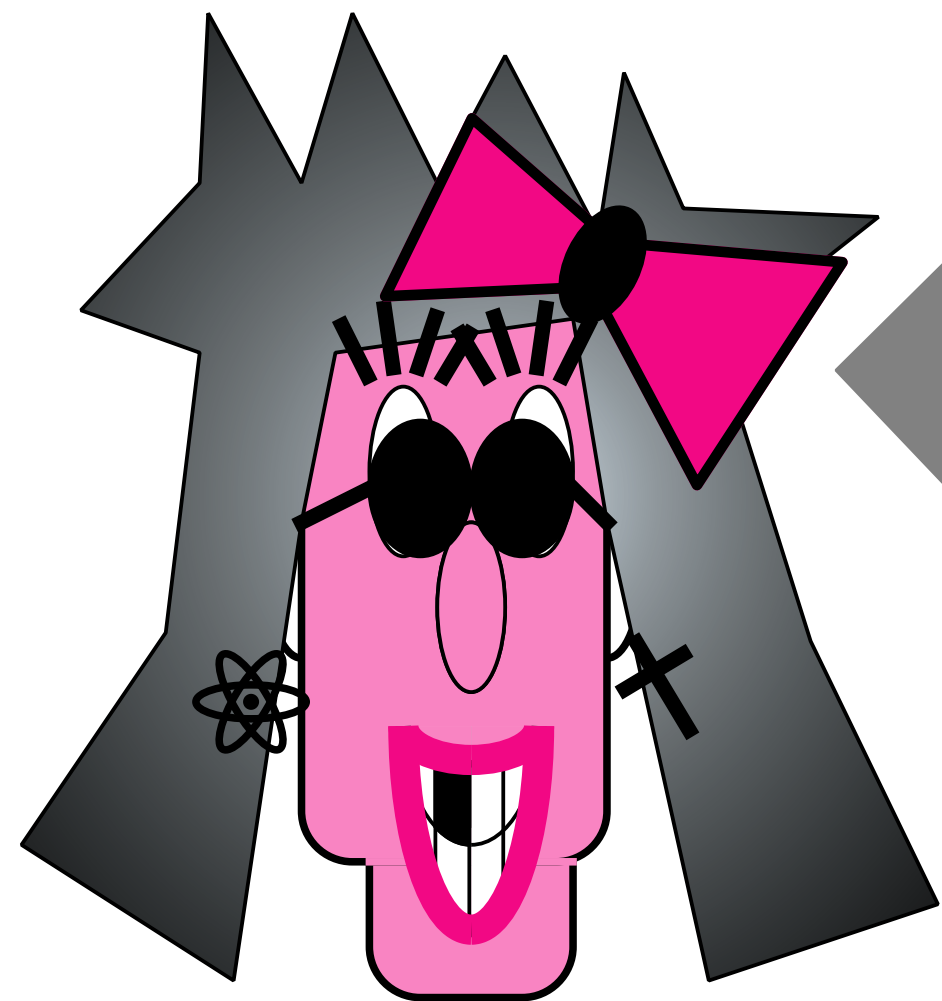
b x



$D_H(x \oplus z, b \cdot y) < n/5?$

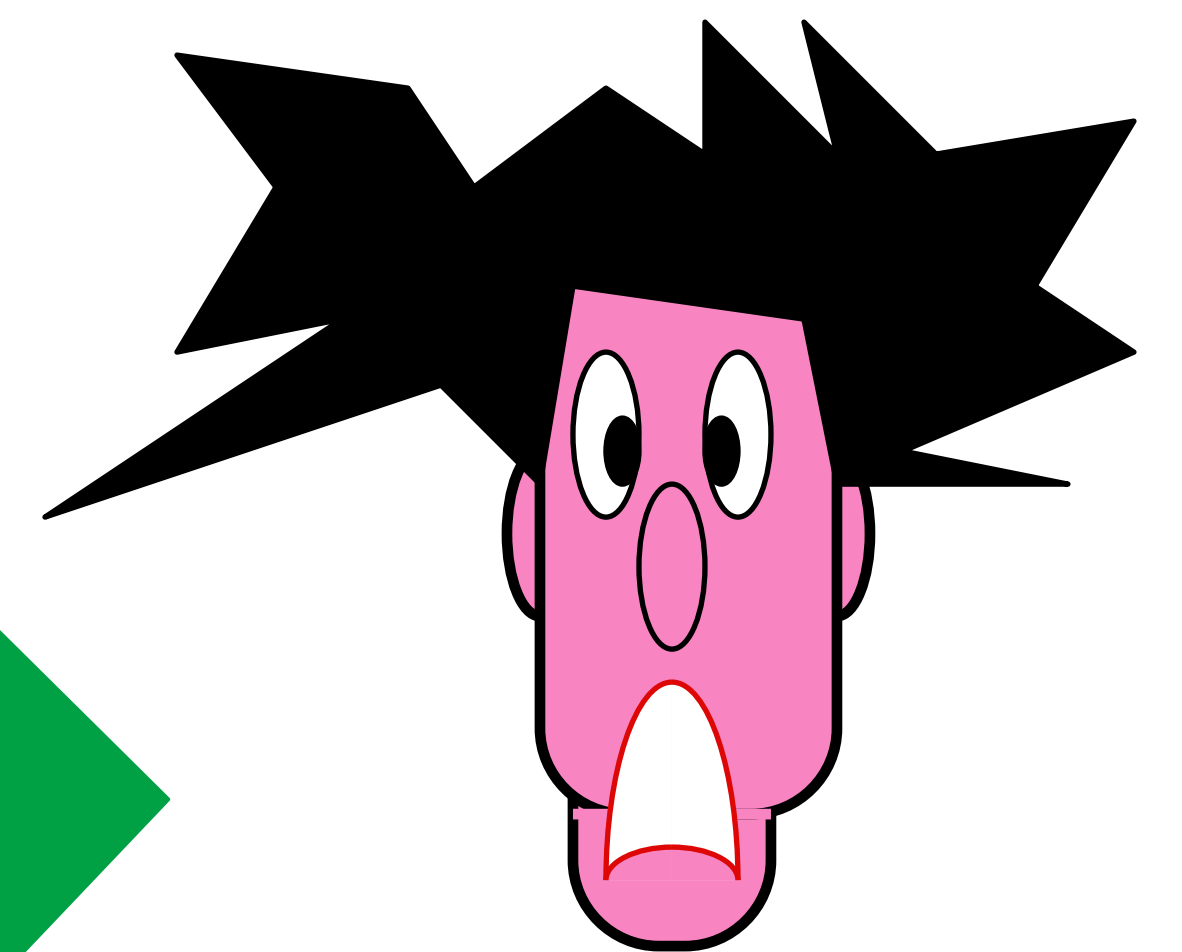
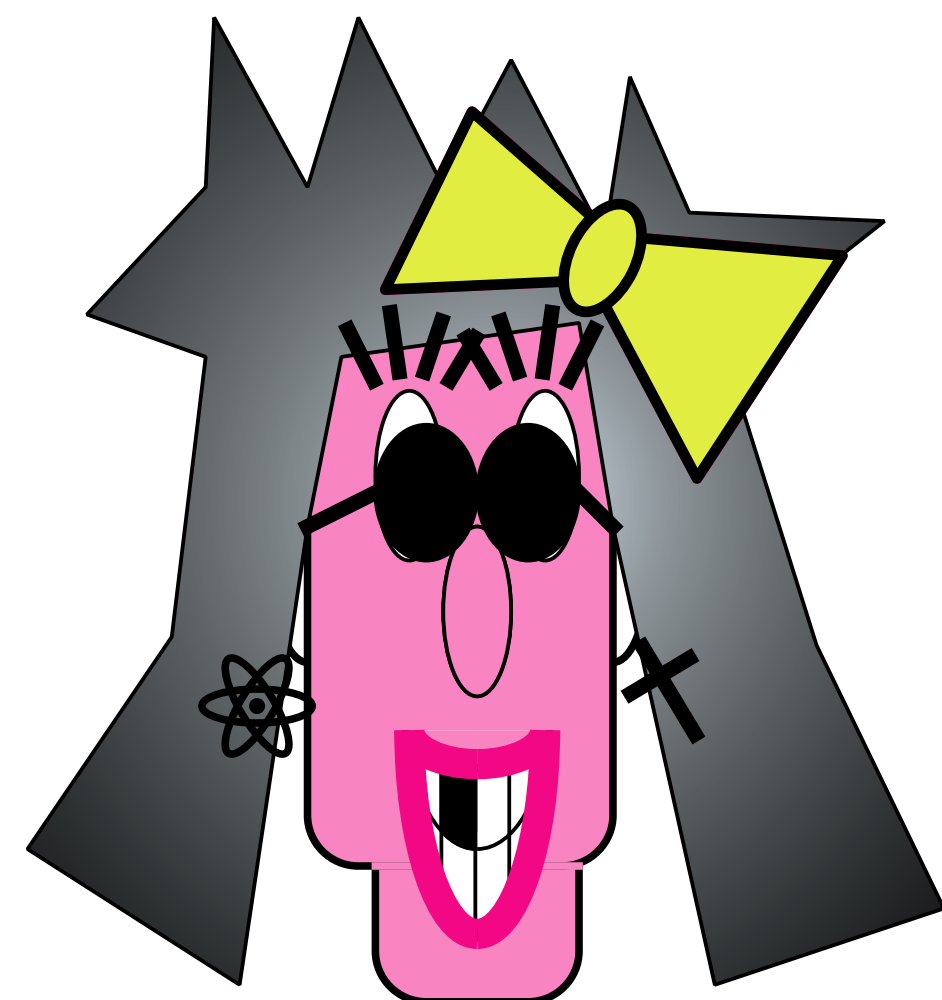
Ben-Or, Goldwasser, Kilian, Wigderson

# Quantumly



$\approx 85\%$  **NL**  $\rightarrow D_H(x \oplus z, b \cdot y) \approx 15\% n < n/5$

$b$   $x$



$D_H(x \oplus z, b \cdot y) < n/5?$

~~Ben-Or, Goldwasser, Kilian, Wigderson~~

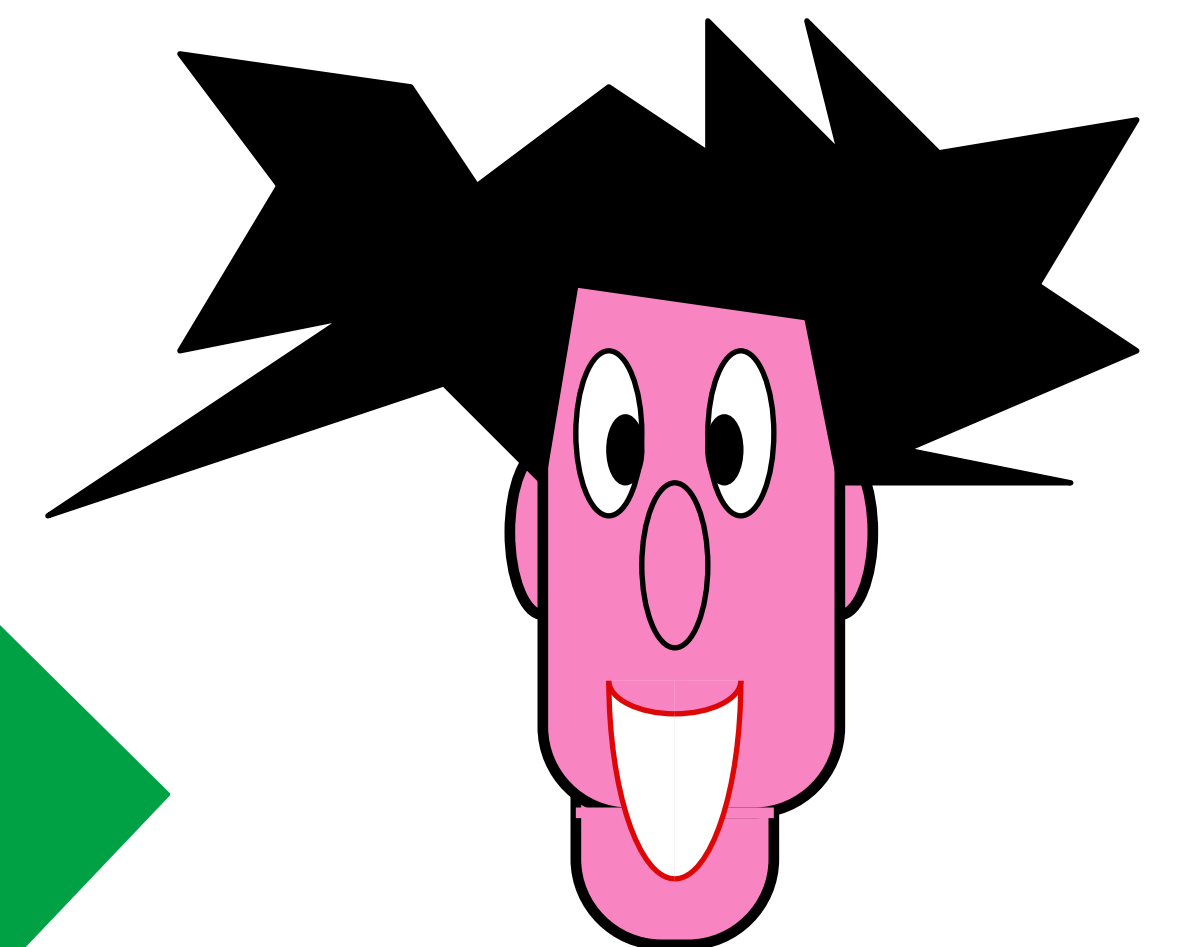
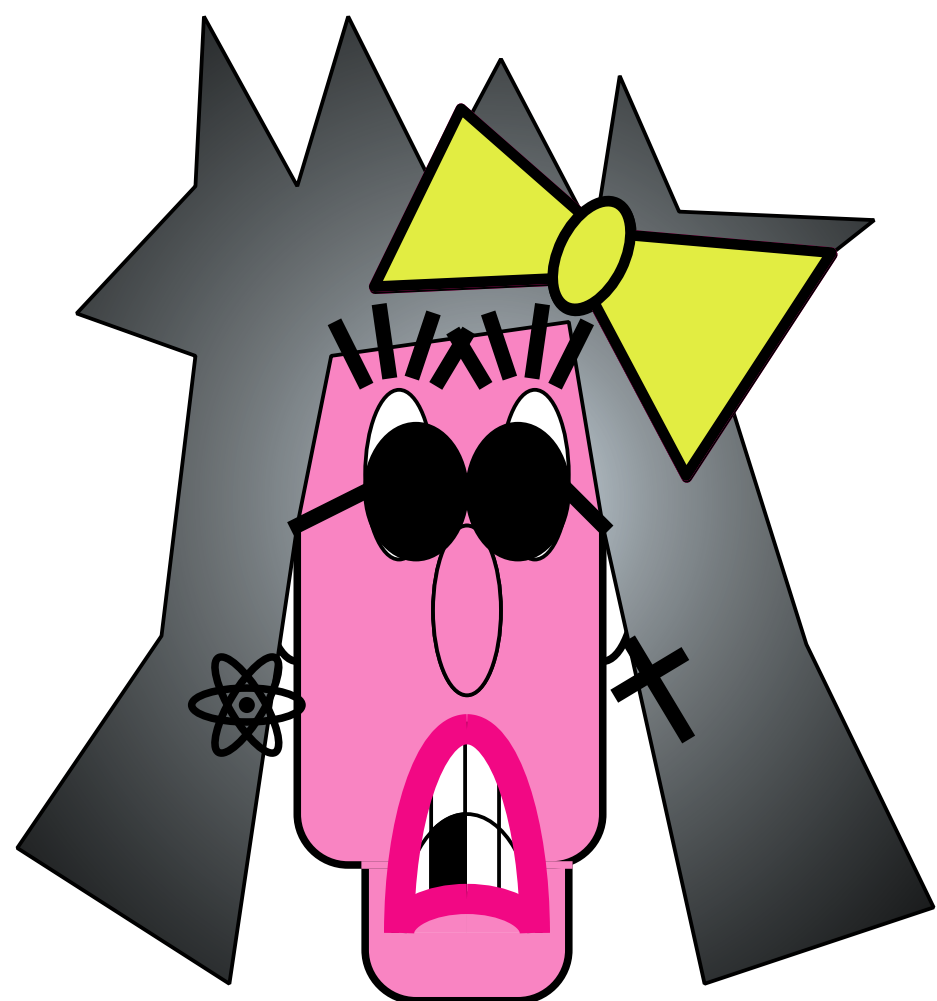
# Classically

$$D_H(x_0 \oplus z, 0 \cdot y) = D_H(x_0 \oplus z, 0) < n/5$$

$$D_H(x_1 \oplus z, 1 \cdot y) = D_H(x_1 \oplus z, y) < n/5$$

$$D_H(x_0 \oplus x_1, y) = D_H((x_0 \oplus z) \oplus (x_1 \oplus z), y) < 2n/5 < n/2$$

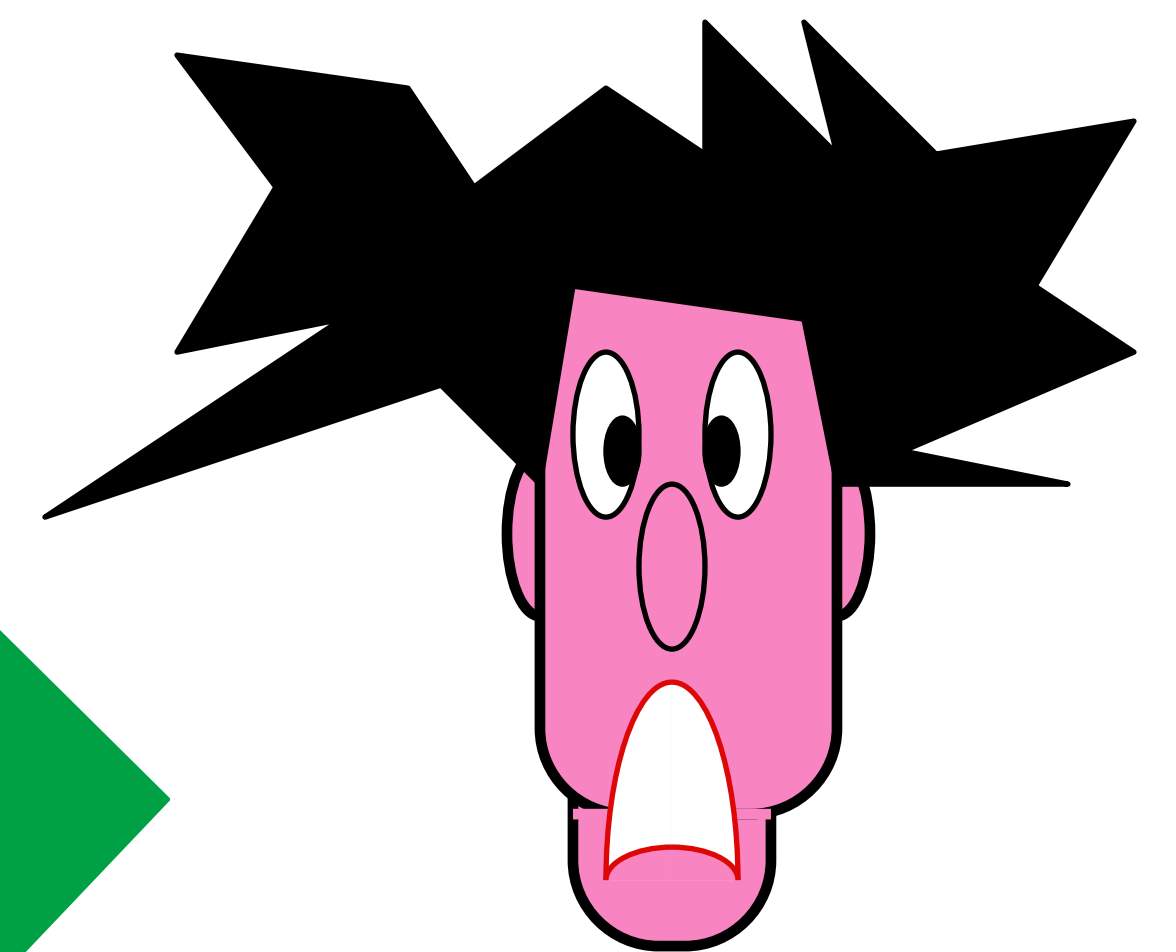
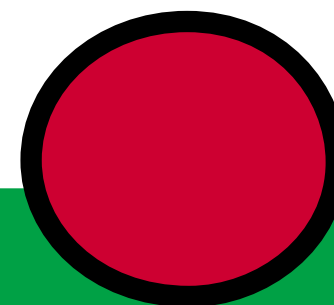
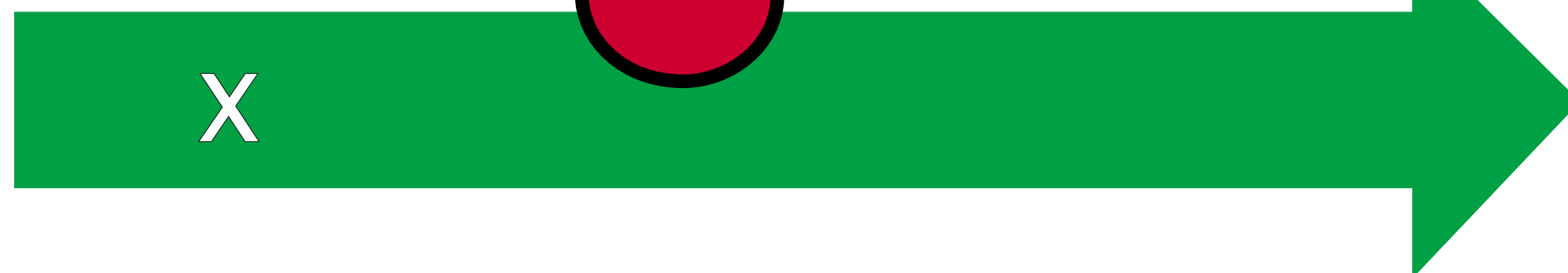
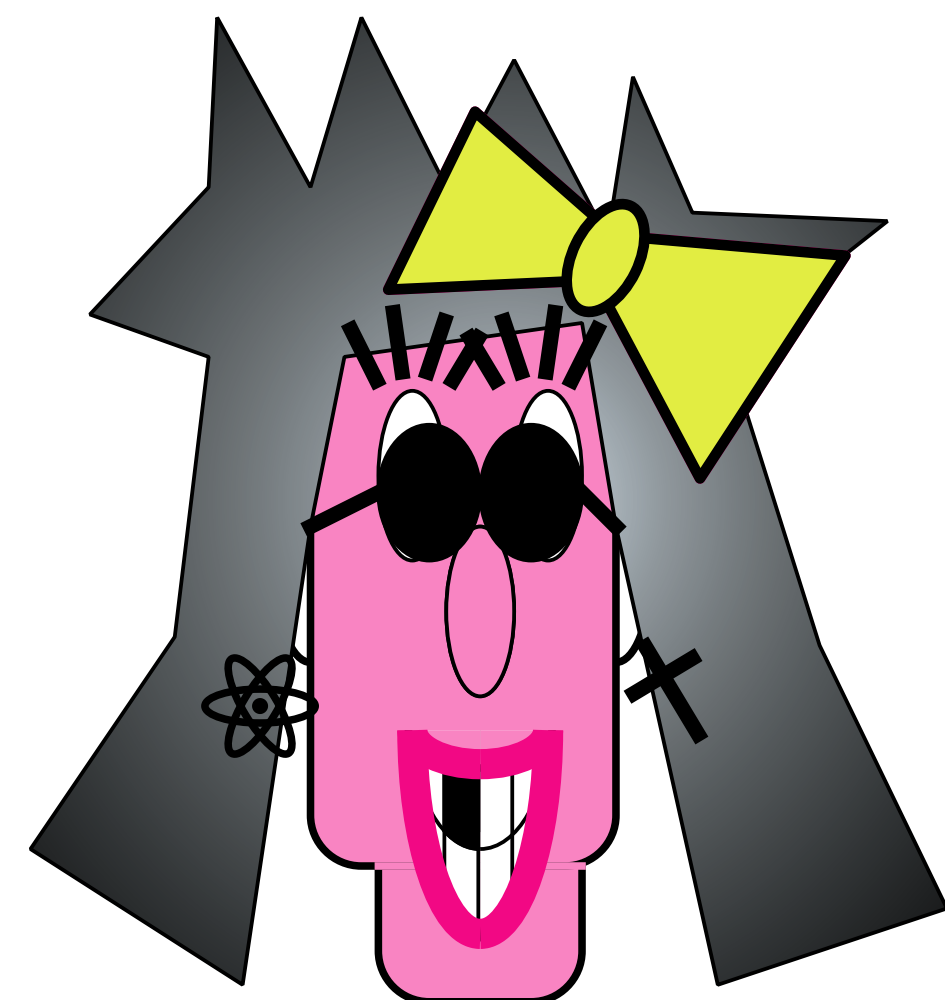
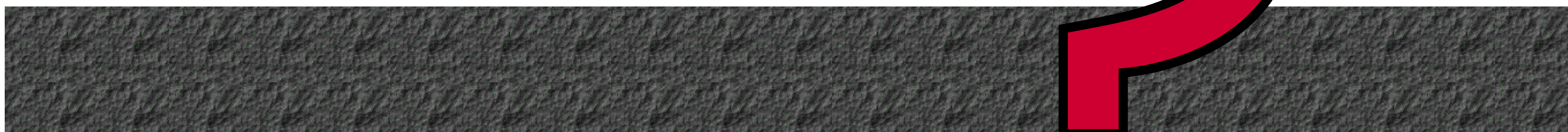
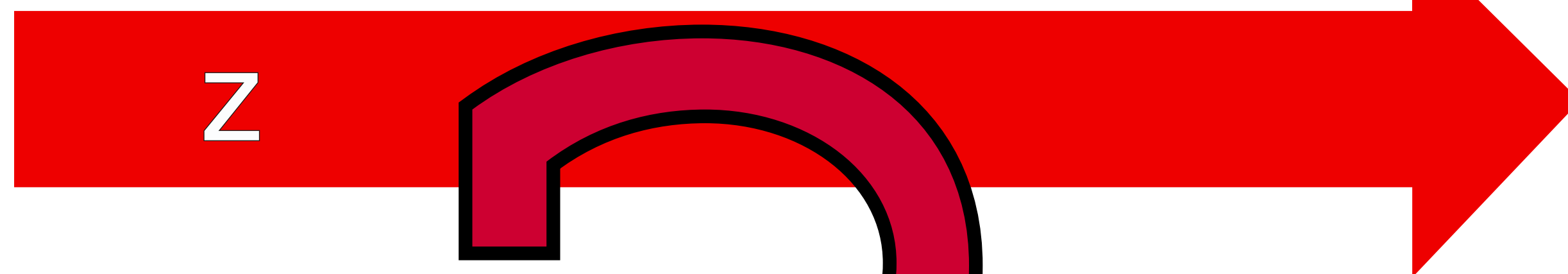
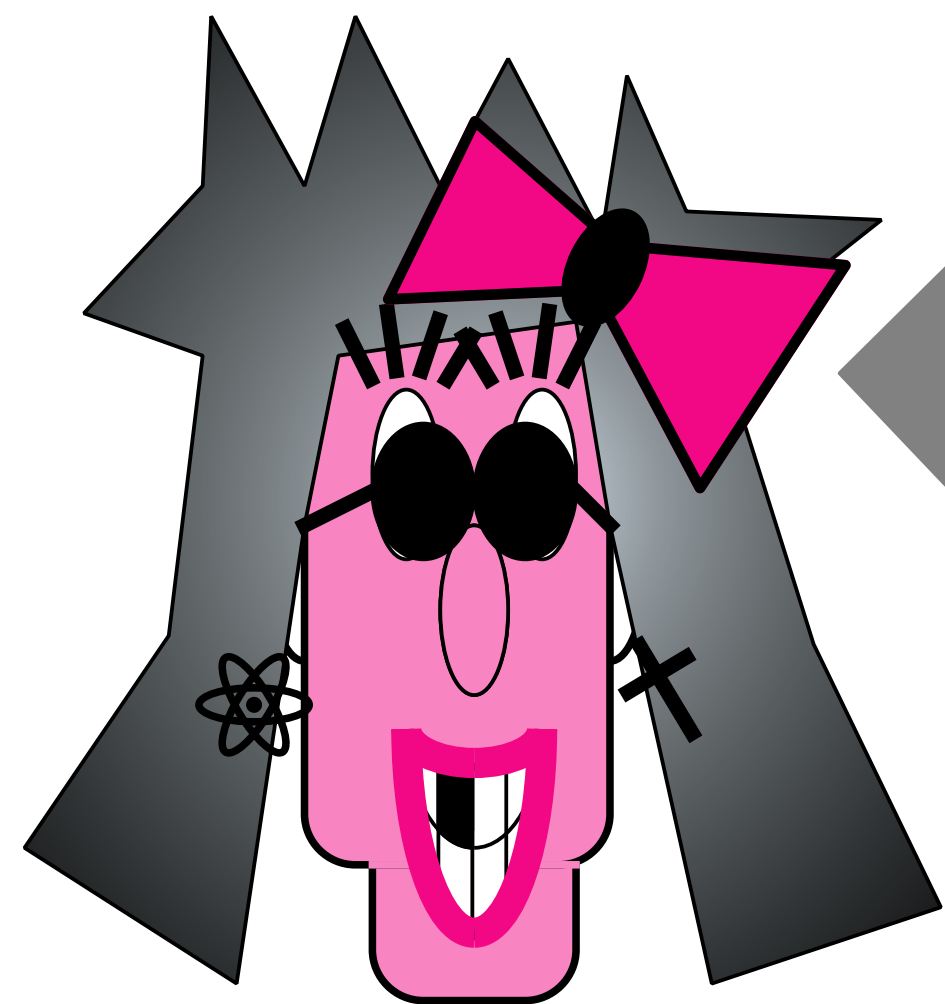
possible with prob. at most  $c^{-n}$



Ben-Or, Goldwasser, Kilian, Wigderson



# Quantumly



$$x \oplus z = b \cdot y$$

~~Ben-Or, Goldwasser, Kilian, Wigderson~~

**(8)**

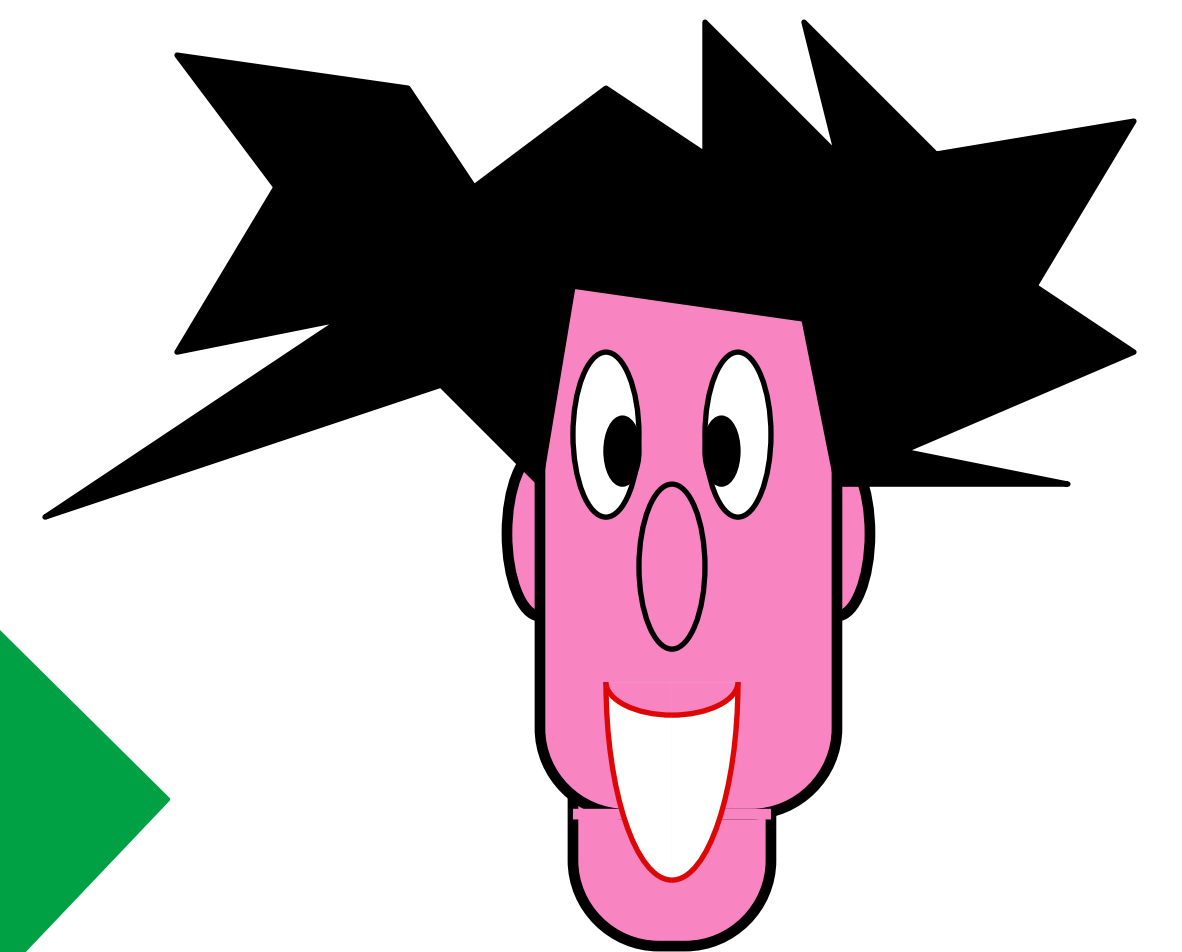
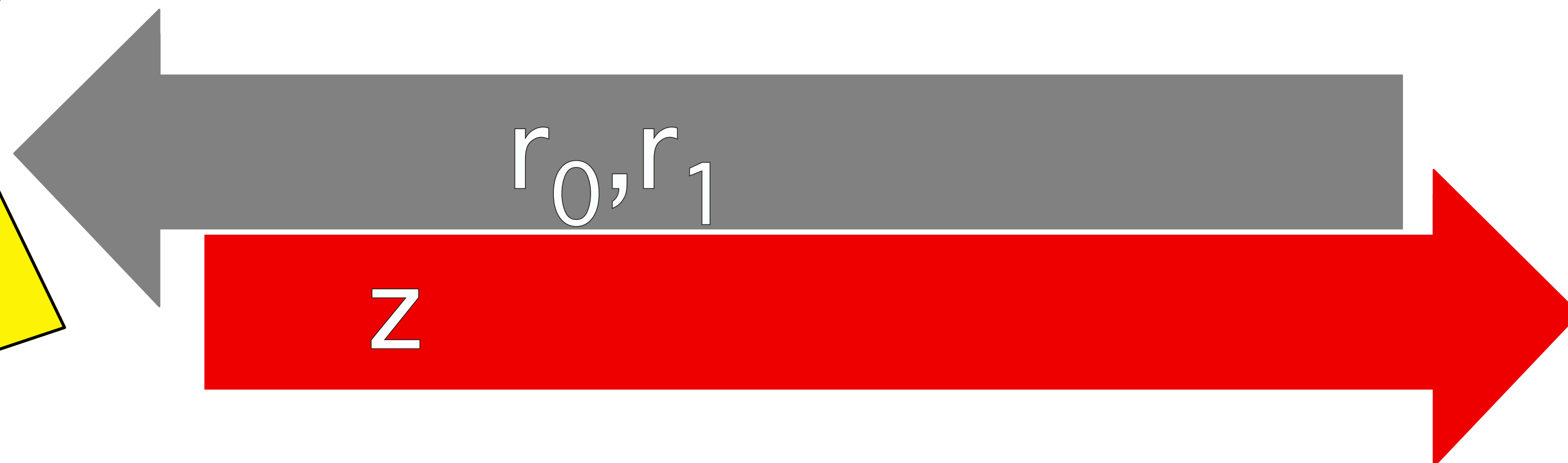
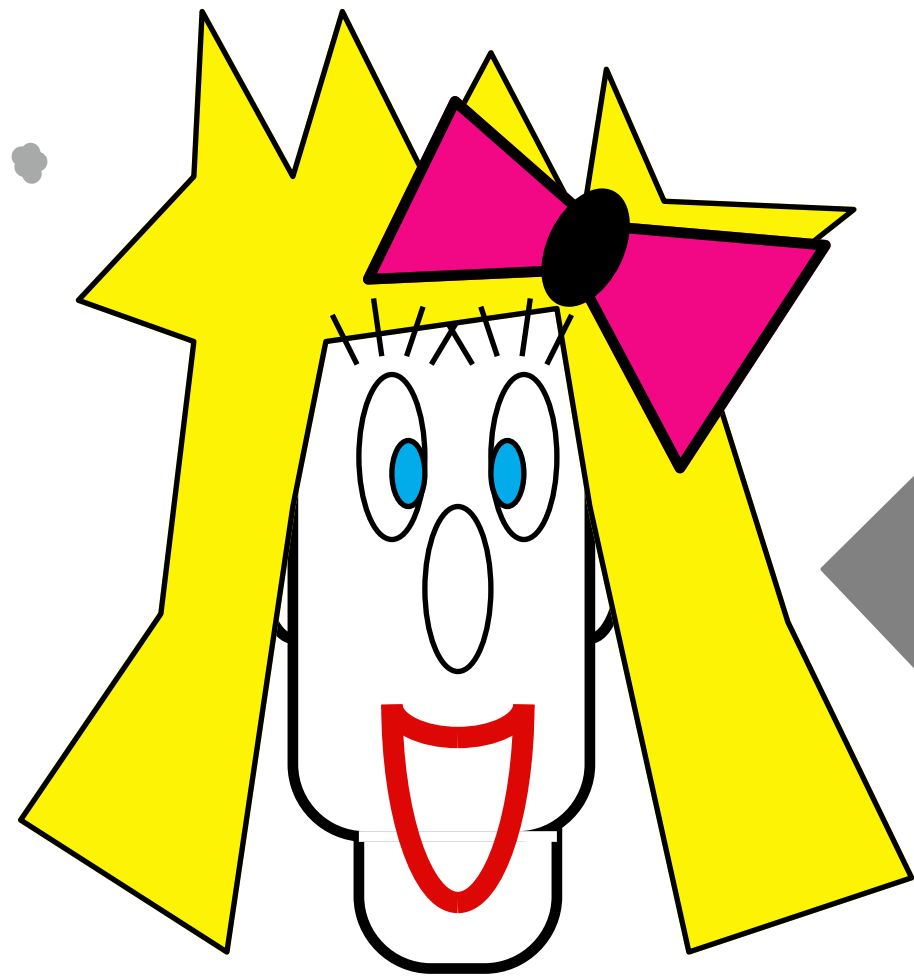
**two provers BC**

**Classically and**

**Quantumly Secure**

$$z = x \oplus r_b$$

b



$$x = z \oplus r_b ?$$



modified BGKW

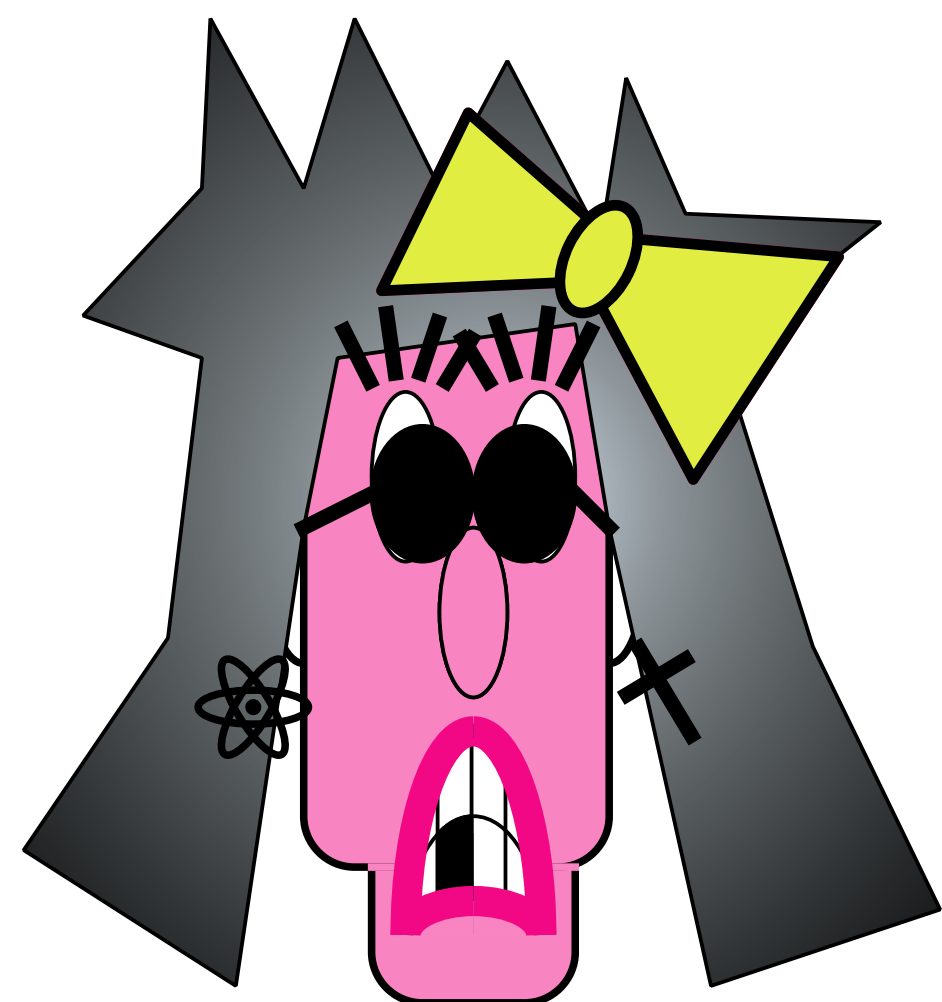
# Classically

$$x_0 \oplus z = r_0$$

$$x_1 \oplus z = r_1$$

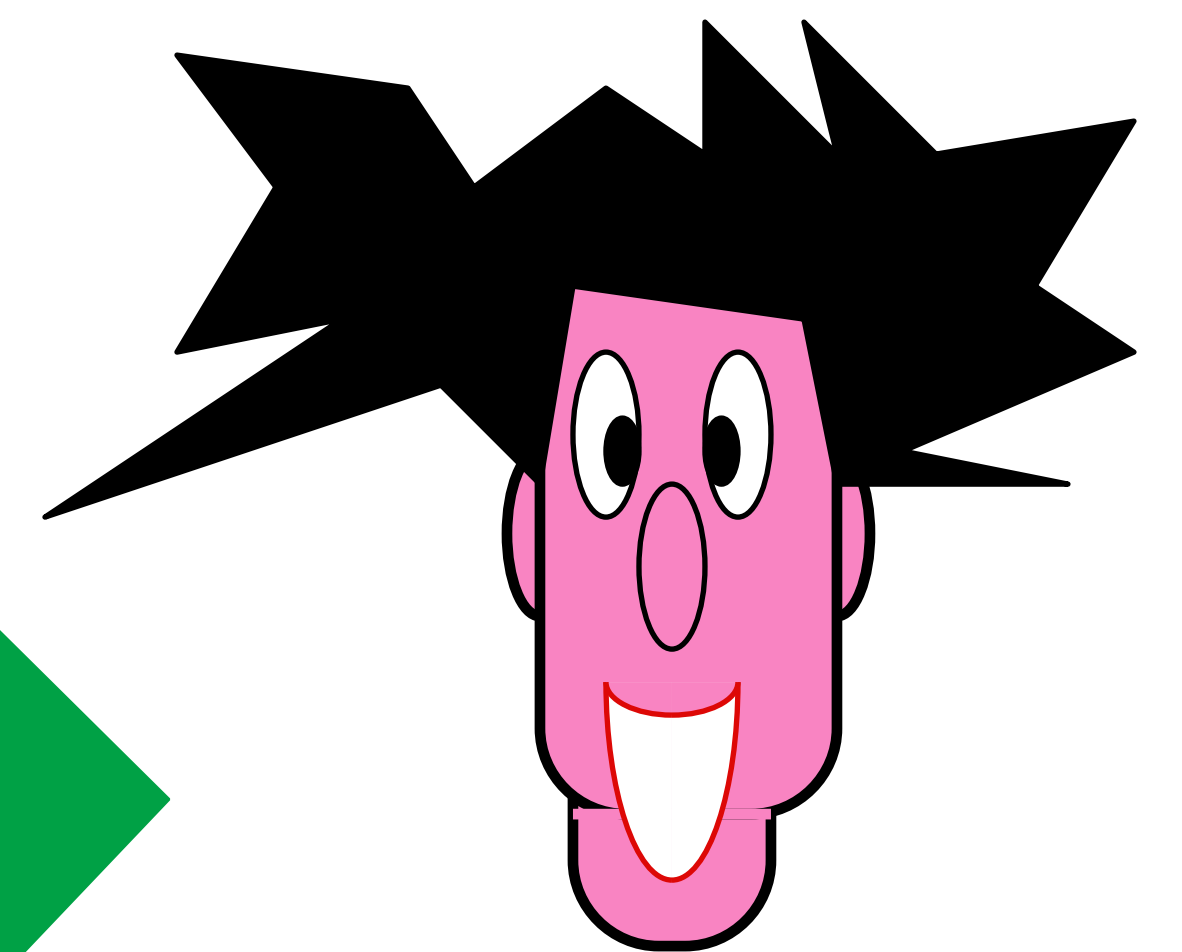
$$x_0 \oplus x_1 = (x_0 \oplus z) \oplus (x_1 \oplus z) = r_0 \oplus r_1$$

possible with prob. at most  $2^{-n}$



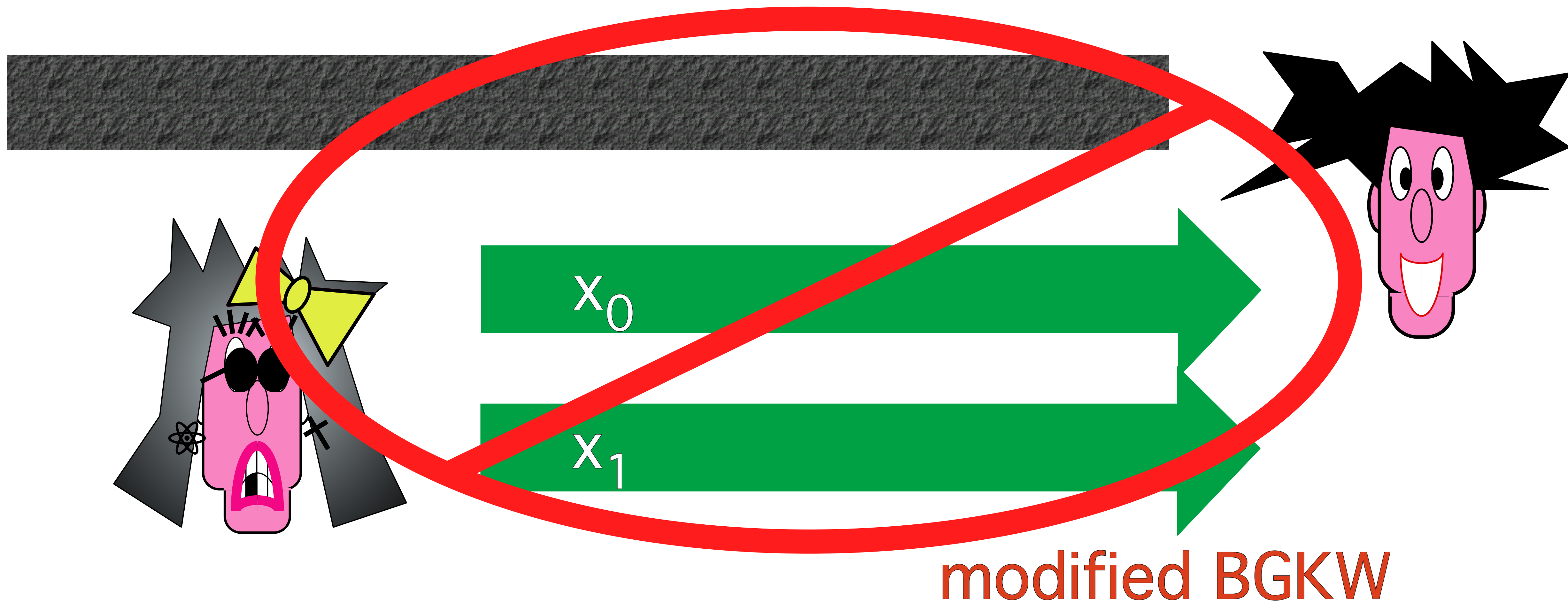
$x_0$

$x_1$



modified BGKW

# Quantumly



# Quantumly

## MAIN THEOREM

Let  $\mathbf{Z}$  and  $\mathbf{O}$  be POVMs such that outputs  $x_0$  and  $x_1$  one could obtain by applying one of them to the state shared among the two provers.

Suppose the success probability of unveiling is

$$p_0 + p_1 > 1 + \delta,$$

then the (prediction probability of  $y_0 \oplus y_1$ )  $> \delta$ .

This prediction probability is achieved by first applying  $\mathbf{Z}$  to the shared state followed by  $\mathbf{O}$  on the leftover system or the other way around.

Imagine that Peggy and Paula would like to be able to unveil a certain instance of  $b$  both as 0 and as 1. Our only assumption is that Paula knows nothing about  $r_0, r_1$ . Let them share an unlimited quantity of entanglement in any form they wish. Without loss of generality to unveil a zero the message of Paula is defined by the outcome  $w_0$  of a POVM  $\mathbb{Z} = \{Z_1^\dagger Z_1, \dots, Z_{2^n}^\dagger Z_{2^n}\}$  and to unveil a 1 by the outcome  $w_1$  of a POVM  $\mathbb{O} = \{O_1^\dagger O_1, \dots, O_{2^n}^\dagger O_{2^n}\}$ .

Each operator in a POVM is a positive matrix and can thus be decomposed into a linear combination of orthogonal projectors with coefficients between 0 and 1.

Let  $p_0$  be the probability of successfully unveiling 0 and  $p_1$  be the probability of successfully unveiling 1. Suppose there exists a pair of POVMs where  $p_0 + p_1 > 1$ . We show that any quantum player can then obtain *both* classical strings  $w_0, w_1$  to unveil both values with probability strictly greater than zero. Notice that if we manage to make the probability of getting both strings  $w_0, w_1$  greater than  $1/2^n$ , then Paula can compute  $r_0 \oplus r_1 = w_0 \oplus w_1$  better than at random. This implies communication between Peggy and Paula, which is impossible by hypothesis.



The strategy of Paula is simply to perform both measurements, one after the other. Let's denote her state by  $\rho$ . Assume the right outcome for unveiling a zero is  $w_0$  and the right outcome for unveiling a one is  $w_1$ .

The probability to obtain  $w_0$  if  $\mathbb{Z}$  is measured is

$$p_0 = \text{Tr}(Z_{w_0}^\dagger Z_{w_0} \rho)$$

and the state becomes

$$Z_{w_0} \rho Z_{w_0}^\dagger / p_0.$$

The probability to obtain  $w_1$  if  $\mathbb{O}$  is measured is

$$p_1 = \text{Tr}(O_{w_1}^\dagger O_{w_1} \rho)$$

and the state becomes

$$O_{w_1} \rho O_{w_1}^\dagger / p_1.$$

If  $\mathbb{O}$  is measured after  $\mathbb{Z}$  the probability to obtain  $w_0$  and  $w_1$  is given by

$$p_{01} = p_0 \text{Tr}[O_{w_1}^\dagger O_{w_1} Z_{w_0} \rho Z_{w_0}^\dagger / p_0] = \text{Tr}[O_{w_1}^\dagger O_{w_1} Z_{w_0} \rho Z_{w_0}^\dagger]$$

If  $\mathbb{Z}$  is measured after  $\mathbb{O}$  the probability to obtain  $w_1$  and  $w_0$  is given by

$$p_{10} = p_1 \text{Tr}[Z_{w_1}^\dagger Z_{w_1} O_{w_0} \rho O_{w_0}^\dagger / p_1] = \text{Tr}[Z_{w_1}^\dagger Z_{w_1} O_{w_0} \rho O_{w_0}^\dagger]$$

Both  $p_{01}$  and  $p_{10}$  must be smaller or equal to  $1/2^n$  otherwise Paula learns something about  $r_0 \oplus r_1 = w_0 \oplus w_1$  (which is impossible without communication).

Having all this in mind, consider the following sequence of implications:

$$\begin{aligned}
 p_{01} + p_{10} &\leq 1/2^{n-1} \\
 Tr[O_{w_1}^\dagger O_{w_1} Z_{w_0} \rho Z_{w_0}^\dagger] + Tr[Z_{w_1}^\dagger Z_{w_1} O_{w_0} \rho O_{w_0}^\dagger] &\leq 1/2^{n-1} \\
 Tr[(I - (I - O_{w_1}^\dagger O_{w_1})) Z_{w_0} \rho Z_{w_0}^\dagger] + Tr[(I - (I - Z_{w_1}^\dagger Z_{w_1})) O_{w_0} \rho O_{w_0}^\dagger] &\leq 1/2^{n-1} \\
 Tr[Z_{w_0} \rho Z_{w_0}^\dagger] - Tr[(I - O_{w_1}^\dagger O_{w_1}) Z_{w_0} \rho Z_{w_0}^\dagger] + \\
 Tr[O_{w_0} \rho O_{w_0}^\dagger] - Tr[(I - Z_{w_1}^\dagger Z_{w_1}) O_{w_0} \rho O_{w_0}^\dagger] &\leq 1/2^{n-1}
 \end{aligned}$$

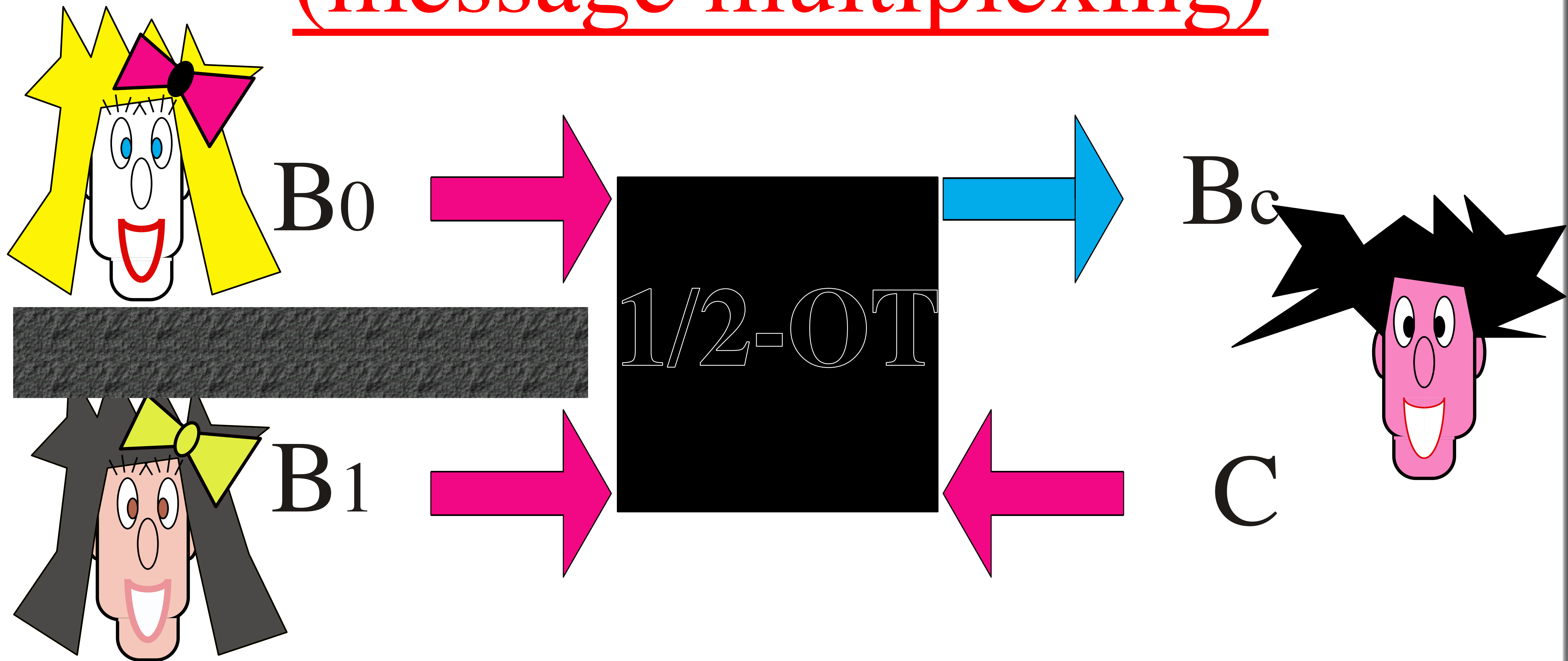
Using that  $p_0 = Tr(Z_{w_0}^\dagger Z_{w_0} \rho)$  and  $p_1 = Tr(O_{w_1}^\dagger O_{w_1} \rho)$  we get

$$\begin{aligned}
 p_0 + p_1 &\leq Tr[(I - O_{w_1}^\dagger O_{w_1}) Z_{w_0} \rho Z_{w_0}^\dagger] + Tr[(I - Z_{w_1}^\dagger Z_{w_1}) O_{w_0} \rho O_{w_0}^\dagger] + 1/2^{n-1} \\
 p_0 + p_1 &\leq Tr[I - O_{w_1}^\dagger O_{w_1}] + Tr[I - Z_{w_1}^\dagger Z_{w_1}] + 1/2^{n-1} \\
 p_0 + p_1 &\leq (1 - p_0) + (1 - p_1) + 1/2^{n-1} \\
 2(p_0 + p_1) &\leq 2 + 1/2^{n-1} \\
 p_0 + p_1 &\leq 1 + 1/2^n
 \end{aligned}$$

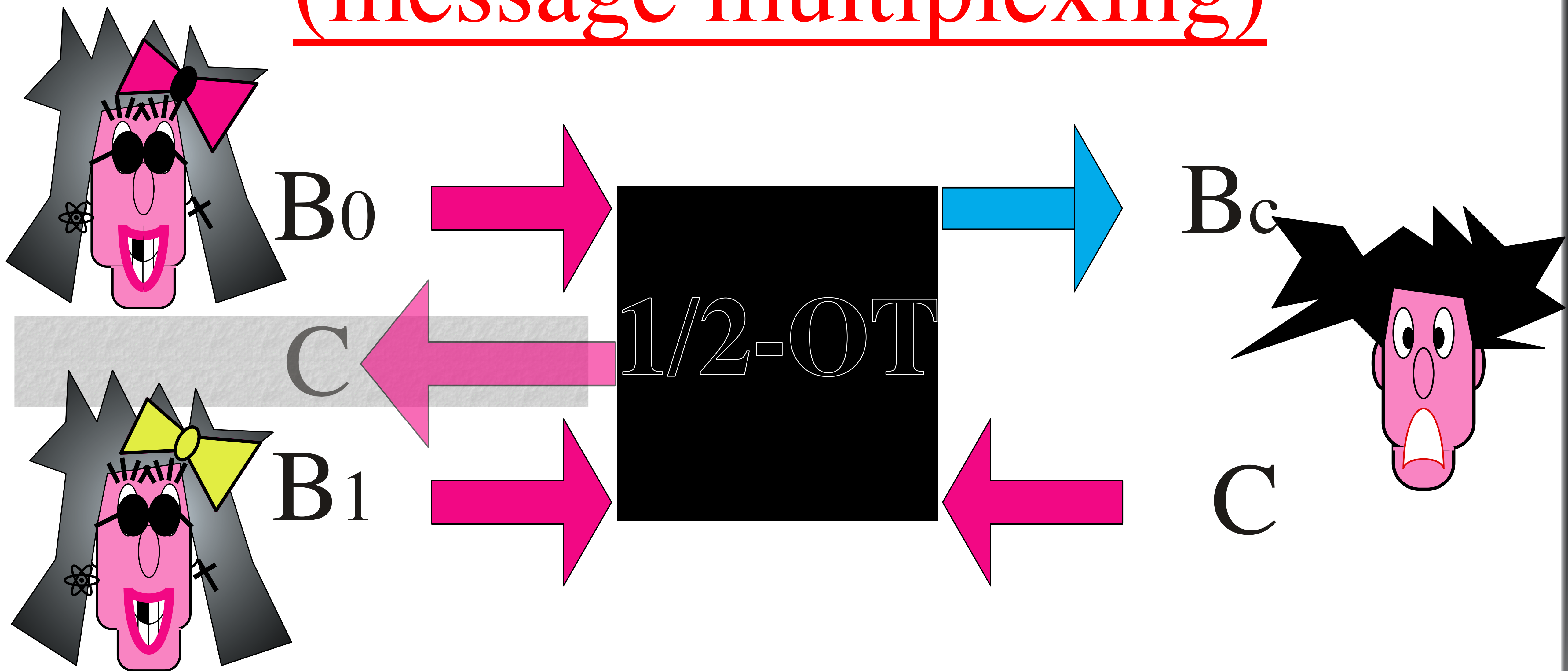
This last statement means that the probability of cheating the bit commitment scheme is only exponentially little better than in the honest case. This is the best we could hope for because this value is reached by Peggy-Paula acting nearly honestly: Peggy and Paula act honestly except that when Paula unveils if she wish to unveil the opposite bit to Peggy she sends a random string instead of  $w$ . With probability  $1/2^n$  she succeeds in unveiling the opposite bit.

**(9)**  
**WARNING!**

# Oblivious Transfer (message multiplexing)

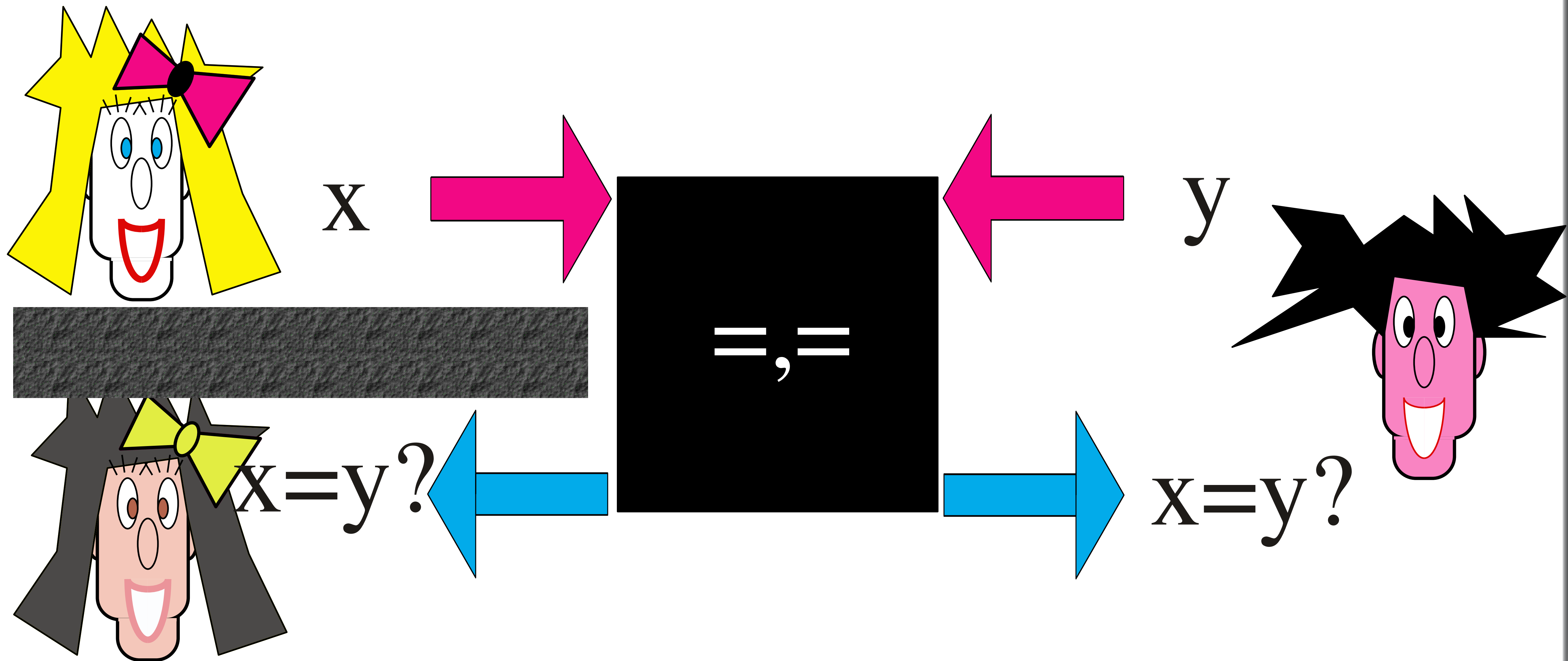


# Oblivious Transfer (message multiplexing)



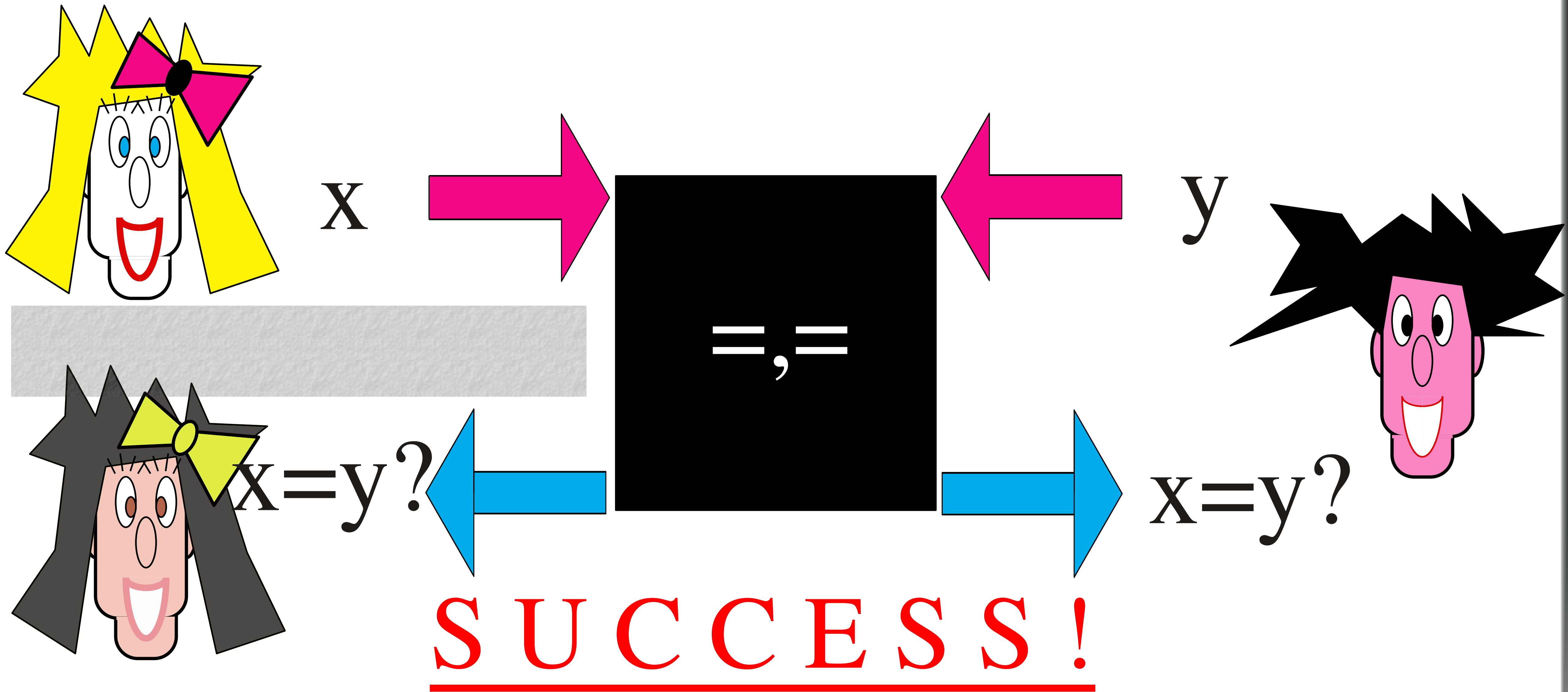
Brassard, Crépeau, Mayers, Salvail 97

# Mutual Identification

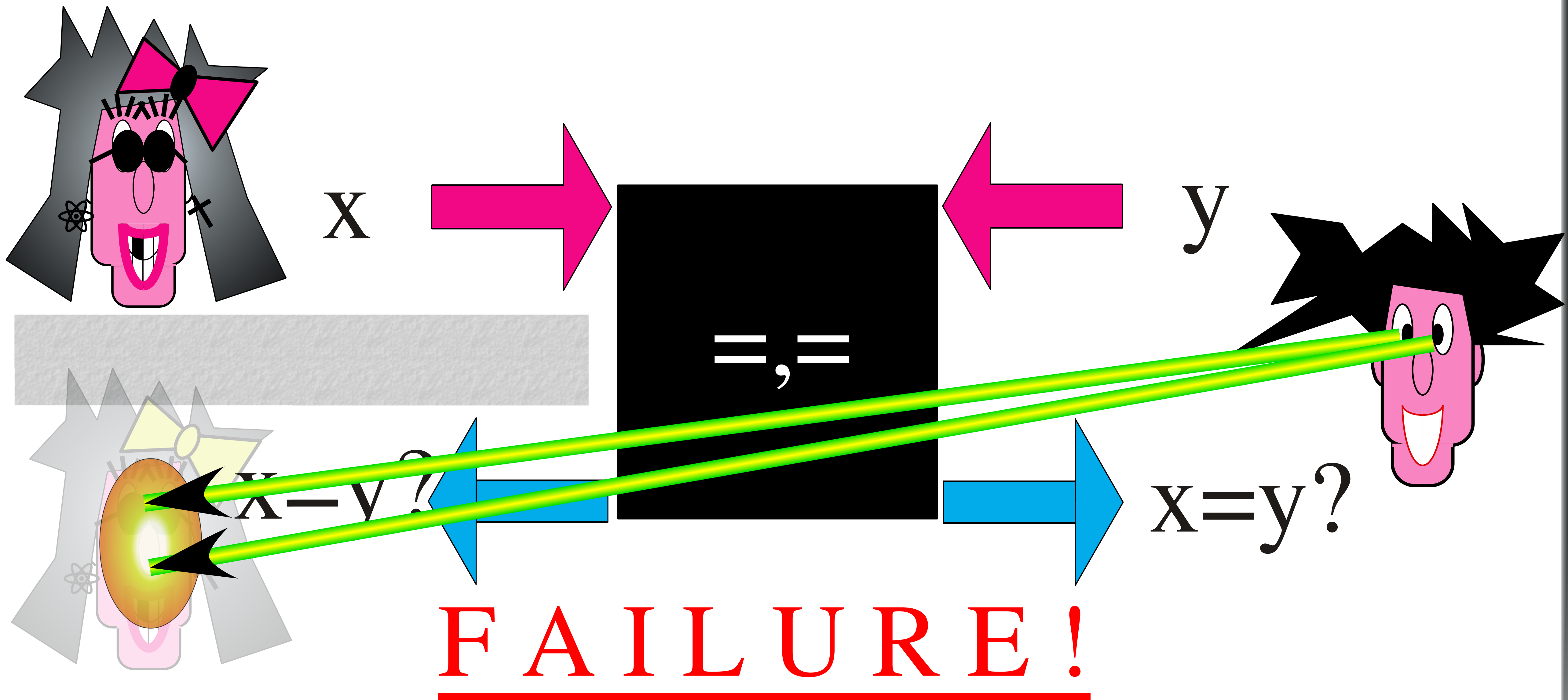




# Mutual Identification



# Mutual Identification

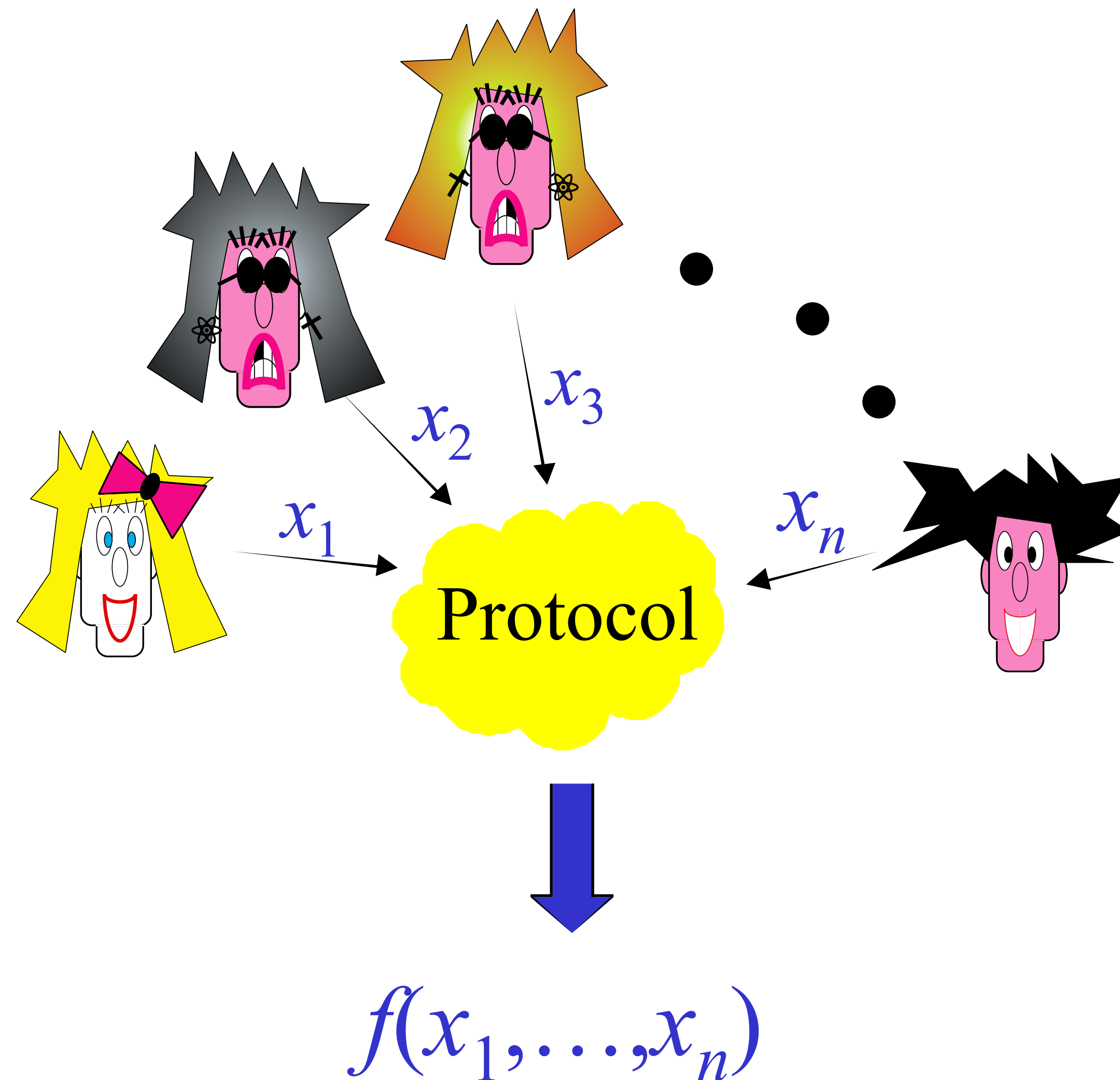




# **(10) Classical Multi-party Computing**

# Classical Multi-party Computing

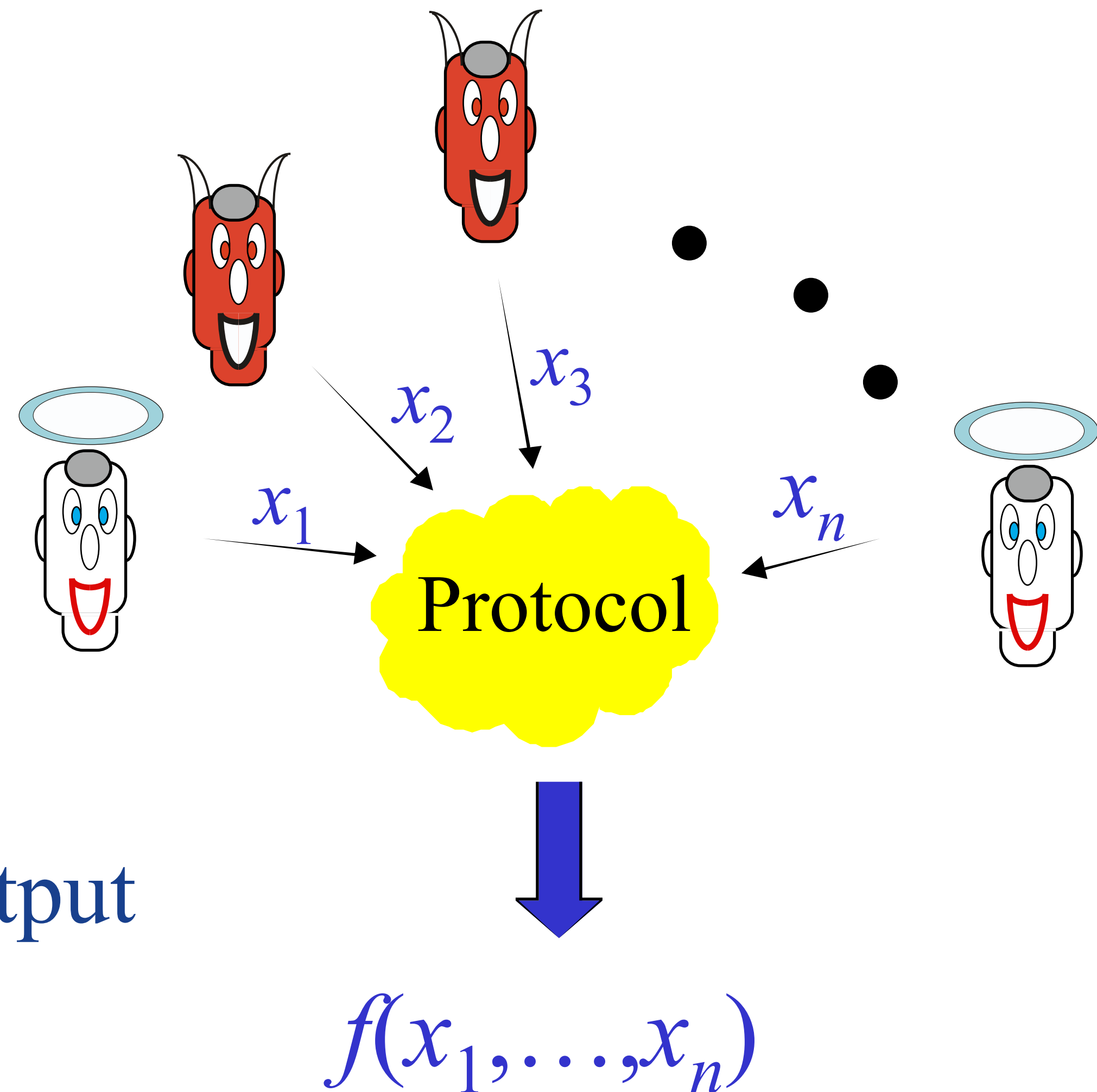
- Network of  $n$  players
- Each has input  $x_i$
- Want to compute  $f(x_1, \dots, x_n)$  for some known function  $f$
- *E.g. electronic voting*



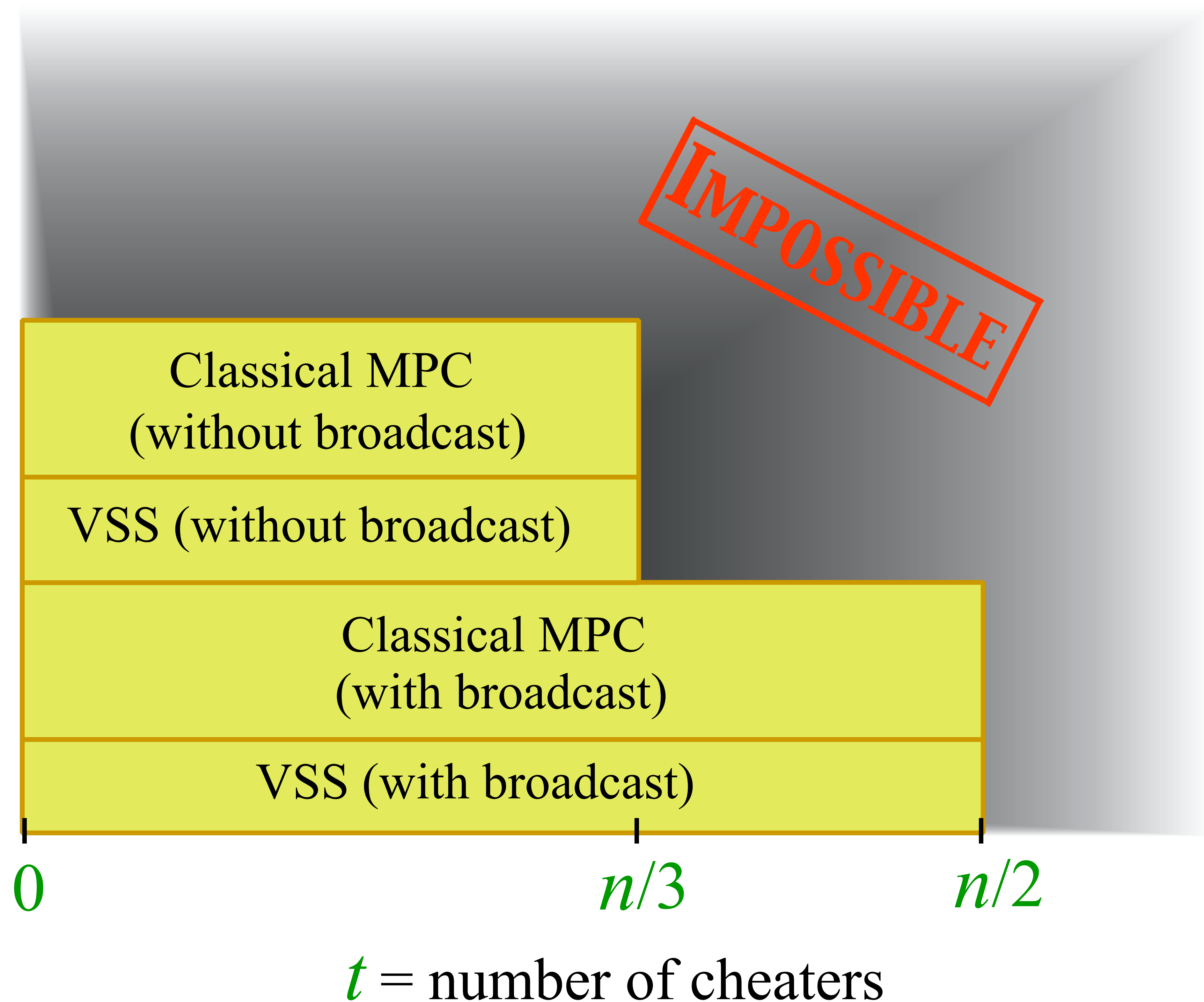
# Classical Multi-party Computing

Even if  $t$  out of  $n$  players try to cheat:

1. Cheaters **learn nothing** (except **output**)
2. Cheaters **cannot affect output** (except by choice of input)



# Results



# **(11) Multi-Party Quantum Computing**

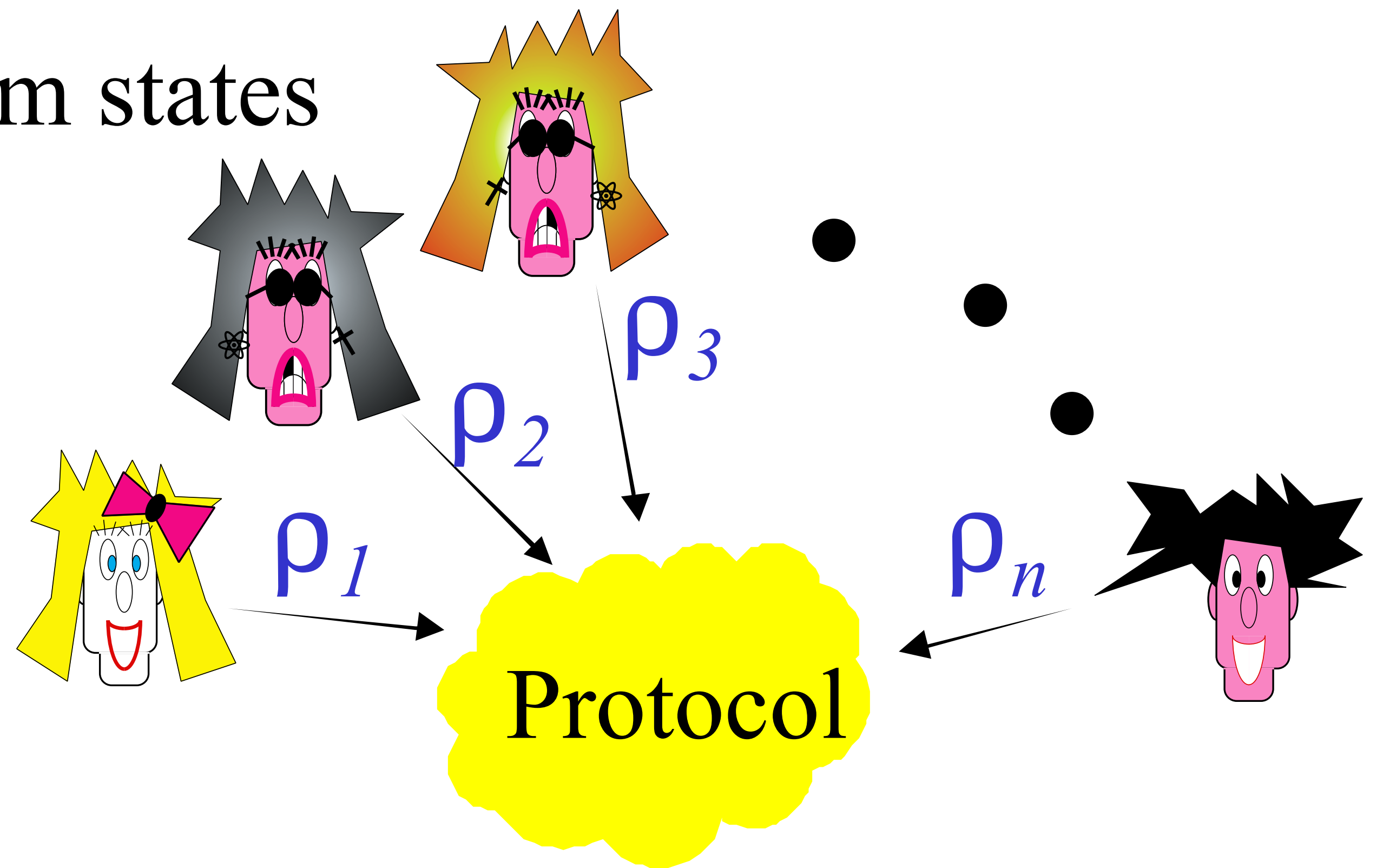


# Multi-party Quantum Computing

- Players' inputs are quantum states

- Possibly entangled
- No description necessary (protocol is “oblivious”)

- Output is quantum
- Want to evaluate a known quantum circuit  $U$
- Player  $i$  gets  $i$ -th component of output



# Multi-party Quantum Computing

- Players' inputs form an arbitrary state

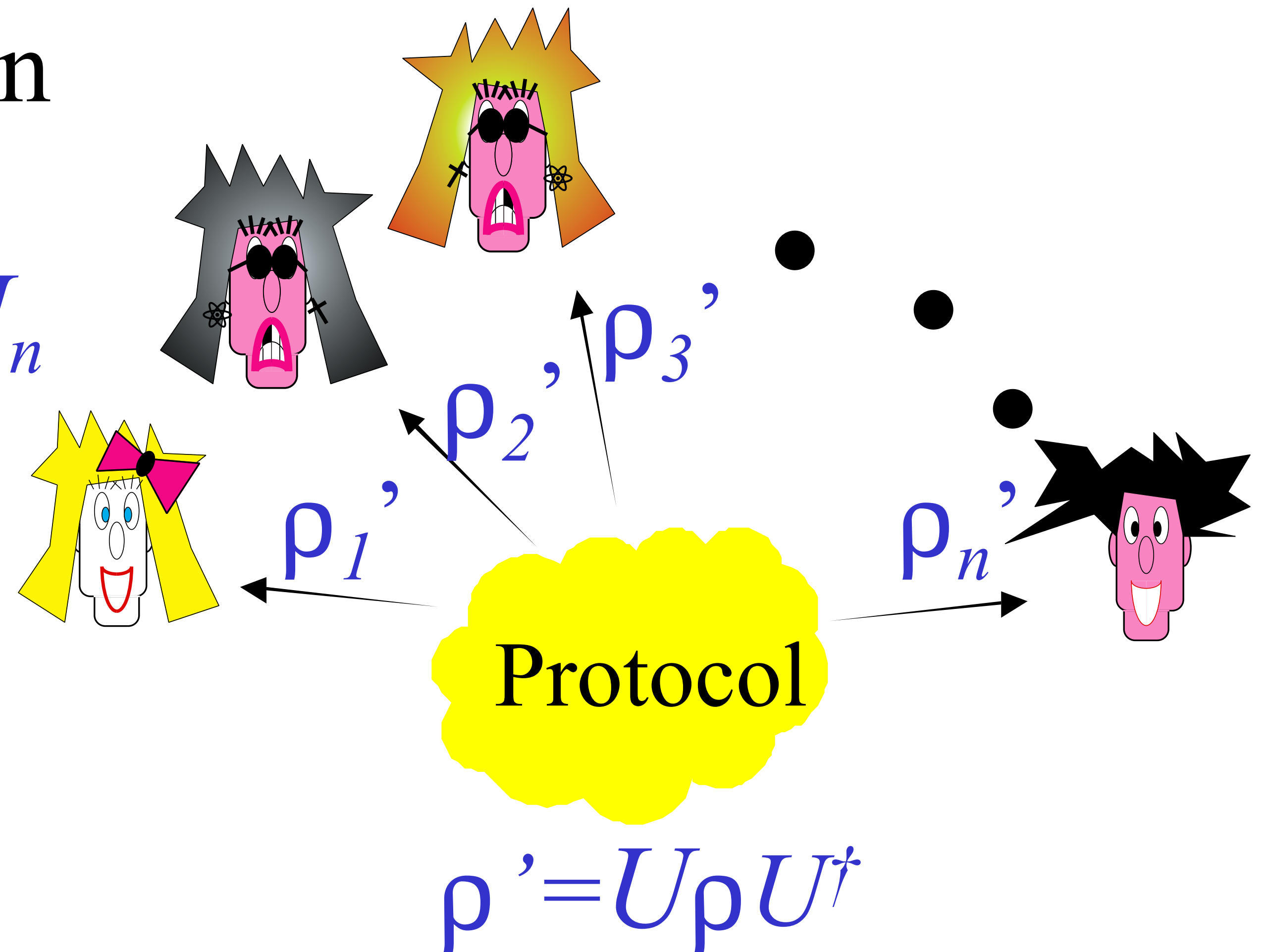
$$\rho \text{ in } H_1 \otimes H_2 \otimes \dots \otimes H_n$$

- Player  $i$  holds  $i$ -th component:

$$\rho_i$$

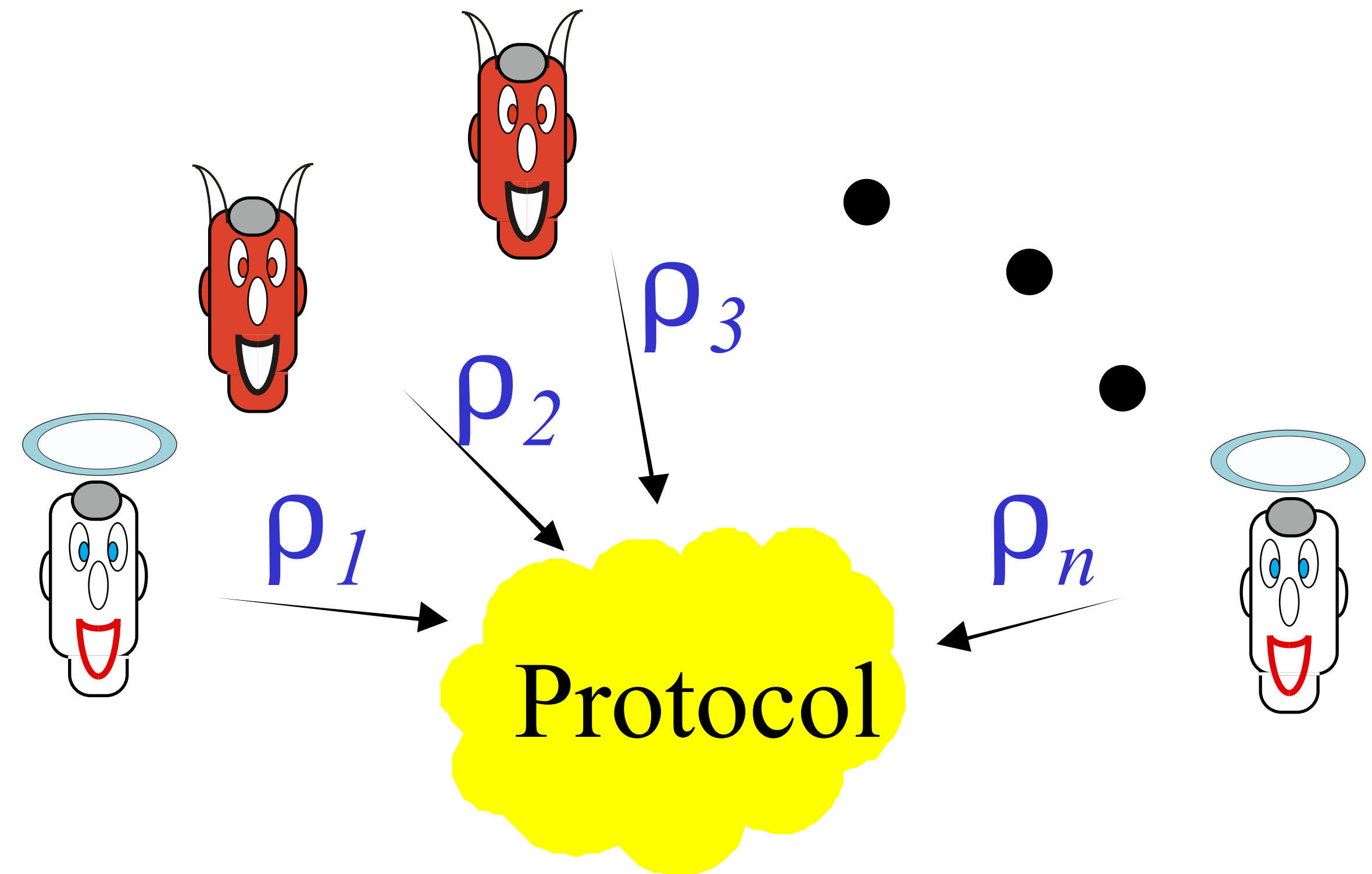
- Each player gets one output:

$$\rho_i' = (U\rho U^\dagger)_i$$



# Multi-party Quantum Computing

Even if  $t$  out of  $n$   
players try to cheat:



1. Cheaters **learn nothing**  
(except **output**)
2. Cheaters **cannot affect output**  
(except by choice of inputs)

## Results

- $t < n/6$ :

Any Multi-party Quantum Computation

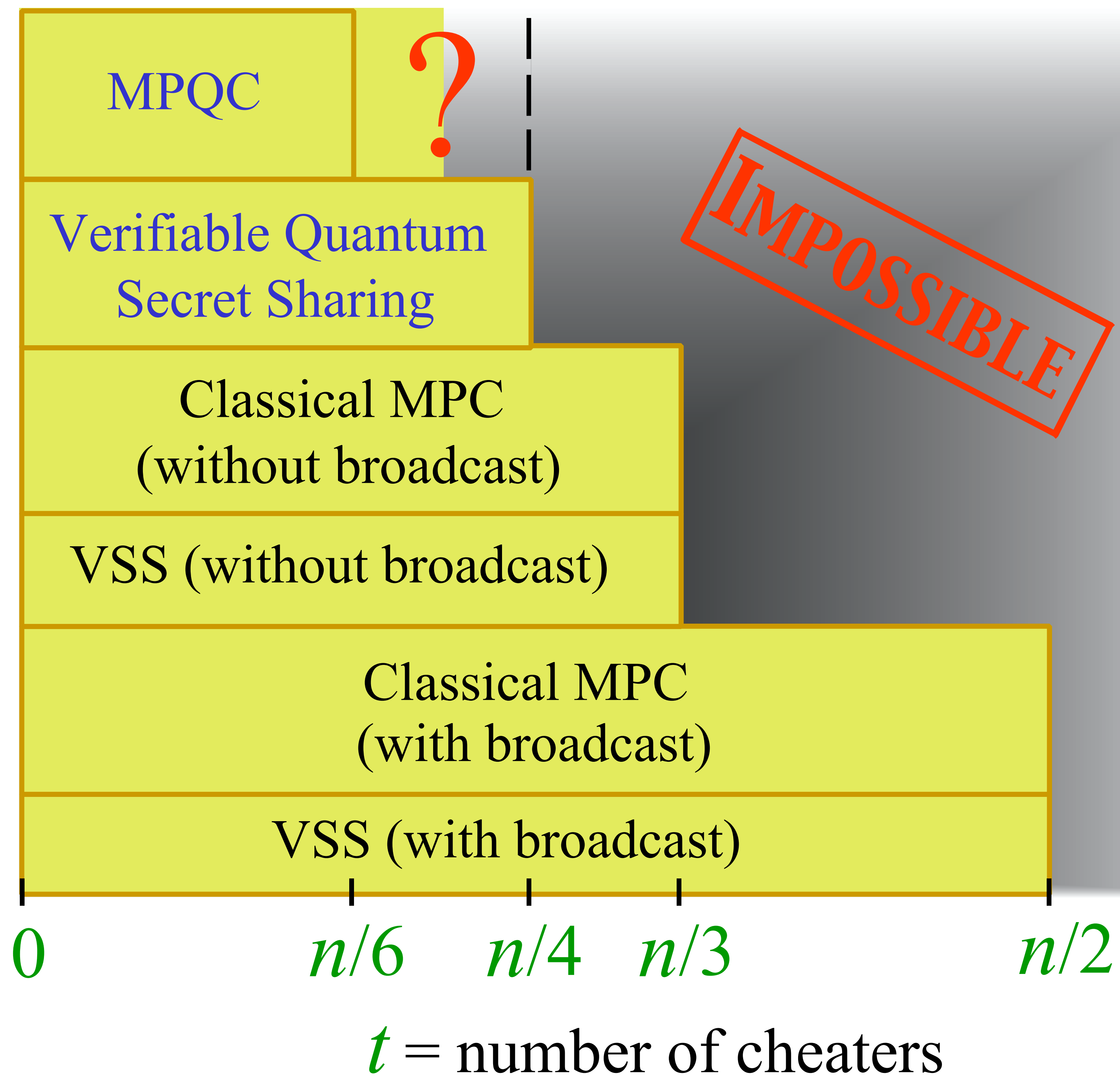
- $t < n/4$ :

Verifiable Quantum Secret-Sharing

- $t \geq n/4$ :

Even (perfect) VQSS is impossible

# Results



# MPQC and Fault-Tolerant Computing

- MPQC is like FTQC with a different error model...

	FTQC	MPQC
Type of errors	randomly spread, independent	maliciously placed, entangled with data
Error location	Can occur anywhere	At most $t$ positions

- Similar protocol techniques:

Classical MPC [BGW, CCD] → FTQC [AB99] → MPQC [CGS]

- Different proof techniques

(Need different notion of “proximity” to coding subspaces)

an Introduction to  
theoretical quantum  
CRYPTOGRAPHY

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